

## Measurement of Apparent Spin-Spin Relaxation Times in Nuclear Quadrupole Resonance using a Double Pulsed Super-regenerative Oscillator

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### Abstract

A super-regenerative oscillator has been used to obtain apparent spin-spin relaxation times  $T_2^*$  for nuclear quadrupole resonance signals from some polycrystalline compounds. A mathematical analysis is given to show how  $T_2^*$  values may be obtained from a double pulsed super-regenerative oscillator for both logarithmic and linear modes of detection; each of these modes is described. Results obtained from both modes of operation are examined.

### Introduction

In a previous publication (Doolan and Hacobian 1973) we have described the detection of nuclear quadrupole resonance (n.q.r.) using a super-regenerative oscillator (SRO) that is quenched externally by a double pulse signal. The present paper provides a more complete analysis of this method of detection to show how apparent spin-spin relaxation times  $T_2^*$  may be evaluated. Before proceeding with this analysis, the operation of the SRO is examined to explain what is meant by linear and logarithmic modes of detection. The changes in  $T_2^*$  with impurity concentration in solid mixtures of *p*-dichlorobenzene will be examined in a subsequent communication.

### Super-regenerative Oscillator

#### *Spectrometer*

A block diagram of the spectrometer used to record n.q.r. signals is given in Fig. 1. The SRO designed to obtain  $T_2^*$  values is shown schematically in Fig. 2 and is a modified form of a circuit published by Narath *et al.* (1964). The SRO arrangement used here is cheaper and easier to construct than the spin-echo apparatus employed by other workers (e.g. Bloom *et al.* 1955; Woessner and Gutowsky 1963). Also, the high frequency stability required for the RF oscillator in the spin-echo technique is not necessary when using the SRO. The quench and oscillator tubes  $V_2$  and  $V_1$  of Fig. 2 were taken from separate valves to avoid any interelectrode interference that may arise from using the twin triodes of one glass envelope. The SRO was frequency modulated with a 30 Hz square wave signal applied to a TRW PG 222 variable capacitance diode (varicap) with a +40 V reverse bias. Other workers (Dixon and Bloembergen 1964; Caldwell 1973) have reported that amplitude modulation results when varicaps are used to obtain frequency modulation and have proposed methods to eliminate it. Although amplitude modulation was obtained with the SRO of Fig. 2, it was reduced to a negligible level by adjustment of the trimmer capacitors in the tuned circuit and careful choice of the other components.

The quench signal, shown schematically in Fig. 3, consisted of a train of negative pulses of amplitude  $-10$  V supplied by a Philips modular pulse generator to the quench input of the SRO. This train of pulses is inverted at the plate of  $V_2$  so that the grid of  $V_1$  is at earth potential during the quench pulses and RF oscillations build up exponentially (Frink 1938; Whitehead 1950) from noise and/or any signal in the tuned circuit. Between quench pulses the grid of  $V_1$  is at about  $-30$  V and  $V_1$  is cut off, damping out the RF oscillations.

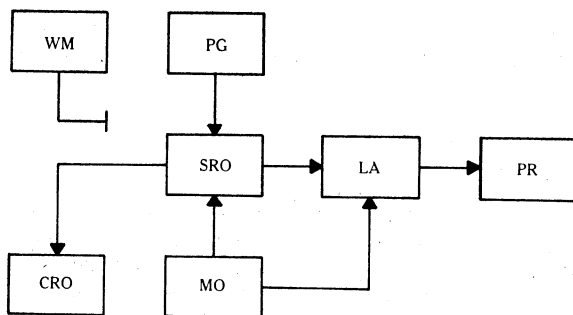


Fig. 1. Block diagram of the n.q.r. spectrometer:

WM, loosely coupled wavemeter; PG, Philips modular pulse generator model PM5720/40; SRO, super-regenerative oscillator; LA, lock-in amplifier; PR, pen recorder; CRO, oscilloscope for display of RF pulses; MO, modulation oscillator.

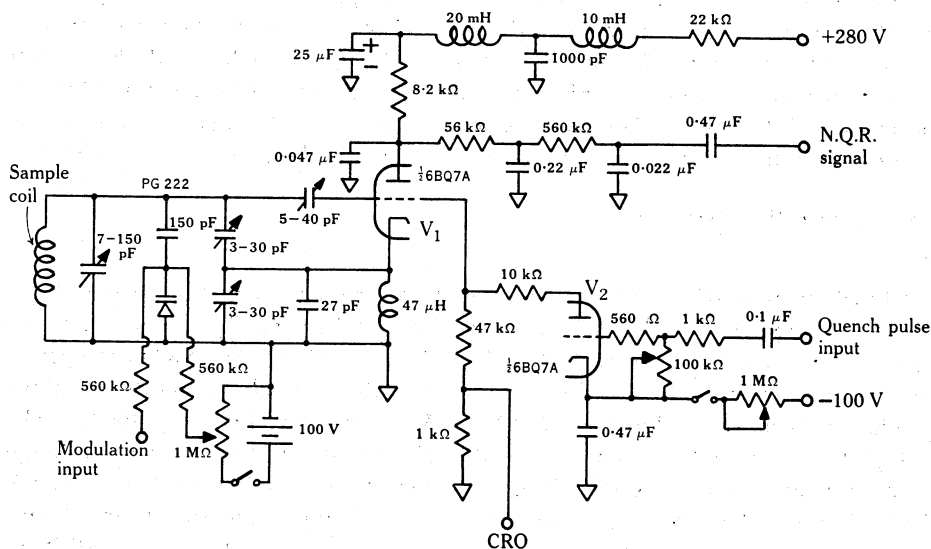


Fig. 2. Circuit diagram of the SRO.

When the rise time of the quench pulses was very fast the high frequency components of the rise time induced RF buildup in the SRO tuned circuit so that the RF pulses were generated from these HF components rather than n.q.r. Results for the variation of n.q.r. signal amplitude at the pen recorder output versus quench pulse rise time are given in Fig. 4, for the experimental conditions described. In all

experiments to determine relaxation times the quench pulse rise time was kept fixed at  $3 \mu\text{s}$ .

### RF Pulse Area Increase

An SRO is essentially a c.w. oscillator that is periodically turned off by a quench signal which damps out RF oscillations, as explained in the previous subsection. The RF pulses build up exponentially from noise and/or any signal at the oscillator frequency in the tuned circuit and, since they build up earlier when initiated by a signal, these pulses have longer durations and increased 'area' (measured in volt-seconds), as shown in Fig. 5. The waveforms of the quench pulse and RF pulse envelope at the grid of  $V_1$  are shown in Fig. 5b for the case where the RF pulse reaches equilibrium oscillation. This grid waveform is inverted and amplified at the plate of  $V_1$ .

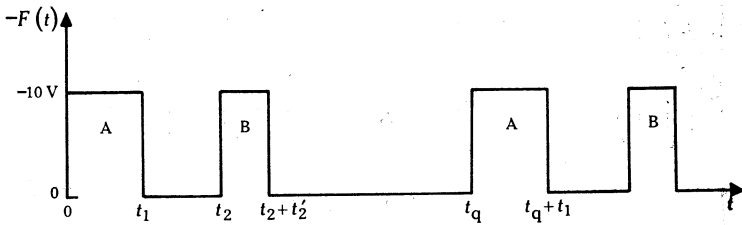


Fig. 3. Schematic representation in the time domain of a double pulse quench signal  $F(t)$  with A and B pulses of duration  $t_1$  and  $t_2'$  respectively.

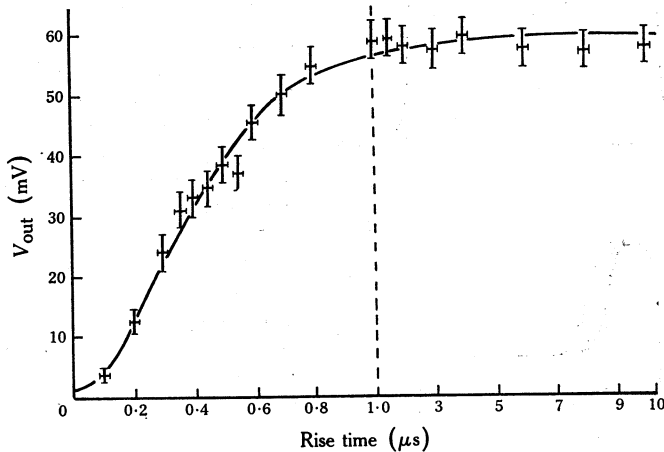


Fig. 4. Dependence of n.q.r. output signal  $V_{\text{out}}$  on quench pulse rise time. The sample used was *p*-dichlorobenzene at  $21^\circ\text{C}$  and the pulse characteristics were  $t_q = 1000 \pm 10 \mu\text{s}$ ,  $t_1 = t_2' = 40 \pm 1 \mu\text{s}$  and  $\tau (= t_2 - t_1) = 30 \pm 1 \mu\text{s}$ , with a pulse fall time of  $400 \pm 10 \text{ ns}$  and an SRO frequency of  $34.3 \text{ MHz}$ .

The time constant of the integrating circuit at the plate of  $V_1$ , which consists of a resistor  $R$  of  $56 \text{ k}\Omega$  and a capacitor  $C$  of  $0.22 \mu\text{F}$ , is approximately  $10 \text{ ms}$ . For the experiments described here the quench pulses had durations of less than  $100 \mu\text{s}$  so that during a quench pulse the charge on the  $0.22 \mu\text{F}$  capacitor only reached a low

level. If  $V_C$  and  $V_R$  are the voltages across  $C$  and  $R$  respectively and  $V_P$  is the total voltage across  $C$  and  $R$  then, during a quench pulse,

$$V_P = V_R + V_C \approx iR,$$

since we have  $V_C \ll V_R$  and  $i$  is the current flow through  $R$ . At frequencies greater than 100 Hz most of the current  $i$  flows through  $C$  so that

$$V_C \approx C^{-1} \int i dt \approx (1/RC) \int V_P dt. \quad (1)$$

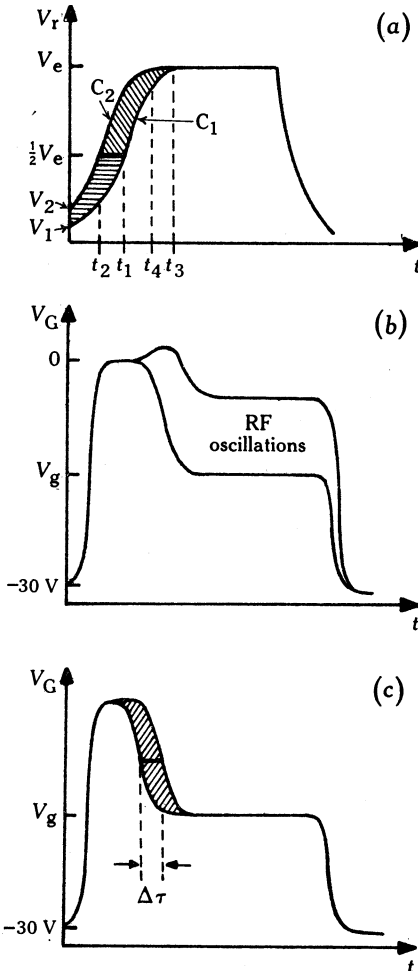


Fig. 5. Waveforms observed in the tuned circuit and at the grid of  $V_1$  of the SRO at equilibrium oscillation:

(a) Half of the RF pulse envelope in the tuned circuit when the equilibrium amplitude  $V_e$  is reached.  $V_1$  and  $V_2$  are the amplitudes of RF buildup after initiation by noise and noise plus signal respectively,  $t_2$  and  $t_1$  are the times at which the RF pulses have risen to half of their equilibrium level, and  $t_4$  and  $t_3$  are the times at which equilibrium oscillation is reached.

(b) RF and quench pulse waveforms observed at the grid of  $V_1$  of Fig. 2 at equilibrium oscillation. As the RF pulse builds up, the grid bias of  $V_1$  becomes more negative, reaching a static value when the pulse attains equilibrium (Whitehead 1950).

(c) Grid voltage  $V_G$  for two RF pulse leading edges which correspond to two initiating signal amplitudes in the tuned circuit;  $\Delta\tau$  is called the time of advance. The complete RF pulse envelopes are not shown.

Let  $V_P$  be equal to  $GV_G$ , where  $V_G$  is the grid waveform of Fig. 5c and  $G$  is the voltage gain of the circuit. It is not necessary to take the DC voltage at the plate of  $V_1$  into account because there is a capacitor between the output of the SRO and the lock-in amplifier. During an RF pulse it will be assumed that there are many oscillations so that it is only necessary to consider the pulse envelope when evaluating its area. Consequently the voltage across  $C$  during a quench pulse is determined by

the pulse envelope of Fig. 5c and

$$V_C \approx (G/RC) \int V_G dt. \quad (2)$$

The voltage across  $C$  is proportional to the area under the function  $V_G$ . When a signal is detected the RF pulses will build up earlier and equation (2) will have the form

$$V'_C \approx (G/RC) \int V'_G dt, \quad (3)$$

where  $V'_C$  and  $V'_G$  represent the new values of  $V_C$  and  $V_G$ .

If the SRO is frequency modulated by a low frequency square wave signal with a mark space ratio of 1, half of the quench pulses which occur during a modulation cycle and can detect a signal, will detect one signal level, while the other half will detect another signal level. From equations (2) and (3) the difference in output signal across the capacitor  $C$  between consecutive half-modulation cycles for the above modulation signal is given by

$$\frac{nt_m}{2t_q}(V'_C - V_C) = \frac{nt_m G}{2t_q RC} \int (V'_G - V_G) dt, \quad (4)$$

where  $nt_m/2t_q$  is the number of quench pulses per half modulation cycle which can detect a signal,  $t_m$  and  $t_q$  being the modulation and quench periods respectively and  $n$  the number of pulses per quench period which can detect a signal. For double pulse detection of n.q.r. the value of  $n$  is 1. The output signal voltage  $V_{out}$  at the pen recorder of Fig. 1 is given by

$$V_{out} = k_1(nt_m G/2t_q RC) \Delta A_g, \quad (5)$$

where  $\Delta A_g$  is the area increase of the grid waveform, and represents the integral of equation (4), and  $k_1$  is a constant for constant gain of the pen recorder and lock-in amplifier. Equation (5) may be written in the form

$$V_{out} = k_2 \Delta A_g/t_q, \quad (6)$$

where  $k_2$  is constant if  $k_1$ ,  $n$ ,  $t_m$  and  $G$  are all kept constant.

### Logarithmic Mode

In the logarithmic mode of operation RF oscillations build up to an equilibrium amplitude when the supply of energy by the valve  $V_1$  is equal to the loss of energy from the tuned circuit. As in Fig. 5a, let  $t_4$  and  $t_3$  be the times at which equilibrium oscillation of a particular RF pulse is reached when different signal amplitudes initiate RF buildup. The difference  $t_3 - t_4 = \Delta\tau$  is called the time of advance of the RF pulse due to increase in signal amplitude at the tuned circuit.

The diagram in Fig. 6 of the envelope of the RF pulse buildup in the SRO tuned circuit was obtained by tracing an oscilloscope display onto a sheet of polythene fixed to the screen of the oscilloscope. To obtain this display, a coil consisting of three turns of gauge 16 copper wire and having twice the diameter of the sample coil was

placed coaxially with the sample coil so that the centres of the two coils were about 5 cm apart. The RF oscillations induced in this coil were displayed on a Tektronix 7704 oscilloscope.

Let an RF pulse in the tuned circuit building up from noise reach a voltage  $V_1$  at  $t = 0$ ,  $\frac{1}{2}V_e$  at  $t_1$  and  $V_e$  at  $t_3$ , as shown in Fig. 5a. Similarly, let a pulse building up from noise and signal reach an amplitude  $V_2$  at  $t = 0$ ,  $\frac{1}{2}V_e$  at  $t_2$  and  $V_e$  at  $t_4$ . The voltages  $V_1$  and  $V_2$  are related to the initiating voltages by (Frink 1938; Whitehead 1950)

$$V_1 = \rho \langle V_n^2 \rangle^{\frac{1}{2}}, \quad V_2 = \rho (\langle V_n^2 \rangle + \langle V_s^2 \rangle)^{\frac{1}{2}}, \quad (7)$$

where  $\rho$  is the voltage gain up to the time  $t = 0$ ,  $\langle V_n^2 \rangle$  is the mean square noise voltage at the tuned circuit and  $\langle V_s^2 \rangle$  is the mean square signal voltage that initiates

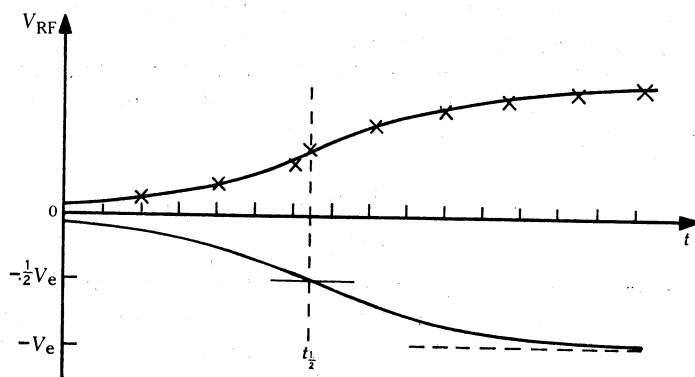


Fig. 6. Initial RF pulse buildup to equilibrium, as traced from an oscilloscope display.  $V_{RF}$  is the pulse amplitude and one division on the time axis represents  $0.2 \mu s$ . At time  $t_{\frac{1}{2}}$  the pulse has reached half its equilibrium level. The crosses were plotted using (with  $a = 0.70 \mu s$ )

$$\begin{aligned} & V_1 \exp(t/a) && \text{for } t < t_{\frac{1}{2}}, \\ & \frac{1}{2}V_e + \frac{1}{2}V_e(1 - \exp\{-(t - t_{\frac{1}{2}})/a\}) && \text{for } t \geq t_{\frac{1}{2}}. \end{aligned}$$

RF buildup at an earlier time in the tuned circuit. The area bounded by the curves  $C_1$  and  $C_2$  of Fig. 5a is equal to the sum of an infinite number of trapezia each with base  $\Delta\tau$  and infinitesimal height. This sum is given by

$$\Delta A = \Delta\tau V_e,$$

since the area of a trapezium is equal to the base length multiplied by its perpendicular height. Similarly, the area increase of the grid waveform,  $\Delta A_g$ , is  $\Delta\tau V_g$ , where  $V_g$  is defined in Fig. 5c. Substitution of these results into equation (6) gives

$$V_{out} = k_3 \Delta\tau V_e / t_q = k_3 \Delta A / t_q, \quad (8)$$

where  $k_3 = k_2 V_g / V_e$  is constant for a particular SRO with constant operating conditions.

The area increase  $\Delta A$  is calculated as follows. As in Fig. 6, RF buildup to  $\frac{1}{2}V_e$  is given by the function  $\exp(t/a)$ , while the buildup between  $\frac{1}{2}V_e$  and  $V_e$  is given by

$$\frac{1}{2}V_e + \frac{1}{2}V_e \{1 - \exp(-(t - t_{\frac{1}{2}})/a)\}.$$

Let the area between the curves  $C_1$  and  $C_2$  below  $\frac{1}{2}V_e$  in Fig. 5a be  $\Delta A_1$  and that above  $\frac{1}{2}V_e$  be  $\Delta A_2$ . Then

$$\Delta A_1 = V_2 \int_0^{t_2} \exp(t/a) dt + \frac{1}{2}V_e(t_1 - t_2) - V_1 \int_0^{t_1} \exp(t/a) dt,$$

that is,

$$\Delta A_1 = a(V_1 - V_2) + \frac{1}{2}aV_e \ln(V_2/V_1). \quad (9)$$

Similarly,

$$\begin{aligned} \Delta A_2 &= \frac{1}{2}V_e \int_{t_2}^{t_4} \{2 - \exp(-(t - t_2)/a)\} dt + V_e(t_3 - t_4) - \frac{1}{2}V_e(t_1 - t_2) \\ &\quad - \frac{1}{2}V_e \int_{t_1}^{t_3} \{2 - \exp(-(t - t_1)/a)\} dt \\ &= \frac{1}{2}V_e(t_1 - t_2) + \frac{1}{2}aV_e \{\exp(-(t_4 - t_2)/a) - \exp(-(t_3 - t_1)/a)\}. \end{aligned} \quad (10a)$$

Since  $t_4 - t_2 = t_3 - t_1$ , equation (10a) reduces to

$$\Delta A_2 = \frac{1}{2}aV_e \ln(V_2/V_1). \quad (10)$$

Combining equations (9) and (10), the total area increase is given by

$$\Delta A = \Delta A_1 + \Delta A_2 \approx aV_e \ln(V_2/V_1), \quad (11)$$

because  $V_1$  and  $V_2$  are of the order of the initiating voltages and are small compared with  $V_e$ . Substituting for  $V_2$  and  $V_1$  from equations (7) we then have

$$\Delta A \approx aV_e \ln\{(\langle V_s^2 \rangle + \langle V_n^2 \rangle) / \langle V_n^2 \rangle\}^{\frac{1}{2}}, \quad (12)$$

and thus from equation (8)

$$V_{out} = \frac{k_3 a V_e}{t_q} \ln\left(\frac{\langle V_s^2 \rangle + \langle V_n^2 \rangle}{\langle V_n^2 \rangle}\right)^{\frac{1}{2}}. \quad (13)$$

Equation (13) relates the output voltage at the pen recorder to the RF signal voltage in the tuned circuit of the SRO when the RF pulses reach equilibrium oscillation. This equation also holds for a diode detector which is loosely coupled to the sample coil. For a particular value  $V_x$  of  $V_{out}$ , for which  $\Delta\tau = \Delta\tau_x$ , equation (8) may be written as

$$V_x = k_3 \Delta\tau_x V_e / t_q \quad \text{or} \quad k_3 = V_x t_q / \Delta\tau_x V_e. \quad (14a, b)$$

Substituting equation (14b) into (13), we have

$$V_{out} = \frac{a V_x}{\Delta\tau_x} \ln\left(\frac{\langle V_s^2 \rangle + \langle V_n^2 \rangle}{\langle V_n^2 \rangle}\right)^{\frac{1}{2}}. \quad (15)$$

To measure  $\Delta\tau_x$  for the circuit of Fig. 2, the buildup of the RF pulses was displayed on a Tektronix 7704 oscilloscope while the SRO was detecting a signal generated by an RF oscillator. For square wave modulation, the pulse envelopes alternated

between two values corresponding to the two signal amplitudes which were initiating RF buildup in the SRO tuned circuit. The leading edges of the RF pulses alternated between two well-defined positions separated by the interval  $\Delta\tau_x$ . At the same time that  $\Delta\tau_x$  was measured, the corresponding output voltage  $V_x$  at the pen recorder was noted. All of the RF pulses of the SRO detected the signal from the RF generator. For double pulse quenching,  $t_q$  was made long enough so that only half of the pulses were able to detect n.q.r. and, as a result, the value of  $V_x$  required was half of the peak to peak output voltage. The values of  $V_e$  and  $t_q$  were also measured from the oscilloscope display. The value of  $k_3$  was found by substituting results for  $V_e$ ,  $t_q$ ,  $\Delta\tau_x$  and  $V_x$  into equation (14b). The time constant  $a$  of RF buildup was determined as indicated in Fig. 6 by fitting a curve of the form  $\exp(t/a)$  to the pulse buildup.

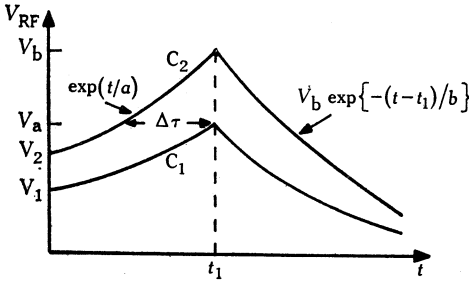


Fig. 7. Half RF pulse envelope  $V_{RF}$  when oscillation is damped out well below equilibrium. Curve  $C_1$  builds up to  $V_a$  at time  $t_1$  from noise while  $C_2$  builds up to  $V_b$  at  $t_1$  from noise plus signal.

### Linear Mode

In the linear mode of operation, RF oscillations are damped out well before equilibrium is reached. Oscillations build up and decay exponentially (Frink 1938; Whitehead 1950) with respect to time, as shown in Fig. 7. The RF pulses at the grid of  $V_1$  and in the SRO tuned circuit have the same buildup envelope, and the pulse area increase at the plate of  $V_1$  is given by a constant times the area between curves  $C_1$  and  $C_2$  of Fig. 7 up to the time  $t_1$ , that is,

$$\begin{aligned} \Delta A &= \int_0^{t_1} V_2 \exp(t/a) dt - \int_0^{t_1} V_1 \exp(t/a) dt \\ &= a(V_2 - V_1)\{\exp(t_1/a) - 1\}. \end{aligned} \quad (16)$$

Substitution of this expression into equation (6) gives

$$V_{out} = (k'_2 a/t_q)(V_2 - V_1)\{\exp(t_1/a) - 1\}$$

and thus, using equations (7),

$$V_{out} = (k_4/t_q)\{(\langle V_s^2 \rangle + \langle V_n^2 \rangle)^{\frac{1}{2}} - \langle V_n^2 \rangle^{\frac{1}{2}}\}, \quad (17)$$

where  $k_4 = pak'_2\{\exp(t_1/a) - 1\}$  is a constant for a particular SRO with fixed operating conditions. For  $\langle V_s^2 \rangle \gg \langle V_n^2 \rangle$  equation (17) reduces to

$$V_{out} = (k_4/t_q)\langle V_s^2 \rangle^{\frac{1}{2}}. \quad (18)$$



If diode detection is used, similar equations to (17) and (18) result but  $\Delta A$  is taken as the area between the curves  $C_1$  and  $C_2$  of Fig. 7 and is evaluated by integrating over all values of  $t$ .

### Measurement of $T_2^*$

If an SRO is quenched with the double pulse train shown in Fig. 3, pairs of RF pulses occur in the tuned circuit. All of these pulses can excite n.q.r., but if the repetition time  $t_q$  of the double pulse train is long compared with the value of the apparent spin-spin relaxation time  $T_2^*$  for the sample that is being excited, the nuclear induction signal from a pair of pulses will have decayed well below noise at the arrival of the next pair. For this condition only the second pulses (B pulses) of each pair will detect the induction signal produced by the first (A) pulses of each pair. Thus if  $t_q \gg T_2^*$  and  $\tau = t_2 - t_1$  is long enough to allow the RF pulses A to decay well below noise before the buildup of the B pulses begins, the response of the SRO to an n.q.r. signal is given by equation (15) when the B pulses reach equilibrium and by equation (17) when they are damped out well below equilibrium. (If  $\tau$  is not long enough to allow this,  $\langle V_s^2 \rangle$  is replaced by  $\langle V_s^2 + V_a^2 \rangle$  in equation (7), where  $V_a$  is the amplitude of the RF pulse A which initiates the buildup of pulse B. Consequently in the present work  $\tau$  was kept greater than  $20 \mu s$  to avoid taking  $V_a$  into account.)

It has been shown for n.q.r. (Bloom *et al.* 1955) that the average components of the nuclear spin  $I$  of a sample after irradiation by an RF pulse in zero static magnetic field are given by

$$\langle I_x \rangle = \frac{1}{2} \xi^{\pm} \sin(\xi^{\pm} \gamma B_1 t_1) \sin\{\omega_0(t - t_1)\} \exp\left\{-((t - t_1)/T_2^*)^2\right\} \quad (19a)$$

and

$$\langle I_y \rangle = \langle I_z \rangle = 0, \quad (19b)$$

where

$$\xi = (I + |m|)(I - |m| + 1),$$

$m$  being the  $z$  component of  $I$ . In equation (19a),  $\gamma$  is the magnetogyric ratio of the nuclei undergoing n.q.r.,  $B_1$  is the amplitude of the RF magnetic field,  $t$  is the time,  $t_1$  is the duration of the RF pulse and  $\omega_0$  is the radio frequency (of the SRO). The apparent spin-spin relaxation time  $T_2^*$  is taken to be the time for the induction signal from the sample after one RF pulse to decay to  $e^{-1}$  times its maximum value. It should be noted that the quantities  $t_w$  and  $\delta$  used by Bloom *et al.* (1955) are related to  $t_1$  and  $T_2^*$  by  $t_1 = t_w$  and  $T_2^* = 2/\delta$ . For a single crystal in zero static magnetic field, the total magnetization  $M$  induced in the sample by an RF pulse is given by  $M = \gamma \hbar n \langle I_x \rangle$ , where  $n$  is the total number of nuclei which have been excited. For a polycrystalline sample  $B_1$  is replaced by  $B_1 \sin \theta$  (Bloom *et al.* 1955) and  $M$  is averaged with respect to  $\theta$ , the angle between  $B_1$  and the axis of quantization of  $I$ .

The magnetization  $M$  produces a magnetic induction  $B$  equal to  $\mu_0 M$  in free space (MKS units). As in Bloch's (1946) paper, the flux  $\Phi$  produced by  $B$  through the receiver coil of  $N$  turns containing a sample of cross sectional area  $A$  is given by

$$\Phi = \mu_0 NAM,$$

assuming the sample has a constant cross sectional area over the length of the coil.

The signal voltage  $V_s$  induced in the receiver coil is determined by (in MKS units)

$$V_s = -d\Phi/dt = -\mu_0 N A dM/dt.$$

Substitution of equation (19a) into this expression, with  $\tau = t - t_1$ , gives

$$V_s = -\frac{1}{2}\mu_0 N A \gamma \hbar n \xi^{\pm} \omega_0 \sin(\xi^{\pm} \gamma B_1 t_1) \times \left[ \cos(\omega_0 \tau) \exp\left\{-\left(\frac{\tau}{T_2^*}\right)^2\right\} - \frac{2\tau}{\omega_0 (T_2^*)^2} \sin(\omega_0 \tau) \exp\left\{-\left(\frac{\tau}{T_2^*}\right)^2\right\} \right]. \quad (20)$$

For the experimental work reported here  $2\tau/(T_2^*)^2$  is much less than  $\omega_0$  for all values of  $\tau$  used. Therefore the second term of equation (20) is neglected and, for a polycrystalline sample or single crystal, the mean square signal voltage induced in the sample coil may be written in the form

$$\langle V_s^2 \rangle = D^2 \exp\{-2(\tau/T_2^*)^2\}, \quad (21)$$

where  $D$  is a constant if  $N$ ,  $A$ ,  $\xi$ ,  $n$ ,  $\gamma$ ,  $B_1$ ,  $t_1$  and  $\omega_0$  are all held constant. This is possible if each of the RF pulses applied to the sample has fixed amplitude and duration, the RF frequency is constant and the sample has a fixed mass and occupies a constant volume in the given sample coil.

#### Logarithmic Mode

Substituting equation (21) into (15), we have

$$V_{out} = \frac{aV_x}{2\Delta\tau_x} \ln\left(\frac{D^2 \exp\{-2(\tau/T_2^*)^2\} + \langle V_n^2 \rangle}{\langle V_n^2 \rangle}\right).$$

Rearranging this expression, taking natural logarithms and putting  $b = (aV_x/2\Delta\tau_x)$ , gives

$$-2(\tau/T_2^*)^2 = \ln\{\exp(V_{out}/b) - 1\} + \ln\{\langle V_n^2 \rangle/D^2\}. \quad (22)$$

Equation (22) shows that, for logarithmic mode detection, the gradient of a graph of  $\ln\{\exp(V_{out}/b) - 1\}$  against  $\tau^2$  is  $-2/(T_2^*)^2$ , from which  $T_2^*$  can be evaluated.

#### Linear Mode

Substituting equation (21) into (17), we have

$$V_{out} = (k_4/t_q) [\{\langle V_n^2 \rangle + D^2 \exp(-2(\tau/T_2^*)^2)\}^{\frac{1}{2}} - \langle V_n^2 \rangle^{\frac{1}{2}}].$$

Rearranging this expression and taking natural logarithms gives

$$-2(\tau/T_2^*)^2 = \ln\{(V_{out} t_q/k_4 + \langle V_n^2 \rangle^{\frac{1}{2}})^2 - \langle V_n^2 \rangle\} - 2 \ln D. \quad (23)$$

If we have  $\langle V_s^2 \rangle \gg \langle V_n^2 \rangle$ , equation (23) reduces to

$$-(\tau/T_2^*)^2 \approx \ln(V_{out} t_q/k_4) - \ln D. \quad (24)$$

Equation (23) is difficult to apply because  $\langle V_n^2 \rangle$  must be determined before  $T_2^*$  can be evaluated. However, for  $\langle V_s^2 \rangle \gg \langle V_n^2 \rangle$ , the gradient of a graph of  $\ln V_{out}$  against  $\tau^2$  is  $-(T_2^*)^{-2}$ .

## Results

### Logarithmic Mode

Using double pulse quenching the result of Fig. 8 was obtained for fused *p*-dichlorobenzene and the experimental conditions listed. For logarithmic-mode detection, the second RF pulse (B) of each pair was allowed to build up to equilibrium oscillation so that equation (22) described the SRO response to an n.q.r. signal. The results of Table 1 were obtained from graphs similar to Fig. 8. For each determination,  $t_q$  was made large enough so that no signal was detected at the pen recorder for  $\tau = \frac{1}{2}t_q$ .

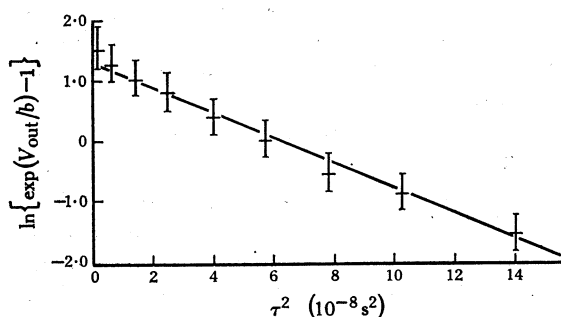


Fig. 8. Graph for determination of  $T_2^*$  for  $^{35}\text{Cl}$  n.q.r. in fused *p*-dichlorobenzene at  $25^\circ\text{C}$ . The pulse sequence was  $t_1 = 40 \pm 1 \mu\text{s}$  (A pulse),  $t_2' = 12 \pm 1 \mu\text{s}$  (B pulse) and  $t_q = 1000 \pm 10 \mu\text{s}$ , and the SRO frequency was  $34.3 \text{ MHz}$ . The experimental value of  $b$  was  $40 \pm 5 \text{ mV}$ . The result of the measurement was  $T_2^* = 310 \pm 15 \mu\text{s}$ .

Table 1.  $T_2^*$  values obtained using SRO

The SRO of Fig. 2 with double pulse quenching was used for the n.q.r. of the polycrystalline compounds listed. In all measurements  $t_1$  and  $t_2'$  were  $40 \pm 1$  and  $12 \pm 1 \mu\text{s}$  respectively. The results were obtained from graphs similar to Fig. 8

Nucleus	Compound	Temp.	$\omega_0$ (MHz)	$t_q$ ( $\mu\text{s}$ )	$T_2^*$ ( $\mu\text{s}$ )
$^{35}\text{Cl}$	<i>p</i> -dichlorobenzene	$25^\circ\text{C}$	34.3	1000	$310 \pm 15$
		81 K	34.8	1000	$205 \pm 10$
$^{37}\text{Cl}$	<i>p</i> -dichlorobenzene	$23^\circ\text{C}$	27.1	1000	$350 \pm 30$
		81 K	27.4	1000	$240 \pm 20$
$^{35}\text{Cl}$	$\text{NaClO}_3$	$23^\circ\text{C}$	30.0	1000	$330 \pm 30$
	$\text{SbCl}_3$	$31^\circ\text{C}$	19.0	1000	$200 \pm 15$
	$\text{SbCl}_3$	$31^\circ\text{C}$	20.4	1000	$180 \pm 20$
$^{63}\text{Cu}$	$\text{Cu}_2\text{O}$	$25^\circ\text{C}$	26.0	$300 \pm 4$	$34 \pm 3$
$^{65}\text{Cu}$	$\text{Cu}_2\text{O}$	$27^\circ\text{C}$	24.1	$200 \pm 4$	$30 \pm 3$

The results in Table 1 may be compared with the  $T_2^*$  values of  $310$  and  $230 \mu\text{s}$  for  $^{35}\text{Cl}$  n.q.r. in *p*-dichlorobenzene at room temperature and  $77 \text{ K}$  respectively, obtained by Woessner and Gutowsky (1963) using the spin-echo technique. They also found the  $^{63}\text{Cu}$  n.q.r. signal at room temperature to have a  $T_2^*$  value of about  $30 \mu\text{s}$ . No error estimates were given. Bloom *et al.* (1955) obtained an experimental value of  $T_2^* \sim 0.3 \text{ ms}$  for  $^{35}\text{Cl}$  n.q.r. at room temperature in polycrystalline  $\text{NaClO}_3$ , also using the spin-echo technique.

In the present work, the  $T_2^*$  values for  $^{37}\text{Cl}$  n.q.r. in *p*-dichlorobenzene were found to be significantly higher than those obtained for  $^{35}\text{Cl}$ , indicating that the  $^{35}\text{Cl}$  and  $^{37}\text{Cl}$  nuclei interact differently with the crystal lattice. The  $T_2^*$  values for  $^{35}\text{Cl}$  and

$^{37}\text{Cl}$  in fused *p*-dichlorobenzene were found to be lower at 81 K than at room temperature, presumably due to strains or other imperfections (Woessner and Gutowsky 1963) arising in the crystal lattice when it was cooled. The strong and weak  $^{35}\text{Cl}$  n.q.r. lines of polycrystalline  $\text{SbCl}_3$  gave the same  $T_2^*$  value within experimental error, as also did the n.q.r. lines of  $^{63}\text{Cu}$  and  $^{65}\text{Cu}$  in powdered  $\text{Cu}_2\text{O}$  at room temperature.

### Linear Mode

For linear-mode detection using double pulse quenching, the A pulses were allowed to reach equilibrium and were made long to excite as many nuclei as possible. The B pulses were made short enough ( $\sim 0.5 \mu\text{s}$ ) to ensure that RF oscillations were damped out well below equilibrium and their response to an n.q.r. signal was in the linear mode. As for the logarithmic mode,  $t_q$  was made sufficiently long so that no signal was detected by the pen recorder at  $\tau = \frac{1}{2}t_q$ .

Using equation (24) and assuming  $\langle V_s^2 \rangle \gg \langle V_n^2 \rangle$ , estimates of  $T_2^*$  were obtained from graphs of  $\ln V_{\text{out}}$  against  $\tau^2$ . The resulting values of  $T_2^*$  from this method were:  $230 \pm 10 \mu\text{s}$  for  $^{35}\text{Cl}$  in fused *p*-dichlorobenzene at  $24^\circ\text{C}$ ,  $220 \pm 20 \mu\text{s}$  for  $^{35}\text{Cl}$  in polycrystalline  $\text{NaClO}_3$  at  $23^\circ\text{C}$ , and  $240 \pm 10 \mu\text{s}$  for  $^{37}\text{Cl}$  in fused *p*-dichlorobenzene at  $25^\circ\text{C}$ . (The pulse sequence used was  $t_1 = 40 \pm 1 \mu\text{s}$ ,  $t'_2 = 0.5 \pm 0.2 \mu\text{s}$  and  $t_q = 1000 \pm 10 \mu\text{s}$ .) These  $T_2^*$  values are much lower than those obtained from the logarithmic-mode analysis and by the spin-echo technique (Bloom *et al.* 1955; Woessner and Gutowsky 1963). This indicates that the assumption  $\langle V_s^2 \rangle \gg \langle V_n^2 \rangle$  is incorrect for the experimental conditions used here. Since  $\langle V_n^2 \rangle$  is difficult to measure, equation (23) was not applied.

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