

**Accessory publication****Assessing WHAM/Model VII against field measurements of free metal ion concentrations: model performance and the role of uncertainty in parameters and inputs**Stephen Lofts<sup>A,B</sup> and Edward Tipping<sup>A</sup>

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**Sources of supporting chemical composition for speciation calculations**

Tables A1 and A2 summarise the sources of supporting chemical compositional data required for speciation modelling of the water samples in this study.

**Table A1. Sources of major ion concentrations in datasets**

Ticks indicate measured data quoted for all samples. Empty cell indicates concentrations not estimated. Alk, Alkalinity

Datasets	Reference	Na	Mg	Al	K	Ca	Fe <sup>II</sup>	Fe <sup>III</sup>	Cl	NO <sub>3</sub>	SO <sub>4</sub>	Alk	F
Ni-04, Cu-08, Zn-05, Cd-05, Pb-04	[1]	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
Cd-02	[2]	✓	✓	A	✓	✓		B	✓	✓	✓	✓	✓
Cu-10, Zn-06, Cd-06	[3]	✓	✓	✓	✓	✓		✓	✓	✓	✓	✓	✓
Ni-01	[4]	✓	✓	✓	✓	✓		✓	✓	✓	✓	B	✓
Cu-01, Zn-01, Cd-01	[5]	✓	✓	✓	✓	✓		✓	C	✓	C	B	✓
Ni-03, Cu-07, Zn-04, Cd-04, Pb-03	[6]	✓	E	D	✓	E		F, G, H, I	J		K	B	✓
Cu-02, Zn-02	[7]	L	E	D	L	E		G, M	L	N	O	✓	
Cu-04, Pb-01	[8]	P	✓	D		✓		Q	P		R	✓	
Co-01	[9]	S	S	D	S	✓		T	S	S	S	✓	
Ni-02, Cu-03, Cd-03, Pb-02	[10]	✓	✓	Q	✓	✓		F, G	✓	✓	✓	✓	✓
Ni-05	[11]	✓	✓	✓	✓	✓		✓	✓	✓	✓	✓	✓
Cu-05	[12]	?	✓	D		✓		F	✓	✓	✓	✓	✓
Zn-03	[13]	?	✓	D		✓		F, U	V		V	✓	

<sup>A</sup>Hydroxide solubility control assumed for Lake Greifen samples.

<sup>B</sup>Assumed to be 0.08 µM, based on measurements given in Emmenegger et al.<sup>[14]</sup>

<sup>B</sup>Partial pressure of atmospheric CO<sub>2</sub> set to 36.98 Pa (365 ppm).

<sup>C</sup>Quoted concentrations for 2002 samples unrealistically low. Quoted concentrations from 2001 samples used.

<sup>D</sup>Hydroxide solubility control assumed.

<sup>E</sup>Calculated from measured hardness assuming a Mg : Ca ratio of 1 : 9.

<sup>F</sup>Concentrations in Lake Greifen from Emmenegger et al.<sup>[14]</sup>

<sup>G</sup>Concentrations in Furtbach stream from mean of all concentrations recorded for the Limmat River by NADUF (National River Monitoring and Survey Programme, <http://www.bafu.admin.ch/hydrologie/01831/01840/index.html?lang=en>), for the month of sampling.

<sup>H</sup>Concentrations in the Rhine at Wageningen from mean of all concentrations recorded for the Rhine at the Netherlands–German border by the United Nations Global Environment Monitoring System (GEMSTAT; <http://www.gemstat.org>), for the month of sampling.

<sup>I</sup>Concentration in River Wyre from Unsworth et al.<sup>[10]</sup>

<sup>J</sup>Calculated as  $[\text{Cl}] = [\text{Na}] + [\text{K}]$ .

<sup>K</sup>Calculated from charge balance.

<sup>L</sup>For Furtbach samples, after Kalis et al.<sup>[6]</sup> For Glatt samples, from concentration in Lake Greifen after Cao et al.<sup>[2]</sup>

<sup>M</sup>Assumed to be 0.1 μM, based on measurements made in Emmenegger et al.<sup>[14]</sup>

<sup>N</sup>For Furtbach samples, after Kalis et al.<sup>[6]</sup> Not estimated for Glatt samples.

<sup>O</sup>For Furtbach samples, after Kalis et al.<sup>[6]</sup> For Glatt samples, from charge balance.

<sup>P</sup>Calculated by fitting to charge balance and measured conductivity.

<sup>Q</sup>From Kauppi et al.,<sup>[15]</sup> using mean concentration given for northern Finnish lakes.

<sup>R</sup>Calculated by assuming that if  $[\text{Ca}] + [\text{Mg}] - 2[\text{HCO}_3] > 0$ ,  $[\text{SO}_4] = [\text{Ca}] + [\text{Mg}] - 2[\text{HCO}_3]$ , otherwise  $[\text{SO}_4] = 0$ .

<sup>S</sup>Measured values where quoted. Remaining value calculated assuming the ratio to Ca to be the mean of that in the other samples.

<sup>T</sup>Measured values where quoted. 0.1 μM assumed for Lake Lucerne sample.

<sup>U</sup>0.1 μM assumed for Aabach River sample.

<sup>V</sup>Calculated from Xue and Sigg<sup>[12]</sup> assuming Cl : SO<sub>4</sub> ratio of 1 : 2.

**Table A2. Sources of major ion concentrations in dataset Cu-03**

Ticks indicate measured data quoted for all samples. Alk, Alkalinity

Sample(s)	Na	Mg	Al	K	Ca	Fe <sup>III</sup>	Cl	NO <sub>3</sub>	SO <sub>4</sub>	Alk
	A	B	C	A	D	C	A	A	A	
Lake Sempach										✓
Lake Sabbia	E	E	C	E	E	C	E	E	E	✓
Lake Inferiore	E	E	C	E	E	C	E	E	E	✓
Lake Zotta	E	E	E	E	E	C	E	E	E	✓
Lake Cristallina	E	E	E	E	E	C	E	E	E	✓
Lake Orta	F	F	F	F	F	F	F	F	F	✓
River Aare, Eichholz/Halenbrucke	G	G	C	G	G	G	G	G	G	✓
River Aare, Brugg	H	H	C	H	H	C	H	H	H	✓
River Birs, Munchenstein	I	I	C	I	I	I	I	I	I	✓
River Glatt, Rheinsfelden/Niederglatt/Rumlang	J	J	C	J	J	C	J	J	J	✓
River Rhine, Reckingen	H	H	C	H	H	C	H	H	H	✓
River Rhine, Village–Neuf	I	I	C	I	I	C	I	I	I	✓
River Thur, Andelfingen	I	I	C	I	I	C	I	I	I	✓

<sup>A</sup>From log : log regressions between the concentration of this determinand and Ca, at all other sites in this dataset with measured concentrations of this determinand.

<sup>B</sup>From Xue et al.,<sup>[16]</sup> assuming [Mg] : [Ca] is 0.35.

<sup>C</sup>Assumed to be 0.1 µM for lake samples, for river samples taken to be the mean of NADUF (National River Monitoring and Survey Programme, <http://www.bafu.admin.ch/hydrologie/01831/01840/index.html?lang=en>) measurements at the site for the month of sampling. Values for Glatt all taken from the single NADUF site on this river. Values for the Aare taken from the other NADUF site on the river.

<sup>D</sup>From Ramisch et al.<sup>[17]</sup>

<sup>E</sup>From Giovanoli et al.<sup>[18]</sup>

<sup>F</sup>From Calderoni et al.<sup>[19]</sup>

<sup>G</sup>Mean of all concentrations recorded for the Aare at Bern by NADUF for the month of sampling.

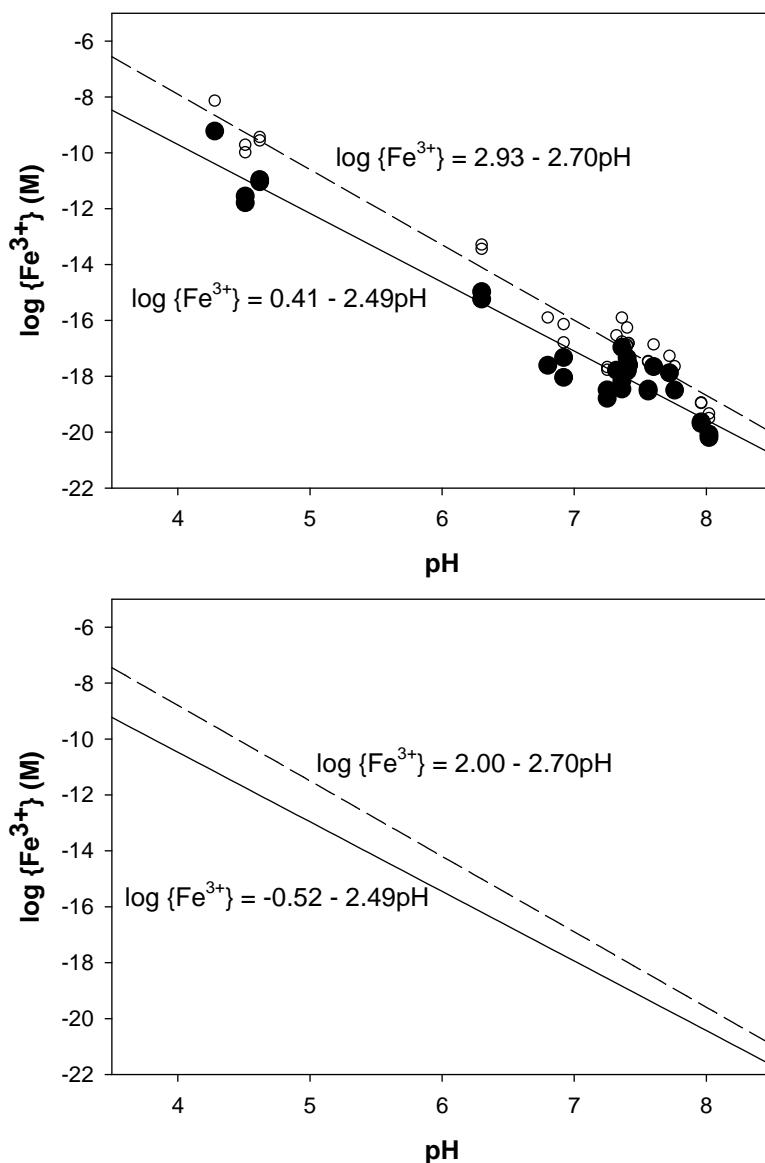
<sup>H</sup>Mean of all concentrations recorded for the sampling location in GEMSTAT (United Nations Global Environment Monitoring System, <http://www.gemstat.org/>) for the month of sampling.

<sup>I</sup>Mean of all concentrations recorded for the sampling location by NADUF for the month of sampling.

<sup>J</sup>Mean of all concentrations recorded for the Glatt at Rheinsfelden by NADUF for the month of sampling.

### Recalculation of iron(III) solubility using Model VII

Lofts et al.<sup>[20]</sup> calculated a solubility expression for Fe<sup>III</sup> as a function of pH, based on activities of Fe<sup>III</sup> in natural waters calculated from samples dialysed to remove colloidal Fe<sup>III</sup>. Because the Fe<sup>III</sup> activities were calculated using Model VI, it was necessary to recalculate the activities and the solubility expression using Model VII in order to calculate Fe<sup>III</sup> solubilities for application in WHAM/Model VII. Recalculated activities are shown in Fig. A1 along with the activities calculated using WHAM/Model VI.



**Fig. A1.** Top pane: Fe<sup>III</sup> activities in natural samples dialysates at 283 K calculated using Model VII (filled circles) and values from Lofts et al.<sup>[20]</sup> calculated using Model VI (open circles). Regression of Model VII-calculated activities versus pH (solid line) and of Model VI-calculated values against pH (dashed line). Bottom pane: Relationships between Fe<sup>III</sup> activity and pH at 298 K, assuming the enthalpy change of Fe<sup>III</sup>(OH)<sub>3(s)</sub> solubility of Liu and Millero.<sup>[21]</sup> Solid line: relationship derived using Model VII; dashed line: relationship derived using Model VI.

Comparing Fe<sup>III</sup> activities calculated using Model VI and Model VII clearly shows that the latter predicts stronger binding of Fe<sup>III</sup> to humics, and that the increase in predicted binding strength becomes larger at lower pH, giving a somewhat smaller slope of log  $a_{\text{Fe}^{3+}}$  activity against pH. As was done previously, it is possible to generalise the activity–pH–temperature relationship, assuming the enthalpy change for Fe(OH)<sub>3</sub> precipitation of Liu and Millero<sup>[21]</sup>:

$$\log \{\text{Fe}^{3+}\} = -18.15 - 2.49\text{pH} + 5253/T \quad (\text{A1})$$

where  $T$  is the temperature in Kelvin. Alternatively, the activity can be expressed in terms of a solid phase solubility:

$$K_{\text{so}} = \{\text{Fe}^{3+}\} \cdot \{\text{H}^+\}^{-2.49} \text{ or } \log K_{\text{so}} = \log \{\text{Fe}^{3+}\} + 2.49 \text{ pH} \quad (\text{A2})$$

$$\log K_{\text{so}} = -18.15 - 5253/T \quad (\text{A3})$$

At  $T = 298$  K,  $\log K_{\text{so}} = -0.51$ . The root mean squared error in the regression of  $\log a_{\text{Fe}^{3+}}$  against pH at 283K was 0.68; this was used (rounded up to 0.7) as the standard deviation of the sampling distribution of  $\log K_{\text{so}}$  for calculation of uncertainty in WHAM/Model VII.

## References

- [1] J. A. B. Bass, R. Blust, R. T. Clarke, T. A. Corbin, W. Davison, K. A. C. De Schamphelaere, C. R. Janssen, E. J. J. Kalis, M. G. Kelly, N. T. Kneebone, A. J. Lawlor, S. Loftus, E. J. M. Temminghoff, S. A. Thacker, E. Tipping, C. D. Vincent, K. W. Warnken, H. Zhang, *Environmental quality standards for trace metals in the aquatic environment. Environment Agency Science Report – SC030194 2008* (Environment Agency: Bristol, UK).
- [2] J. Cao, H. B. Xue, L. Sigg, Effects of pH and Ca competition on complexation of cadmium by fulvic acids and by natural organic ligands from a river and a lake. *Aquat. Geochem.* **2006**, *12*, 375. [doi:10.1007/s10498-006-9004-6](https://doi.org/10.1007/s10498-006-9004-6)
- [3] C. Fortin, Y. Couillard, B. Vigneault, P. G. C. Campbell, Determination of Free Cd, Cu and Zn concentrations in lake waters by in situ diffusion followed by column equilibration ion-exchange. *Aquat. Geochem.* **2010**, *16*, 151. [doi:10.1007/s10498-009-9074-3](https://doi.org/10.1007/s10498-009-9074-3)
- [4] Y. Gopalapillai, I. I. Fasfous, J. D. Murimboh, T. Yapici, P. Chakraborty, C. L. Chakrabarti, Determination of free nickel ion concentrations using the ion exchange technique: application to aqueous mining and municipal effluents. *Aquat. Geochem.* **2008**, *14*, 99. [doi:10.1007/s10498-008-9027-2](https://doi.org/10.1007/s10498-008-9027-2)
- [5] J. W. Guthrie, N. M. Hassan, M. S. A. Salam, I. I. Fasfous, C. A. Murimboh, J. Murimboh, C. L. Chakrabarti, D. C. Grégoire, Complexation of Ni, Cu, Zn, and Cd by DOC in some metal-impacted freshwater lakes: a comparison of approaches using electrochemical determination of free-metal-ion and labile complexes and a computer speciation model, WHAM V and VI. *Anal. Chim. Acta* **2005**, *528*, 205. [doi:10.1016/j.aca.2004.10.003](https://doi.org/10.1016/j.aca.2004.10.003)

- [6] E. J. J. Kalis, L. Weng, F. Dousma, E. J. M. Temminghoff, W. H. van Riemsdijk, Measuring Free metal ion concentrations in situ in natural waters using the Donnan membrane technique. *Environ. Sci. Technol.* **2006**, *40*, 955. [doi:10.1021/es051435v](https://doi.org/10.1021/es051435v)
- [7] S. Meylan, N. Odzak, R. Behra, L. Sigg, Speciation of copper and zinc in natural freshwater: comparison of voltammetric measurements, diffusive gradients in thin films (DGT) and chemical equilibrium models. *Anal. Chim. Acta* **2004**, *510*, 91. [doi:10.1016/j.aca.2003.12.052](https://doi.org/10.1016/j.aca.2003.12.052)
- [8] A. Plöger, E. Fischer, H.-P. Nirmaier, L. M. Laglera, D. Monticelli, C. M. G. van den Berg, Lead and copper speciation in remote mountain lakes. *Limnol. Oceanogr.* **2005**, *50*, 995. [doi:10.4319/lo.2005.50.3.0095](https://doi.org/10.4319/lo.2005.50.3.0095)
- [9] J. Qian, H. B. Xue, L. Sigg, A. Albrecht, Complexation of cobalt by natural ligands in freshwater. *Environ. Sci. Technol.* **1998**, *32*, 2043. [doi:10.1021/es971018l](https://doi.org/10.1021/es971018l)
- [10] E. R. Unsworth, K. W. Warnken, H. Zhang, W. Davison, F. Black, J. Buffle, J. Cao, R. Cleven, J. Galceran, P. Gunkel, E. Kalis, D. Kistler, H. P. van Leeuwen, M. Martin, S. Noël, Y. Nur, N. Odzak, J. Puy, W. van Riemsdijk, L. Sigg, E. J. M. Temminghoff, M.-L. Tercier-Waeber, S. Topperwien, R. M. Town, L. Weng, H. B. Xue, Model predictions of metal speciation in freshwaters compared to measurements by in situ techniques. *Environ. Sci. Technol.* **2006**, *40*, 1942. [doi:10.1021/es051246c](https://doi.org/10.1021/es051246c)
- [11] L. Van Laer, E. Smolders, F. Degryse, C. Janssen, K. A. C. De Schampelaere, Speciation of nickel in surface waters measured with the Donnan membrane technique. *Anal. Chim. Acta* **2006**, *578*, 195. [doi:10.1016/j.aca.2006.06.070](https://doi.org/10.1016/j.aca.2006.06.070)
- [12] H. B. Xue, L. Sigg, Free cupric ion concentration and Cu(II) speciation in a eutrophic lake. *Limnol. Oceanogr.* **1993**, *38*, 1200. [doi:10.4319/lo.1993.38.6.1200](https://doi.org/10.4319/lo.1993.38.6.1200)
- [13] H. B. Xue, L. Sigg, Zinc speciation in lake waters and its determination by ligand-exchange with EDTA and differential-pulse anodic-stripping voltammetry. *Anal. Chim. Acta* **1994**, *284*, 505–515. [doi:10.1016/0003-2670\(94\)85057-7](https://doi.org/10.1016/0003-2670(94)85057-7)
- [14] L. Emmenegger, D. W. King, L. Sigg, B. Sulzberger, Oxidation kinetics of Fe<sup>II</sup> in a eutrophic Swiss lake. *Environ. Sci. Technol.* **1998**, *32*, 2990. [doi:10.1021/es980207g](https://doi.org/10.1021/es980207g)
- [15] P. Kauppi, P. Anttila, K. Kenttämies, *Acidification in Finland* **2000** (Springer-Verlag: Berlin).
- [16] H. B. Xue, R. Gachter, L. Sigg, Comparison of Cu and Zn cycling in eutrophic lakes with oxic and anoxic hypolimnion. *Aquat. Sci.* **1997**, *59*, 176. [doi:10.1007/BF02523179](https://doi.org/10.1007/BF02523179)
- [17] F. Ramisch, M. Dittrich, C. Mattenberger, B. Wehrli, A. Wuest, Calcite dissolution in two deep eutrophic lakes. *Geochim. Cosmochim. Acta* **1999**, *63*, 3349. [doi:10.1016/S0016-7037\(99\)00256-2](https://doi.org/10.1016/S0016-7037(99)00256-2)
- [18] R. Giovanoli, J. L. Schnoor, L. Sigg, W. Stumm, J. Zobrist, Chemical weathering of crystalline rocks in the catchment area of acidic Ticino lakes, Switzerland. *Clays Clay Miner.* **1988**, *36*, 521. [doi:10.1346/CCMN.1988.0360605](https://doi.org/10.1346/CCMN.1988.0360605)
- [19] A. Calderoni, R. Mosello, A. Quirci, Chemical response of Lake Orta (northern Italy) to liming. *Arch. Hydrobiol.* **1991**, *122*, 421.

- [20] S. Loft, E. Tipping, J. Hamilton-Taylor, The chemical speciation of Fe<sup>III</sup> in freshwaters. *Aquat. Geochem.* **2008**, 14, 337. [doi:10.1007/s10498-008-9040-5](https://doi.org/10.1007/s10498-008-9040-5)
- [21] X. Liu, F. J. Millero, The solubility of iron hydroxide in sodium chloride solutions. *Geochim. Cosmochim. Acta* **1999**, 63, 3487. [doi:10.1016/S0016-7037\(99\)00270-7](https://doi.org/10.1016/S0016-7037(99)00270-7)