model values (Fig. 5(a)) in order to improve the fits to the angular distribution at 10.74 MeV (Fig. 3).

The background phases at the resonance energy were then changed by the same amounts. The fits to the differential cross sections presented in Figure 1 were obtained

$egin{array}{c} { m Proton} \ { m Energy} \ {E_p} \ ({ m MeV}) \end{array}$	17 F-Level Energy E_x (MeV)	Spin and Parity J^{π}	Orbital Angular Momentum <i>l</i>	Total Width Γ (MeV)	Ratio of Partial to Total Width Γ _p /Γ	$\frac{\gamma_{lj}^2}{3\hbar^2/2Ma^2} = \theta_{lj}^2$
$10 \cdot 52$ $12 \cdot 40$	$10 \cdot 50 \\ 12 \cdot 26$	$\frac{7}{2}$ - $\frac{3}{2}$ -	3 1	0.15 0.20	$\begin{array}{c} 0\cdot 3 \\ 0\cdot 3_5 \end{array}$	0·010 0·23

ARAMETERS	USED	IN	LEVEL	ANALYSES

P

using the parameters presented in Table 1, which also gives the fractions θ_{ij}^2 of the Wigner sum rule limit $3\hbar^2/2Ma^2$ (Teichmann and Wigner 1952) constituted by γ_{ij}^2 . Note that use was made of Lane and Thomas's (1958) definition of the reduced width γ^2 , being Wigner's γ^2 divided by the channel radius a. Note also that the



fit obtained. (See also caption of Figure 5.)

values of l, given in Table 1 are not, of course, quantum numbers of the compound nucleus levels of 17 F.

The same procedure was applied to the level at $12 \cdot 39$ MeV (Figs. 2, 4, and 5(b)) except that, in addition to the combinations of values (l,j) tried for the level

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at 10.52 MeV, $(4, \frac{7}{2})$ and $(4, \frac{9}{2})$ were tried. (It was assumed that $\delta_{4,7/2} = \delta_{4,9/2} = 0$.) The best fit was obtained for l = 1 and $j = \frac{3}{2}$. The parameters used are presented in Table 1.

IV. COMPARISON WITH OPTICAL MODEL CALCULATIONS

Duke (1963) obtained good fits to the ${}^{16}O(p, p)$ cross sections at energies between 8.66 and 19.2 MeV in an optical model analysis. No resonance analysis was attempted by Duke but he obtained nevertheless a reasonable fit to the resonance structure at 10.5 MeV by allowing the parameters describing the optical potential



Fig. 5.—The optical model phase shifts at (a) 10.74 MeV, (b) 12.6 MeV, for the different partial waves as obtained by Hardie, Dangle, and Oppliger (1963) are represented in the complex plane by tails of arrows in the points $\alpha_{Ij} = \{\exp(2i\delta_{Ij}) - 1\}/2i$. An improved fit to the angular distribution was obtained by small alterations of the phase shifts, the new values being represented by the tips of the arrows. (For the absorption cross section to remain positive, the values of α_{Ij} have to be kept inside the circle.)

to vary rapidly with energy. In such a description one would expect a single partial wave to be "suddenly" absorbed at the resonance energy; for the resonance at $E_{\rm p} = 10.52$ MeV this would be the $f_{7/2}$ partial wave. Duke (1963, p. 689) reported such a strong absorption at this energy. This seems to support our spin and parity assignment of the 10.52 MeV level.

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