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# Quantifying the differences between gravity reduction techniques

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**Abstract.** Gravity data processing (reduction) generally utilises the best-available formulae. New and improved formulae have been introduced over time and the resulting newly processed gravity will not match the old. Additionally, mistakes made in the gravity reduction process, as well as the incompatibilities between various equations, will inevitably lead to errors in the final product. This can mean that overlapping gravity surveys are often incompatible, leading to incorrect geological interpretations. In this paper I demonstrate the magnitude of change that results when different information is introduced at various stages of the gravity reduction process. I have focussed on differences relating to calibration factors, time zones and time changes, height, geodetic datums, gravity datums and the equations involved therein. The differences range from below the level of detection (0.01 mGal) to over 16.0 mGal.

The results not only highlight the need to be diligent and thorough in processing gravity data, but also how it is necessary to document the steps taken when processing data. Without proper documentation, gravity surveys cannot be reprocessed should an error be identified.

Key words: error, geodesy, gravity, processing, reduction.

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## Introduction

A common product of Australian state and territory geological surveys is a regional Bouguer gravity map. These images are compilations of multiple gravity surveys and it is an ongoing problem that overlapping surveys rarely match. Most commonly there appears to be an offset between the surveys, leading to mismatched points and anomalies in the final image. Numerous attempts have been undertaken to create a smooth image of the gravity in South Australia using merging tools and different gridding algorithms (e.g. Heath et al., 2012), but to date a perfect image hasn't been created.

There are multiple reasons that surveys might mismatch. Different resolutions from different gravity meters as well as different precision and accuracy in elevation measurement techniques are two common issues. Another issue is how the data are processed. The process of gravity reduction is straightforward; however, at each step of the process decisions need to be made regarding which formulae to use, which gravity and geodetic datum is required and so on. This paper attempts to quantify some of the differences involved in using different equations.

Multiple software packages exist (e.g. Intrepid Geophysics & Geosoft) that have the ability to process raw gravity data. In order to have full control over the reduction process I have constructed a simple spreadsheet to undertake reduction in the field or in the office with minimal effort and to avoid software licensing issues. (The spreadsheet has been tested by undertaking gravity reduction using similar software and comparing results. The approach has allowed me to analyse the differences involved at different stages of the gravity reduction process should erroneous information be input. It is freely available to anyone who requests it.)

Many geophysical textbooks contain information regarding the gravity reduction process (e.g. Blakely, 1995; Parasnis, 1962; Telford et al., 1990); however, these don't contain comparisons between what happens when equations of different vintage are used. Talwani (1998) discusses the errors involved in Bouguer reduction, especially relating to the gravity effect of a spherical cap and Bullard B correction, which I have not replicated here.

A series of examples have been undertaken to illustrate quantitatively how much difference is introduced at various stages of the gravity reduction process. Each demonstration takes an element of the process, inserts realistic, but incorrect, values and presents the results in a series of tables.

# Method and results

## Applying the scale factor

The scale factor (often referred to as a Calibration Factor; Heath, 2016) is a multiplication factor that must be applied to all raw gravity readings. A typical Scintrex CG5 gravity meter measures relative gravity values in mGal; however, the dynamic range of the meter doesn't match reality. As an illustrative example, two points on the Earth's surface with the values 980 000 and 980 100 mGal, respectively, have a difference of 100 mGal. In comparison, a gravity meter might measure 4000 and 4100.1 mGal with a difference of 100.1 mGal. Therefore, a scaling factor must be calculated before all survey work by recording values at the end points of a calibration range with a significant change (typically over 50 mGal) in the gravity values. The scale factor (*c*) is the ratio of the actual difference in gravity ( $\Delta g_a$ ) to the measured difference in gravity ( $\Delta g_m$ ):

$$c = \frac{\Delta g_a}{\Delta g_m}.$$
 (1)

Raw gravity readings must be divided by the scale factor c. One potential source of error is using the inverse of the calibration factor (effectively multiplying instead of dividing by c). For a typical scale factor of 0.9997281, a typical raw reading of 3785.98 mGal becomes 3787.01 mGal if applied correctly and 3784.95 mGal if the inverse is used, creating a difference of 2.06 mGal. The dynamic range of a Scintrex CG5 is 1000 to 9000 mGal, meaning this error could range from anywhere between 0.5 to 5.0 mGal (for the scale factor referred to here).

## Methods to calculate c

For the simplest approach, c can be calculated from two measurements on the calibration range. It can also be calculated from an ABABA-type loop between two points A and B. In both cases the processor must decide to assume either a linear drift in the measurements, or to undertake a more thorough calculation to determine the scale factor. Furthermore, the processor may have multiple readings to choose from. If a CG5 is being used, does the processor choose the readings with the lowest standard deviation (s.d.) or should they average them all? A single measurement on a CG5 gravity meter is actually an average of a series of readings; hence, s.d. is available for each measurement. The following demonstration shows the effects of computing different scale factors from the same set of observations.

Table 1 shows the raw data collected from a gravity calibration run between the Kensington Gardens Sportsfield and Norton Summit Cemetery, South Australia.

Eight scenarios are considered, each a different way to calculate the calibration factor. The scenarios are:

- 1. Scale factor using two 'best' values only (from first A and B readings);
- 2. Scale factor using two average values (from first A and B readings);
- 3. Scale factor using average values, assuming linear drift (from first ABA loop);
- 4. Scale factor using average values, assuming linear drift (from second ABA loop);
- Scale factor using average values, assuming linear drift (ABABA);
- 6. Scale factor using best values only, treated as a gravity loop (from first ABA loop);

- 7. Scale factor using best values only, treated as a gravity loop (from second ABA loop); and
- 8. Scale factor using best values only, treated as a gravity loop (ABABA).

For each calculation technique (listed 1 to 8 above) I've calculated the scale factor and the minimum and maximum corrected value of a CG5 gravity meter, assuming a dynamic range of 1000 to 9000 mGal. I've then calculated the difference between the values calculated from each scenario with the final scenario (which is arguably the most accurate). The differences range from 0.01 to ~1.00 mGal. Table 2 shows these results.

Scenario 3 produces the least difference compared to Scenario 8. Scenario 4 is effectively the same as Scenario 3, as it uses the same method, just at a different time. Most of the scenarios produce a maximum difference in the range of 0.1 to 0.2 mGal, with the greatest difference (1.0 mGal) resulting from Scenario 2, where only two values are used to calculate the scale factor.

To illustrate how different scale factors affect a gravity survey, consider the Coompana gravity survey (Allpike, 2017). The dynamic range of the survey is -64.59 to 19.20 mGal, a total of ~84 mGal. This survey used three CG5 gravity meters, one measuring at ~2500 mGals, one at 4000 mGals and one at 5000 mGals. I'll call these gravity meters 1, 2 and 3, respectively, and I designate each gravity meter with its own scale factor from the scenarios above. I assign gravity meter 1 the scale factor from scenario 2, gravity meter 2 the scale factor from scenario 5, and gravity meter 3 the scale factor from scenario 8. If gravity meter 1 measures values from 2458 to 2542 mGal (84 mGal around 2500 mGal), the scaled values become 2456.954-2540.921 mGal, a difference of 83.964 mGal. Performing the same operation for gravity meters 2 and 3, we find scaled values of 83.972 and 83.973 mGal, respectively. The maximum difference here is 0.009 mGal, just under the 0.01 mGal level of detection.

#### Scale factor gravity datum

The scale factor will also be different depending on the gravity datum used for the known values in the calculation. Assuming

 Table 1. Raw readings taken from a scale factor run between Kensington Gardens (A) and Norton Summit Cemetery (B) using the CG5 gravity meter, serial number 050 800 135.

	А			В			А			В			А	
Reading	s.d.	Time	Reading	s.d.	Time									
4939.358	0.056	9:08 a.m.	4863.987	0.035	9:31 a.m.	4939.35	0.057	9:52 a.m.	4863.979	0.044	10:15 a.m.	4939.338	0.06	10:37 a.m.
4939.368	0.035	9:09 a.m.	4863.999	0.049	9:32 a.m.	4939.364	0.056	9:53 a.m.	4863.993	0.049	10:16 a.m.	4939.351	0.046	10:38 a.m.
4939.373	0.077	9:10 a.m.	4864.005	0.066	9:33 a.m.	4939.369	0.05	9:54 a.m.	4864	0.047	10:17 a.m.	4939.354	0.037	10:39 a.m.
4939.376	0.034	9:11 a.m.	4864.035	0.035	9:34 a.m.	4939.373	0.073	9:55 a.m.	4864.002	0.047	10:18 a.m.	4939.357	0.042	10:40 a.m.
4939.379	0.053	9:12 a.m.	4864.011	0.044	9:35 a.m.	4939.374	0.037	9:56 a.m.	4864.006	0.034	10:19 a.m.	4939.359	0.052	10:41 a.m.

Table 2. The scale factor determined by eight different scenarios and compared to scenario 8, revealing the greatest difference occurs when only two measurements are used in the calculation.

Scenario	Scale factor	Min. reading (mGal)	Max. reading (mGal)	Difference from scenario 8 (min.) (mGal)	Difference from scenario 8 (max.) (mGal)
1	1.000337147	999.6629664	8996.966697	-0.021357902	-0.192221115
2	1.000424752	999.5754279	8996.178851	-0.108896386	-0.980067476
3	1.000305291	999.6948024	8997.253221	0.010478076	0.094302685
4	1.00033051	999.6695987	8997.026388	-0.014725574	-0.132530162
5	1.000332723	999.6673879	8997.006491	-0.016936359	-0.152427234
6	1.000303843	999.6962495	8997.266245	0.011925214	0.107326928
7	1.000328416	999.6716916	8997.045224	-0.012632687	-0.113694185
8	1.000315775	999.6843243	8997.158918	0	0

the difference recorded on a CG5 meter is roughly the same, the difference in the scale factor is noticeable. Table 3 illustrates this, and further examples can be found in Hackney (2001), chapter 5.

The average of the scale factor differences in Table 2 is 0.05 mGal. Using a CG5 gravity meter, a measured difference between the two points is 62.703 mGal (this is a separate loop from the one shown in Table 1). The resulting difference in the two scale factors (using the two differences in Table 3) is 0.0008. Over the dynamic range of a CG5, this will lead to differences between 0.8 and 7.2 mGal. The maximum differences in the scale factors used in the Coompana example is ~0.0001, eight times smaller than the difference here.

Finally, it is worth noting that scale factor values change over time due to spring changes and other instrument factors. The two values below were calculated using the same method (method 8 above) and gravity meter on two dates approximately four months apart, and they differ by 0.000139785682:

1 June 2015 : 0.999544539

6 October 2015 : 0.999684324.

Over the dynamic range of a CG5, changes in scale factor values over time will result in differences of 0.14 to 1.26 mGal. Although it is unlikely the measurement range of a single gravity meter will change enough over the course of four months to affect the magnitude of readings, these results suggest that a scale factor should be undertaken before all surveys.

It's worth noting that the scale factors presented here can be reduced to seven significant figures without affecting the magnitude of the final difference.

## Effect of time on gravity reading

The equation that determines the observed gravity (in the Australian Absolute Gravity Datum 2007 (AAGD07)) from raw readings can be written as Equation 2:

$$g_{obs_{07}} = b_{07} - \frac{1}{c} \left( r_1 - r_s + \frac{(r_f - r_1)(t_s - t_1)}{(t_f - t_1)} \right)$$
(2)

where  $b_{07}$  is the known base station value (in AAGD07), *c* is the scale factor from Equation 1,  $r_1$  is the first reading at the base station,  $r_s$  is the reading taken at the station,  $r_f$  is the final reading at the base station,  $t_1$  is the time of the first reading at the base station,  $t_s$  is the time of the reading at the station and  $t_f$  is the time of the reading at the station. For gravity datums other

 Table 3.
 Different gravity datums have different dynamic ranges, which result in different scale factor calculations.

1965 Obs <i>g</i> AAGD07
6.660 979692.682
4.050 979630.022
610 62.660
62.703
0.999314

than AAGD07, simply change the datum of the known base station value  $b_{07}$ .

Two ways in which time can affect the value given by Equation 2 are if the wrong number is inserted for a time due to operator error (e.g. setting the wrong UTM zone or not setting daylight savings time on the CG5) or through processing error (e.g. typing the wrong number into the reduction software).

If, for example, we assume the error is due to processing, this can be demonstrated by taking the simple gravity loop shown in Table 1 and modifying the time component.

Consider the raw CG5 data in Table 4. Given the known value at A (Kensington Sportsfield) is 979706.660 mGal, the reduced value of B (Norton Summit Cemetary; subtracting one minute) is 979631.272 mGal (Table 5). The results of altering the time of B by adding and subtracting half-minutes, whole minutes and whole hours are shown in Table 5. While this isn't a comprehensive list of all possible gravity values, it should be suffice to demonstrate that the difference is negligible (< 0.01 mGal) for small time changes.

The time of a gravity measurement is typically recorded to the nearest minute. A reading on a CG5 gravity meter is effectively an average of a series of measurements, so the time recorded on the internal computer is the average time of the measurements to a precision of the nearest second. Changes of an hour due to incorrectly setting daylight savings time on a gravity meter can also be tested by simply modifying the time.

If the time zone (or latitude) is set incorrectly on a CG5 and the CG5 has been set up to calculate the tidal correction, a further correction will need to be applied. The incorrect tidal correction will need to be removed and the correct one added. Numerous webpages are available that can calculate tidal corrections (for no charge) for any part of the world, at any time, and are ideal for applying these corrections. Tidal corrections are cyclical, vary between ~-0.1 and ~0.1 mGal and have a wavelength of ~12 h.

Hackney (2001) illustrates distinct improvement in gravity reference network misclosures when instrument tide corrections were removed and recalculated using the more accurate latitude of the station in question.

### Height and gravity

A simple experiment to show the effect of height on gravity can be conducted by measuring acceleration due to gravity from on top of and underneath a desk. This experiment was undertaken at the Geological Survey of South Australia offices. We found that for a difference in height of 72 cm, the change in gravity was ~0.30 mGal (Figure 1). Linear extrapolation of the results shown in Figure 1 indicate that for over 1 m in height the change in gravity is ~0.42 mGal.

Each time a gravity meter is placed on a tripod and levelled, the sensor will be at a different height above the ground. This height can be measured, recorded and added to the elevation as measured by Differential GPS. For regional surveys, this might be added as a constant throughout the survey (~24 cm when using a CG5), but for microgravity surveys (measuring to tens of microgals (Sheriff, 1991) the elevation must be carefully taken into account. This can be demonstrated from some sampled survey data. Consider the data presented in Table 6. This data is from a portion of a microgravity survey undertaken in early

Table 4. This simple gravity loop (a subset of Table 1) is used to demonstrate what happens when a time is modified.

	А			В			А	
Reading (mGal)	s.d. (mGal)	Time	Reading (mGal)	s.d. (mGal)	Time	Reading (mGal)	s.d. (mGal)	Time
4939.376	0.034	9:11 a.m.	4863.987	0.035	9:31 a.m.	4939.374	0.037	9:56 a.m.

2017 (Heath et al., 2017). The table shows the station numbers, observed gravity readings, heights, Bouguer gravity values and the difference between Bouguer gravity values for three stations. The three readings selected show a range of sensor heights from 21 to 28.2 cm, and the difference in Bouguer gravity ranges from 0.041 to 0.055 mGal, detectable on the CG5 gravity meter. A microgravity survey such as in Heath et al. (2017) may be looking at gravity anomalies with magnitudes smaller than 0.26 mGal, suggesting this height measurement is important for precise Bouguer gravity values.

The effect of using an incorrect height in processing can also be demonstrated by taking an existing loop, modifying the height of a single point and observing the differences. Considering again the loop shown in Table 4, Table 7 shows the same reading repeated 14 times but with incorrect heights. The final two columns are simple Bouguer anomalies and the difference between the actual values. These are consistent with the calculations in the desk experiment (Figure 1) and the microgravity example (Table 6). The difference becomes noticeable when the height varies more than ~5 cm.

Table 5. Considering the loop in Table 4, the effect of getting the time wrong by a minute in the reduction process is less than below the level of detection (< 0.01 mGal), but an hour difference is noticeable (> 0.01 mGal).

	Observed gravity (mGal)	Difference (mGal)
Time of B subtract one hour	979630.7633508	-0.5085381
Time of B subtract one minute	979631.2718444	-0.0000444
Time of B subtract half minute	979631.2718667	-0.0000222
Time of B	979631.2718889	0
Time of B add half minute	979631.2719111	0.0000222
Time of B add one minute	979631.2719333	0.0000444
Time of B add one hour	979630.7686825	0.5032064

Another potential difference in height comes when using Orthometric heights instead of Ellipsoidal heights in the Bouguer calculation. Until recently, it has been routine to use Orthometric heights in gravity calculations as they represent a height from an equi-gravity datum (i.e. sea level, see Reynolds, 1997). However, this thinking has fallen out of favour as Hackney and Featherstone (2003) and Hinze et al. (2005) explain. Not using the Ellipsoidal height leads to underor over-correction of normal gravity (theoretical gravity) when computing free-air or Bouguer anomalies. The difference between Elliposidal and Orthometric heights is generally in the order of meters, so the differences in gravity value will be greater than in the height examples shown in Tables 6 and 7. This issue is particularly relevant when comparing older, pre-GPS surveys with newer surveys, as normal/theoretical gravity is always linked to a particular ellipsoid and free-air/Bouguer anomalies are always relative to the surface of that ellipsoid. And, of course, in the past we didn't have a good way to determine Ellipsoidal heights, which leads to issues when merging older datasets with newer ones.

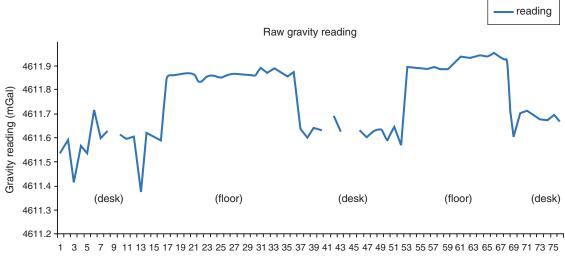
# Gravity datums

The fifth demonstration relates to gravity datums. The Geological Survey of South Australia commonly use three gravity datums: Isogal65 (Potsdam), Isogal84 (ISGN1971) and AAGD07. To add further confusion, these are often presented in different units: either mGal or  $\mu$ ms<sup>-2</sup>.

There are two commonly used equations to convert between Isogal65 and Isogal84 in Australia (Wellman et al., 1985):

$$g_{obs_{1984}} = 979671.88 + 1.00053(g_{obs_{1965}} - 979685.74) \,(\text{mGal})$$
(3)

$$g_{obs_{1984}} = g_{obs_{1965}} - V(\text{mGal})$$
 (4)



Reading number

Fig. 1. The change in gravity of ~0.30 mGal over a distance of 72 cm at a location in Adelaide, South Australia.

Table 6.	Taking – or not taking – i	nto account the height of the sen	sor will produce a n	oticeable difference i	n Bouguer gra	vity values (	> 0.01 mGal).

Station	Observed gravity (mGal)	Height of sensor (m)	Ellipsoidal height (m)	Bouguer gravity from ellipsoidal height (mGal)	Bouguer gravity from ellipsoidal height plus sensor height (mGal)	Difference (mGal)
101501700	979399.062	0.256	71.647	-38.8002	-38.7503	0.0499
101202900	979398.745	0.210	71.484	-38.9605	-38.9195	0.0410
101802600	979398.835	0.282	71.820	-38.9481	-38.8931	0.0550

where

$$V = 14.166 - 0.001838X + 0.0405366Y - 0.000220256X^2$$

$$+ 0.000476101XY + 0.00070915Y^2 + 0.0000016635X^2$$

 $-\ 0.0000964709 X^2 Y - 0.0000373075 XY^2$ 

 $-0.00014788Y^3 + 0.000000915962X^4$ 

- $+\ 0.000000764998 X^3 Y 0.0000000772339 X^2 Y^2$
- $-\ 0.00000673367XY^3 0.00000982392Y^4$
- $+\ 0.0000000910128 X^5 + 0.000000147126 X^4 Y$
- $+ 0.000000666914X^{3}Y^{2} + 0.000000568814X^{2}Y^{3}$
- $+ 0.00000045662XY^4 + 0.000000438121Y^5.$  (5)

In Equation 5, *X* is the longitude minus  $135^{\circ}$  east and *Y* is the latitude minus  $25^{\circ}$  south (i.e. if using the equations, use a positive value of latitude in the southern hemisphere).

The difference between Isogal65 and Isogal84 values is ~14 mGal; however, the difference varies depending on which

equation is used. For a point in Adelaide, the Isogal65 value is 979 706.660 mGal, giving Isogal84 values of 979 692.811 mGal (using Equation 3) and 979 692.237 mGal (using Equation 4). The difference between the values is 0.574 mGal. Generally this isn't a problem unless converting values back and forth between datums, in which case a single formula should be used only. These issues occur in databases such as the South Australian geophysical database (SA Geodata) and Geoscience Australia's Geophysical Archive Data Delivery (GADDS) system, which use different equations to automatically populate whichever values are not present in the database.

The following equation is used to convert between Isogal84 and AAGD07 (in mGal):

$$g_{obs_{2007}} = g_{obs_{1984}} - 0.078. \tag{6}$$

Another issue between datums occurs when published values don't match. Consider the data in Table 8. The gravity values for De Rose Hill in South Australia, for example, are 978975.48 mGal (Isogal65) and 9789612.42  $\mu$ ms<sup>-2</sup> (AAGD07).

Table 7. Considering again the loop in Table 4, the effect of an incorrect height can be up to 0.1 mGal at 50 cm height change.

Station	Reading	Time	Height (m)	Height change	Bouguer anomaly (mGal)	Difference (mGal)
A	4939.376	9:11 a.m.	85	N/A	-16.7607	N/A
В	4863.987	9:31 a.m.	482.5	+50 cm	-14.4781	0.09835
В	4863.987	9:31 a.m.	482.2	+20 cm	-14.5371	0.03934
В	4863.987	9:31 a.m.	482.1	+10 cm	-14.5567	0.01967
В	4863.987	9:31 a.m.	482.05	+5 cm	-14.5666	0.00984
В	4863.987	9:31 a.m.	482.01	+1 cm	-14.5744	0.00197
В	4863.987	9:31 a.m.	482.005	+5 mm	-14.5754	0.00098
В	4863.987	9:31 a.m.	482.001	+1 mm	-14.5762	0.0002
В	4863.987	9:31 a.m.	482	0	-14.5764	0
В	4863.987	9:31 a.m.	481.999	-1 mm	-14.5766	-0.0002
В	4863.987	9:31 a.m.	481.995	-5 mm	-14.5774	-0.00098
В	4863.987	9:31 a.m.	481.99	-1 cm	-14.5784	-0.00197
В	4863.987	9:31 a.m.	481.95	-5 cm	-14.5862	-0.00984
В	4863.987	9:31 a.m.	481.9	-10 cm	-14.5961	-0.01967
В	4863.987	9:31 a.m.	481.8	-20 cm	-14.6157	-0.03934
В	4863.987	9:31 a.m.	481.5	-50 cm	-14.6748	-0.09835
А	4939.374	9:56 a.m.	85	N/A	-16.7607	N/A

 Table 8. Published observed gravity values in different datums do not match. The maximum difference in these examples is 0.55 mGal at the Meningie woolshed.

Site name	Site code	Original	Calculated	Calculated	Reported	Difference	Difference
Site name	Site code	65 value	'07 value mGal	'07 value mGal	'07 values	between	between
		(mGal)	(Equations	(Equations	mGal	column D &	column E &
		(1110111)	3 & 6)	4 & 6)	mour	F (mGal)	F (mGal)
Abminga Fettlers quarters	1966000002	978963.37	978949.049	978949.079	978949.112	0.06	0.03
De Rose Hill shed	1964911081	978975.48	978961.166	978961.176	978961.242	0.08	0.07
Hawker school	1964911117	979394.33	979380.238	979379.849	979380.392	0.15	0.54
Innamincka Airstrip	1964919015	979115.14	979100.900	979100.803	979101.022	0.12	0.22
Kenmore Park Homestead garage	1964911082	978886.71	978872.349	978872.410	978872.482	0.13	0.07
Kingscote Airstrip light tower	1980901306	979828.72	979814.858	979814.221	979814.760	-0.10	0.54
Lake Everard Airstrip end trees	1964911118	979446.80	979432.735	979432.310	979432.812	0.08	0.50
Lake Everard Airstrip phone	1964919118	979447.15	979433.086	979432.660	979433.162	0.08	0.50
Maralinga Airstrip terminal	1964919100	979283.88	979269.729	979269.438	979269.772	0.04	0.33
Meningie Homestead woolshed	1967931305	979790.21	979776.327	979775.722	979776.272	-0.06	0.55
Mt Davies Mining Camp 57-45	1964919083	978957.65	978943.326	978943.361	978943.392	0.07	0.03
Norton Summit hotel	1960910208	979644.05	979630.090	979629.550	979630.022	-0.07	0.47
William Creek hotel	1967939308	979226.61	979212.429	979212.210	979212.532	0.10	0.32
Wooltana Airstrip	1964919103	979350.37	979336.254	979335.932	979336.272	0.02	0.34
Woomera Aerodrome hangar	1950999938	979370.74	979356.635	979356.269	979356.792	0.16	0.52
Woomera Airstrip Terminal	1964910138	979372.75	979358.646	979358.279	979358.699	0.05	0.42

Using Equations 3 to 6 to convert between the values results in differences of 0.07 or 0.08 mGal. The highest variation found in South Australia was at the Meningie Homestead Woolshed, with a difference of 0.55 mGal. A comprehensive analysis of all Isogal stations in Australia is beyond the scope of this paper, but should be examined.

# Theoretical gravity

The sixth demonstration relates to theoretical gravity. The latitude of the gravity measurement is part of the theoretical gravity correction component of gravity reduction. Telford et al. (1990) give the theoretical gravity equation for the GRS1967 ellipsoid; however, different sources provide slightly different equations (see list below). There are newer equations for GRS80 and WGS84 as well as the older 1930 equation. Some of these are listed here:

$$g_{t_{1930}} = 978049.0(1 + 0.0052884 \sin^2 \theta) - 0.0000059 \sin^2 2\theta (mGal)$$
(7)

(Sheriff, 1991; Blakely, 1995; Reynolds, 1997)

$$g_{t_{1967}} = 978031.8(1 + 0.0053024 \sin^2 \theta) - 0.0000059 \sin^2 2\theta) (\text{mGal})$$
(8)

(Kearey et al., 1984)

$$g_{t_{1967}} = 978031.8(1 + 0.0053024 \sin^2 \theta) - 0.0000058 \sin^2 2\theta) (mGal)$$
(9)

(Sheriff, 1991)

$$g_{t_{1967}} = 978031.846(1 + 0.0053024 \sin^2 \theta) - 0.0000058 \sin^2 2\theta) (mGal)$$
(10)

(Blakely, 1995)

$$g_{t_{1967}} = 978031.846(1 + 0.005278895 \sin^2\theta + 0.000023462 \sin^4\theta) \text{ (mGal)}$$
(11)

(Telford et al., 1990; Reynolds, 1997)

$$g_{t_{1967}} = 978031.85(1 + 0.005278895 \sin^2 \theta + 0.000023462 \sin^4 \theta) \text{ (mGal)}$$
(12)

(Kearey et al., 1984)

$$g_{t_{1980}} = 978032.67715 \frac{1 + 0.001931851353 \sin^2 \theta}{\sqrt{1 - 0.0066943800229 \sin^2 \theta}}$$
(mGal) (13)

(Wikipedia (https://en.wikipedia.org/wiki/Theoretical\_gravity); Hackney and Featherstone, 2003; Hinze et al., 2005)

$$g_{t_{1984}} = 978032.67714 \frac{1 + 0.00193185138639 \sin^2 \theta}{\sqrt{1 - 0.00669437999013 \sin^2 \theta}} (\text{mGal})$$
(14)

$$g_{t_{1984}} = 978032.53359 \frac{1 + 0.00193185265241 \sin^2 \theta}{\sqrt{1 - 0.00669437999013 \sin^2 \theta}} (\text{mGal})$$
(15)

(Blakely, 1995)

(Wikipedia, https://en.wikipedia.org/wiki/Theoretical\_gravity)

$$g_{t_{1987}} = 978032.68(1 + 0.00193185138639 \sin^2 \theta)$$

$$(1 - 0.00669437999013 \sin^2 \theta) (\text{mGal})$$
(16)

(Sheriff, 1991)  

$$g_{t_{1987}} = 978032.68 \frac{1 + 0.00193185138639 \sin^2\theta}{\sqrt{1 - 0.00669437999013 \sin^2\theta}} (\text{mGal}).$$
(17)

#### (modified from Sheriff, 1991)

Equations 7 to 12 use a simplified form of what is represented in the 'closed form' of Equations 13 to 17. This simplification was initially used due to limited computational power. Equation 16 is as presented in Sheriff (1991); it appears to be a misprint and Equation 17 here is a modified version of the equation.

Table 9 demonstrates the differences from Equations 7 to 17. I've taken a series of Australian latitudes  $(-10^{\circ} \text{ to } -45^{\circ})$  and calculated the theoretical gravity for each using Equations 7 to 17. I've then subtracted each value from selected 'benchmark' equations (those with the most references) to demonstrate the difference between 1967 and 1984 values. Typically, the 1930 equation (Equation 7) is different by ~16 mGal, the 1967 equations differ up to ~1 mGal, the 1984 equations differ up to ~0.14 mGa, and the difference between 1967 and 1984 values is in the order of 0.8 mGal.

The seventh demonstration illustrates what happens when latitudes in a different geographic datum are used in the theoretical gravity calculation. Using AGD66 instead of GDA94 values (or vice versa) in the theoretical gravity equation will yield different values.

To demonstrate the difference in theoretical gravity between AGD66 and GDA94 values, I've taken a range of Australian AGD66 latitudes  $(-10^{\circ} \text{ to } -45^{\circ})$  and calculated the equivalent GDA94 values as well various theoretical gravity values at these points. Table 10 shows the gravity values, and Table 11 shows the differences (up to ~1.0 mGal).

The eighth demonstration illustrates how all these issues feed into the final Bouguer anomaly. These arise as combinations of all the previously described scenarios.

To demonstrate a combination of errors in calculating the Bouguer anomaly: if an incorrect datum is used in a calculation (error 0.83 mGal), the elevation is out by 20 cm (error 0.4 mGal) and an incorrect calibration number is used (error 1 mGal). In other words, the total isn't simply the sum of these errors. To demonstrate, consider again the simple loop in Table 4. The difference in the observed gravity is 0.5297 mGal and the difference in the Bouguer anomaly is -0.3667 mGal, as shown in Table 12.

Finally, it's worth mentioning hysteresis effects in Scintrex CG series gravity meters. The hysteresis effect occurs as the result of spring relaxation following transport of the gravity meter between stations, and not necessarily over rough terrain. It usually manifests itself as a slow increase or decrease in readings over half an hour or more once the instrument is levelled at a station. This is evident in the readings in Table 1. The average increase between first and last reading (over 5 min) is ~0.023 mGal. This is a significant amount and raises the question of which value to use for a given station where multiple measurements are recorded. This is not usually documented in gravity acquisition reports. For a thorough

			Table 9. Va	Variations in theoretical gravity equations can yield differences greater much than 0.01 mGal.	cal gravity equatio	ns can yield differe	ences greater mucl	than 0.01 mGal.			
Latitude	Equation 7 (1930)	Equation 8 (1967)	Equation 9 (1967)	Equation 10 (1967)	Equation 11 (1967)	Equation 12 (1967)	Equation 13 (1980)	Equation 14 (1984)	Equation 15 (1984)	Equation 16 (1987)	Equation 17 (1987 – mod)
-10	978 204.2893 078 204.0367	978 187.4995 078 277 7770	978 187.5109 078 277 772 2	978 187.5455 078 377 7030	978 187.5482 078 377 7005	978 187.5522 078 277 8035	978 188.3836 078 378 6308	978 188.3836 078 378 6308	978 188.2401 078 378 4067	977 892.2154 077 770 6075	978 188.3865 078 278 6476
-10	978 651.6616	978 636.0527	978 636.0931	978 636.0988	978 636.1078	978 636.1118	978 636.9538	978 636.9538	978 636.8103	977 487.6351	978 636.9567
-25	978 969.4211	978 954.6505	978 954.7079	978 954.6965	978 954.7088	978 954.7128	978 955.5611	978 955.5611	978 955.4176	977 200.3452	978 955.5639
-30	979 337.7507	979 323.9512	979 324.0245	979 323.9972	979 324.012	979 324.016	979 324.8704	979 324.8704	979 324.7269	976 867.4123	979 324.8732
-35	979 745.5439	979 732.8187	979 732.9051	979 732.8648	979 732.8807	979 732.8847	979 733.7447	979 733.7447	979 733.6013	976 498.906	979 733.7476
-40	980 180.4792	980 168.8991	980 168.994	980 168.9452	980 168.9606	980 168.9646	980 169.8296	980 169.8296	980 169.6863	976 105.9851	980 169.8325
-45	980 629.3867	980 618.9875	980 619.0853	980 619.0336	980 619.0464	980 619.0504	980 619.9202	980 619.9202	980 619.7769	975 700.5636	980 619.9231
Difference	between Equation	Difference between Equation 14 and the rest (mGal)	(1)								
Latitude	Equation 7	Equation 8	Equation 9	Equation 10	Equation 11	Equation 12	Equation 13	Equation 14	Equation 15	Equation 16	Equation 17
	(1930)	(1967)	(1967)	(1967)	(1967)	(1967)	(1980)	(1984)	(1984)	(1987)	(1987 - mod)
-10	15.90574337	-0.884109811	-0.872669012	-0.838102488	-0.835423537	-0.8314229	9.49996E-06	0	-0.143535514	-296.1682296	0.002860455
-15	15.39698665	-0.891861271	-0.867410476	-0.845845	-0.840226651	-0.836225236	8.88982E-06	0	-0.143517816	-658.0372234	0.002861012
-20	14.7077834	-0.901103207	-0.860693289	-0.855074787	-0.846052909	-0.842050437	8.06199 E - 06	0	-0.143493793	-1149.31871	0.002861767
-25	13.86003394	-0.910597074	-0.853203812	-0.86455367	-0.852264343	-0.848260568	7.04173E-06	0	-0.143464171	-1755.21591	0.002862699
-30	12.8803647	-0.919188014	-0.845835629	-0.87312724	-0.858334508	-0.854329223	5.86023E-06	0	-0.143429849	-2457.458033	0.002863779
-35	11.79916447	-0.925994442	-0.83963206	-0.879914437	-0.863955207	-0.859948251	4.55475E–06	0	-0.143391865	-3234.838705	0.002864974
-40	10.64956738	-0.930528361	-0.835674308	-0.884427846	-0.869079462	-0.865070722	3.16417E–06	0	-0.143351372	-4063.84454	0.00286625
-45	9.466429781	-0.932726379	-0.834923199	-0.886604695	-0.873890281	-0.8698797	1.73121E–06	0	-0.143309598	-4919.356667	0.002867566
Difference	Difference between Equation 11 and rest (mGal)	11 and rest (mGal)									
Latitude	Equation 7	Equation 8	Equation 9	Equation 10	Equation 11	Equation 12	Equation 13	Equation 14	Equation 15	Equation 16	Equation 17
	(1930)	(1967)	(1967)	(1967)	(1967)	(1967)	(1980)	(1984)	(1984)	(1987)	(1987 – mod)
-10	16.74116691	-0.048686274	-0.037245475	-0.002678951	0	0.004000637	0.835433037	0.835423537	0.691888023	-295.3328061	0.838283992
-15	16.2372133	-0.05163462	-0.027183825	-0.005618349	0	0.004001415	0.840235541	0.840226651	0.696708835	-657.1969967	0.843087663
-20	15.55383631	-0.055050299	-0.014640381	-0.009021879	0	0.004002471	0.846060971	0.846052909	0.702559116	-1148.472657	0.848914676
-25	14.71229828	-0.058332732	-0.000939469	-0.012289327	0	0.004003774	0.852271384	0.852264343	0.708800171	-1754.363645	0.855127041
-30	13.7386992	-0.060853506	0.012498879	-0.014792732	0	0.004005285	0.858340368	0.858334508	0.714904659	-2456.599699	0.861198286
-35	12.66311967	-0.062039234	0.024323147	-0.01595923	0 0	0.004006957	0.863959762	0.863955207	0.720563342	-3233.97475	0.866820182
04 55	10.34032006	-0.061448899 -0.058836098	0.038967082	-0.012714414	0 0	0.004010581	0.869082627	0.873890281	0.730580683	-4062.97246 -4918.482777	0.876757847

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AGD66 latitude (degrees)	GDA94 latitude (degrees)	A gt1967 (Equation 11) AGD66 (mGal)	B gt1967 (Equation 11) GDA94 (mGal)	C gt1984 (Equation 14) AGD66 (mGal)	D gt1984 (Equation 14) GDA94 (mGal)
-10	-9.998538	978 187.548	978 187.503	978 188.339	978 188.384
-15	-14.998523	978 377.800	978 377.733	978 378.573	978 378.640
-20	-19.998520	978 636.108	978 636.022	978 636.868	978 636.954
-25	-24.998526	978 954.709	978 954.607	978 955.459	978 955.561
-30	-29.998543	979 324.012	979 323.898	979 324.756	979 324.870
-35	-34.998570	979 732.881	979 732.759	979 733.623	979 733.745
-40	-39.998607	980 168.961	980 168.836	980 169.706	980 169.830
-45	-44.998654	980 619.046	980 618.925	980 619.798	980 619.920

Table 10. Theoretical gravity calculated for various latitudes in AGD66 and GDA94.

Table 11. The difference in theoretical gravity values from Table 10 (columns marked A to D) is up to ~1.0 mGal.

AGD66 latitude (degrees)	(A–B) Difference in '67 values (mGal)	(C–D) Difference in '84 values (mGal)	(A–C) Difference in '66 values (mGal)	(B–D) Difference in '94 values (mGal)	
-10	0.045082383	0.045376923	-0.790339961	-0.880505920	
-15	0.066582944	0.067572774	-0.773642105	-0.906809595	
-20	0.085810523	0.088121002	-0.760240574	-0.931863432	
-25	0.101907084	0.106304168	-0.750355427	-0.954171427	
-30	0.1139518	0.121263797	-0.744380996	-0.972286308	
-35	0.121439352	0.132476678	-0.742514323	-0.985394560	
-40	0.124069825	0.139529287	-0.745008265	-0.993149288	
-45	0.121827222	0.142196965	-0.752061778	-0.995717503	

 Table 12.
 This simple loop (from Table 4) with a combination of errors yields a difference of -0.3667 mGal in the final Bouguer anomaly.

Station	Raw	Calibration factor	Observed gravity (mGal)	Latitude	Elevation	Bouguer (mGal)	Difference (mGal)
А	4939.376	1.0003158	979 706.66	-34.9231	85	-16.76068	<u> </u>
В	4863.987	1.0003158	979 631.3	-34.92901	482	-14.57641	
B-wrong	4863.987	1.0004248	979 630.77	-34.92755	482.2	-14.9431	-0.3667
Α	4939.374	1.0003158	979 706.66	-34.9231	85	-16.76068	

analysis of the hysteresis effect on a CG-3M gravity meter see Repanić and Kuhar (2017).

### Discussion

Geophysicists at the Geological Survey of South Australia have tried for many years to produce a 'perfect' image of the state gravity. This has involved experimenting with different gridding techniques: grid merging (Heath et al., 2012), levelling (Heath and Katona, 2016) and supervised variable density gridding (Heath and Katona, 2016; Katona, 2017).

In exploring these techniques it became apparent that simply flagging surveys that didn't fit well and not using them as part of the gridding process was the quickest way to handle them. This isn't a complete solution, and is potentially removing information that would otherwise be useful in a state grid product. This paper is an exploration of the reasons why surveys undertaken in the same area may not match.

As is apparent, there are many reasons why surveys in the same area may not match. Trying to correct for these inconsistencies can be difficult, as the information needed is not always available. Some of the information can be determined by backcalculation (e.g. if you have a Bouguer anomaly value, ellipsoid elevation, density and observed gravity it should be possible to determine which theoretical gravity equation was used) but some information can't easily be recovered (e.g. if only a station number and Bouguer anomaly are provided).

There are many other potential sources of error in gravity surveying (not least of all potential confusion arising from the terms Isogal65, AGD66 and GRS67). Some of the operation errors include (when using a CG5 instrument) setting the internal clock incorrectly and incorrectly setting the reference point on the meter. Other sources of error involve terrain corrections and atmospheric corrections. There are far too many sources of error to include in this paper, so I've restricted myself to those commonly involved in the processing of data.

Thorough documentation and staff training are essential for a successful gravity survey. I argue that a successful survey be undertaken by well-trained staff, and documentation contain (at a minimum) enough information to calculate the Bouguer anomaly from the raw readings during each step of the process.

#### Conclusions

Inconsistencies in processing gravity data can lead to errors in the final product. I've demonstrated that errors due to calibration factors, time zones, height, geodetic datum, gravity datum and the equations used all lead to an incorrect value for gravity at a point. These errors, combined with other potential sources of error not discussed here, mean that adjacent or overlapping gravity surveys will often not correlate. As new geodetic models will undoubtedly be created from time to time, it would be naïve to set some sort of standard; rather, I suggest that all gravity surveys should be documented to a level where the observed and Bouguer gravity anomalies can be recreated from raw readings. This transparency in gravity processing will allow gravity surveys to be reprocessed should any issues with the survey be found and should ultimately allow better gravity products.

The largest source of error discussed in this paper is the effect of using an incorrect theoretical gravity equation (Equation 16). Ignoring the 'incorrect' equation and using the 1930 equation (Equation 7), when the 1984 equation (Equation 14) would be more appropriate, leads to an error of over 16 mGal.

## **Conflicts of interest**

The author declares no conflicts of interest.

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