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*Soil Research*

## Supplementary Material

### **Modelling nitrous oxide emissions: comparing algorithms in six widely used agro-ecological models.**

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**Table S1. Source and equations to represent nitrification APSIM, DNDC, DayCent, FASSAT, NOE and WNMM. Abbreviations are given in Table S4.**

	Model	Equations	Source
<b>Nitrification rate</b>	APSIM	$R_n = R_{P\_n} \times f_{n(NH4)} \times \min(f_{n(SW)}, f_{n(ST)}, f_{n(pH)})$	Thorburn et al. 2010; Xing et al. 2011
	DNDC	$R_n = R_{p\_n} \times f_{n(NH4)} \times B_n \times f_{n(pH)}$	Li et al. 2000
	DayCent	$R_{n\_Max} = K_{max} \times f_{n(NH4)} \times f_{n(SW)} \times f_{n(ST)} \times f_{n(pH)} + K_1 \times N_{min}$ $R_n = \min(R_{p\_n}, C_{NH4} \times R_{n\_Max})$	Parton et al. 1996; del Grosso et al. 2000; Parton et al. 2001
	FASSAT	$R_n = R_{P\_n} \times f_{n(NH4)} \times f_{n(SW)} \times f_{n(ST)} \times f_{n(pH)}$	Chatskikh et al. 2005
	NOE	$R_n = \begin{cases} f_{n(NH4)} \times f_{n(SW)} \times f_{n(ST)} & WFPS < 0.8 \\ 0 & WFPS > 0.8 \end{cases}$	Henault et al. 2005
	WNMM	$R_n = R_{P\_n} \times f_{n(NH4)} \times (1.0 - \exp(-f_{n(SW)} \times f_{n(ST)} \times f_{n(pH)}))$	Li et al. 2007
<i>Soil moisture</i>	APSIM	$f_{n(SW)} = \begin{cases} WFD/0.5; & 0.0 < WFD \leq 0.25 \\ 1.0 ; & 0.5 < WFD \leq 1.0 \\ 1.0 - (WFD - 1.0) * 0.5; & 1.0 < WFD \leq 2.0 \\ 0; & WFD > 2.0 \end{cases}$ $WFD = \begin{cases} 1.0 + (SW - DUL)/(SAT - DUL) & SW > DUL \\ (SW - LL)/(DUL - LL) & SW \leq DUL \end{cases}$	Thorburn et al. 2010; Xing et al. 2011
	DNDC	$f_{n(SW)} = \begin{cases} 0.8 + 0.21 \times (1.0 - WFPS) & WFPS > 0.05 \\ 0 & WFPS \leq 0.05 \end{cases}$	Li et al. 2000
	DayCent	$f_{n(SW)} = \left( \frac{WFPS-b}{a-b} \right)^{d \times \frac{(b-a)}{(a-c)}} \times \left( \frac{WFPS-c}{a-c} \right)$	Parton et al. 1996; del Grosso et al. 2000; Parton et al. 2001

	FASSAT	$f_{n(SW)} = \begin{cases} 0.6 & \varphi \geq -9.81 \times 10^{-5} \\ 0.6 + 0.4 \times \log_{10}(-\frac{\varphi}{-9.81} \times 10^{-5})/1.5 & -9.81 \times 10^{-5} > \varphi \geq -3.1 \times 10^{-3} \\ 1.0 & -3.1 \times 10^{-3} > \varphi \geq -3.1 \times 10^{-2} \\ 1.0 - (\log_{10}(-\frac{\varphi}{-9.81} \times 10^{-5}) - 2.5)/3.0 & -3.1 \times 10^{-2} > \varphi \geq -3.1 \times 10^2 \\ 0.0 & -31 > \varphi \end{cases}$	Chatskikh et al. 2005
	NOE	$f_{n(SW)} = a \times SW_g + b$	Henault et al. 2005
	WNMM	$f_{n(SW)} = \begin{cases} \frac{SW-WP}{SW25-WP} & SW < SW25 \\ 1.0 & SW25 \leq SW < FC \\ 1.0 - \frac{SW-FC}{PO-FC} & SW > FC \end{cases}$	Li et al. 2007
<i>Soil temperature</i>	APSIM	$f_{n(ST)} = \begin{cases} (ST/32)^2 & 0 \leq ST \leq 32 \\ 1 & ST > 32 \end{cases}$	Thorburn et al. 2010; Xing et al. 2011
	DNDC	$f_{n(ST)} = ((60 - ST)/25.78)^{3.503} \times \exp(3.503 \times (ST - 34.22)/25.78)$	Li et al. 2000
	DayCent	$f_{n(ST)} = A_{nitr} + B_{nitr} \times \exp(C_{nitr} \times ST)$	Parton et al. 1996; Parton et al. 2001
	FASSAT	$f_{n(ST)} = a_u \times \exp(b_u + c_u \times ST \times (1 - 0.5 \times \frac{ST}{d_u}))$	Chatskikh et al. 2005
	NOE	$f_{n(ST)} = \begin{cases} \exp((ST - 11) \times \ln(89) - 9 \times \frac{\ln(2.1)}{10}) & ST < 11^\circ\text{C} \\ \exp((ST - 20) \times \frac{\ln(2.1)}{10}) & ST \geq 11^\circ\text{C} \end{cases}$	Henault et al. 2005
	WNMM	$f_{n(ST)} = 0.41 \times \frac{ST-5}{10} \quad ST > 5^\circ\text{C}$	Li et al. 2007

<i>soil pH</i>	APSIM	$f_{n(SW)} = \begin{cases} 0 & pH < 4.5 \\ \frac{pH-4.5}{1.5} & 4.5 \leq pH < 6.0 \\ 1.0 & 6.0 \leq pH < 8 \\ 9.0 - pH & 8.0 < pH \leq 9.0 \\ 0 & pH > 9.0 \end{cases}$	Thorburn et al. 2010; Xing et al. 2011
	DNDC	$f_{n(pH)} = pH$	Li et al. 2000
	DayCent	$f_{n(pH)} = 0.56 + \frac{\tan(\pi \times 0.45 \times (-5 + pH))}{\pi}$	Parton et al. 1996; del Grosso et al. 2000; Parton et al. 2001
	FASSAT	NA	Chatskikh et al. 2005
	NOE	NA	Henault et al. 2005
	WNMM	$f_{n(pH)} = \begin{cases} 0.307 \times pH - 1.269, & pH < 7.0 \\ 1.0, & 7.4 \geq pH \geq 7.0 \\ 5.367 - 0.599 \times pH, & pH > 7.4 \end{cases}$	Li et al. 2007
$\text{NH}_4^+$	APSIM	$f_{n(NH4)} = \frac{C_{NH4}}{K_m + C_{NH4}}$	Thorburn et al. 2010; Xing et al. 2011
	DNDC	$f_{n(NH4)} = C_{NH4}$	Li et al. 2000
	DayCent	$f_{n(NH4)} = 1 - e^{-0.0105 \times C_{NH4}}$	Parton et al. 1996; Parton et al. 2001; DayCent source code
	FASSAT	$f_{n(NH4)} = C_{NH4}$	Chatskikh et al. 2005
	NOE	$f_{n(NH4)} = \frac{C_{NH4}}{K_m + C_{NH4}}$	Henault et al. 2005
	WNMM	$f_{n(NH4)} = C_{NH4}$	Li et al. 2007

<i>Soil organic carbon</i>	APSIM	NA	Thorburn et al. 2010; Xing et al. 2011
	DNDC	$U_g = U_{max} \times (C_{DOC}/(1 + C_{DOC}) + f_{n(SW)}/(1 + f_{n(SW)}))$ $U_d = A_{max} \times B_n/(5 + C_{DOC})/(1 + f_{n(SW)})$ $U_b = (U_g - U_d)B_n \times f_{n(SW)} \times f_{n(ST)}$	Li et al. 2000
	DayCent	$f_{OC} = K_1 \times N_{min}$	Parton et al. 1996; del Grosso et al. 2000; Parton et al. 2001
	FASSAT	NA	Chatskikh et al. 2005
	NOE	NA	Henault et al. 2005
	WNMM	NA	Li et al. 2007
<i>N<sub>2</sub>O from nitrification</i>	APSIM	$N2O_n = K_{N2O\_n} \times R_n$ $K_{N2O\_n} = K_1$	Thorburn et al. 2010; Xing et al. 2011
	DNDC	$N2O_n = K_{N2O\_n} \times R_n \times f_{(ST\_N2O\_n)} \times WFPS$ $K_{N2O\_n} = K_1$ $N2O_n = K_{N2O\_n} \times R_n$	Li et al. 2000  Li (2000)
	DayCent	$N2O_n = K_{N2O\_n} \times R_n$ $K_{N2O\_n} = K_1$	Parton et al. 1996; del Grosso et al. 2000; Parton et al. 2001
	FASSAT	$N2O_n = K_{N2O\_n} \times R_n$ $K_{N2O\_n} = K_1 \times f_{(SW\_N2O\_n)} \times f_{(ST\_N2O\_n)}$ $f_{(ST\_N2O\_n)} = \min [1.0, \exp \left( -0.5 \left( \frac{ST - 2a_n}{a_n} \right)^2 \right)]$	Chatskikh et al. 2005
	NOE	$N2O_n = \begin{cases} K_{N2O\_d} \times K_{N2O\_n} \times R_n & WFPS < 0.62 \\ K_{N2O\_n} \times R_n & WFPS \geq 0.62 \end{cases}$	Henault et al. 2005

		$K_{N2O\_n} = K_1$	
	WNMM	$N2O_n = K_{N2O\_n} \times R_n$ $K_{N2O\_n} = K_1 \times f_{(SW\_N2O\_n)} \times f_{(ST\_N2O\_n)}$ $f_{(SW\_N2O\_n)} = f_{n(SW)}$ $f_{(ST\_N2O\_n)} = 0.9 \times \left( \frac{ST}{ST + \exp(9.93 - 0.312 \times ST)} \right) + 0.1$	Li et al. 2007

**Table S2. Source and equations to represent denitrification APSIM, DNDC, DayCent, FASSAT, NOE and WNMM. Abbreviations are given in Table S4.**

	Model	Equations	Source
Denitrification rate	APSIM	$R_d = R_{P\_d} \times f_{(NO_3)} \times f_{(C_{OC\_A})} \times f_{(SW\_d)} \times f_{(ST\_d)}$	Thorburn et al. 2010; Xing et al. 2011
	DNDC	See Table S3	
	DayCent	$R_d = \min(f_{(NO_3)}, f_{(CO_2)}) \times f_{(SW\_d)}$	Parton et al. 1996; del Grosso et al. 2000; Parton et al. 2001
	FASSAT	$R_d = R_{P\_d} \times f_{(NO_3)} \times f_{(SW\_d)} \times f_{(ST\_d)}$	Chatskikh et al. 2005
	NOE	$R_d = R_{P\_d} \times f_{(NO_3)} \times f_{(SW\_d)} \times f_{(ST\_d)}$	Henault et al. 2005
	WNMM	$R_d = \begin{cases} 0, & WFPS < 0.8 \\ f_{(NO_3)} \times (1.0 - \exp(-1.4 \times f_{(SW\_d)} \times f_{(ST\_d)} \times f_{(SOC)})), & WFPS \geq 0.8 \end{cases}$	Li et al. 2007
Soil moisture	APSIM	$f_{(SW\_d)} = \frac{SW-DUL}{SAT-DUL}$	Thorburn et al. 2010; Xing et al. 2011
	DNDC	See Table S3	
	DayCent	$f_{(SW\_d)} = 0.5 + a \tan(0.6 \times \pi \times (0.1 \times WFPS - a_d)) / \pi$	Parton et al. 1996; del Grosso et al. 2000; Parton et al. 2001
	FASSAT	$f_{(SW\_d)} = \max\left(0, \min\left(1, a_Q + \frac{b_Q}{1 + \exp\left(-\frac{WFPS - c_Q}{d_Q}\right)}\right)\right)$	Chatskikh et al. 2005
	NOE	$f_{(SW\_d)} = \begin{cases} 0 & WFPS < 0.62 \\ ((WFPS - 0.62) / 0.38)^{1.74} & WFPS \geq 0.62 \end{cases}$	Henault et al. 2005

	WNMM	$f_{(SW\_d)} = \exp(-23.77 + 23.77 \times WFPS)$	Li et al. 2007
Soil temperature	APSIM	$f_{(ST\_d)} = 0.1 \times \exp(0.046 \times ST)$	Thorburn et al. 2010; Xing et al. 2011
	DNDC	See Table S3	
	DayCent	NA	Parton et al. 1996; del Grosso et al. 2000; Parton et al. 2001
	FASSAT	$f_{(ST\_d)} = a_u \times \exp(b_u + c_u \times ST \times \left(1 - 0.5 \times \frac{ST}{d_u}\right))$	Chatskikh et al. 2005
	NOE	$f_{(ST\_d)} = \begin{cases} \exp\left((ST - 11) \times \ln(89) - 9 \times \frac{\ln(2.1)}{10}\right) & ST < 11^\circ\text{C} \\ \exp\left((ST - 20) \times \frac{\ln(2.1)}{10}\right) & ST \geq 11^\circ\text{C} \end{cases}$	Henault et al. 2005
	WNMM	$f_{(ST\_d)} = 0.9 \times \left(\frac{ST}{ST + \exp(9.93 - 0.312 \times ST)}\right) + 0.1$	Li et al. 2007
soil pH	APSIM	NA	Thorburn et al. 2010; Xing et al. 2011
	DNDC	See Table S3	
	DayCent	NA	Parton et al. 1996; del Grosso et al. 2000; Parton et al. 2001
	FASSAT	NA	Chatskikh et al. 2005
	NOE	NA	Henault et al. 2005

	WNMM	NA	Li et al. 2007
Soil organic carbon	APSIM	$f_{(C_{OC\_A})} = 0.0031 \times C_{OC\_A} + 24.5$	Thorburn et al. 2010; Xing et al. 2011
	DNDC	See Table S3	
	DayCent	$f_{(CO_2)} = 0.1 \times CO_2^{1.3}$	Parton et al. 1996; del Grosso et al. 2000; Parton et al. 2001
	FASSAT	$R_{P\_d} = (a_d + b_d \times CLAY) \times N_{min}$ $f_{(OC)} = R_{P\_d}$	Chatskikh et al. 2005
	NOE	NA	Henault et al. 2005
	WNMM	$f_{(OC)} = 1.0 - e^{(-1.4 \times C_{OC})}$	Li et al. 2007
NO <sub>3</sub>	APSIM	$f_{(NO_3)} = C_{NO_3}$	Thorburn et al. 2010; Xing et al. 2011
	DNDC	See Table S3	
	DayCent	$f_{(NO_3)} = 1.15 \times C_{NO_3}^{0.57}$	Parton et al. 1996; del Grosso et al. 2000; Parton et al. 2001
	FASSAT	$f_{(NO_3)} = \max(0, \min\left(1, a_N \times \frac{C_{NO_3}}{b_N + C_{NO_3}}\right))$	Chatskikh et al. 2005
	NOE	$f_{(NO_3)} = \frac{C_{NO_3}}{K_{m\_d} + C_{NO_3}}$	Henault et al. 2005
	WNMM	$f_{(NO_3)} = C_{NO_3}$	Li et al. 2007

N <sub>2</sub> O	APSIM	$N2O_d = K_{N2O\_d} \times R_d$ $K_{N2O\_d} = \frac{1}{K_{r\_d} + 1}$ $K_{r\_d} = f_{(NO3/SOC\_N2O\_d)} \times f_{(SW\_N2O\_d)}$ $f_{(NO3/SOC\_N2O\_d)} = \max (0.16 \times k_{d1}, k_{d1} \times \exp(\frac{-0.8 \times C_{NO3}}{CO2}))$ $f_{(SW\_N2O\_d)} = \max (0.1, 1.5 \times WFPS - 0.32)$	Thorburn et al. 2010; Xing et al. 2011
	DNDNC	See Table S3	
	DayCent	$N2O_d = K_{N2O\_d} \times R_d$ $K_{N2O\_d} = \frac{1}{K_{r\_d} + 1}$ $K_{r\_d} = f_{(NO3/SOC\_N2O\_d)} \times f_{(SW\_N2O\_d)}$ $f_{(NO3/SOC\_N2O\_d)} = \max (0.16 \times k_{d1}, k_{d1} \times \exp(\frac{-0.8 \times C_{NO3}}{CO2}))$ $f_{(SW\_N2O\_d)} = \max (0.1, 1.5 \times WFPS - 0.32)$	Parton et al. 1996; del Grosso et al. 2000; Parton et al. 2001
	FASSAT	$N2O_d = K_{N2O\_d} \times R_d$ $K_{N2O\_d} = f_{(SW\_N2O\_d)} \times f_{(ST\_N2O\_d)} \times f_{(NO3\_N2O\_depth)} \times f_{(clay)}$ $f_{(ST\_N2O\_d)} = 1 / (1 + \exp(a_T + b_T \times ST))$ $f_{(SW\_N2O\_d)} = (1.0 - f_{(SW\_a)})$ $f_{(NO3\_N2O\_depth)} = \max (0, \min(1, a_D - b_D \times Depth - c_D \times Depth^2))$ $f_{(clay)} = \max (0, \min(1, a_C \times \exp(b_C \times CLAY) - c_C)))$	Chatskikh et al. 2005
	NOE	$N2O_d = K_{N2O\_d} \times R_d$	Henault et al. 2005
	WNMM	$N2O_d = \begin{cases} 0.05 \times R_d, & WFPS \geq 1.0 \\ a_{den} \times R_d \times (1.0 - f_{(SW\_N2O\_d)}), & WFPS < 1.0 \end{cases}$ $f_{(SW\_N2O\_d)} = \exp(-23.77 + 23.77 \times WFPS)$	Li et al. 2007

**Table S3. Source and equations used to represent denitrification in DNDC.**  
**Abbreviations are given in Table S4.**

Model		Equations	Source
DNDC	The dynamics of dinitrifiers	$U_{NOx} = U_{NOx(max)} \times C_{DOC}/(Kc + C_{DOC}) \times C_{NOx}/(Kn + C_{NOx})$ $U_{dg} = f_{ST\_d} \times (U_{NO3} \times f_{pH1} + U_{NO2} \times f_{pH2} + U_{NO} \times f_{pH2} + U_{N2O} \times f_{pH3})$ $R_{dg} = U_{dg} B_{dg}$ $R_d = M_c \times Y_c \times B_{dg}$ $R_C = (U_{dg}/Y_c + M_c) \times B_{dg}$	Li et al. 2000
	The consumption rates of NO <sub>x</sub>	$R_{NOx} = (\frac{U_{NOx}}{Y_{NOx}} + M_{NOx} \times \frac{C_{NOx}}{C_N})/B_{dg}$	Li et al. 2000
	Soil temperature impact on denitrifiers	$f_{ST\_d} = 2^{((ST-22.5)-10)}$	Li et al. 2000
	pH impact on denitrifiers in each stage	$f_{pH1} = 1.0 - 1.0/(1.0 + \exp(pH - 4.25/0.5))$ $f_{pH2} = 1.0 - 1.0/(1.0 + \exp(pH - 5.25))$ $f_{pH3} = 1.0 - 1.0/(1.0 + \exp(pH - 6.25/1.5))$	Li et al. 2000
	Diffusion rate of N <sub>2</sub> O and NO in the balloon	$D\_NO = (0.0006 + 0.0013 \times f_{clay}) + (0.013 - 0.005 \times f_{clay}) \times PO \times (1.0 - ANVF)$ $D\_N2 = 0.017 + ((0.025 - 0.0013 \times f_{clay}) \times PO \times (1.0 - ANVF))$ $f_{clay} = 2.0 \times CLAY/0.63$	Li et al. 2000

**Table S4.** Nomenclature used in APSIM, DNDC, DayCent, FASSAT, NOE and WNMM.

Terminology	Definitions
R <sub>n</sub>	Actual nitrification rates. The unit varies with models
R <sub>n_Max</sub>	Maximum daily nitrification rate ( $\text{g N ha}^{-1} \text{ day}^{-1}$ ), used in DayCent
R <sub>P_n</sub>	Potential nitrification rates. The unit varies with models
f <sub>n(NH4)</sub>	Effects of $\text{NH}_4^+$ concentration on nitrification
f <sub>n(SW)</sub>	Rate modifiers for the effect of soil moisture on nitrification
f <sub>n(ST)</sub>	Rate modifiers for the effect of soil temperature on nitrification
f <sub>n(pH)</sub>	Rate modifiers for the effect of soil pH conditions on nitrification
N <sub>2</sub> O <sub>n</sub>	$\text{N}_2\text{O}$ flux produced from nitrification
K <sub>N2O_n</sub>	Actual fraction of nitrified N lost as $\text{N}_2\text{O}$ flux
K <sub>I</sub>	Potential fraction of nitrified N lost as $\text{N}_2\text{O}$ flux
K <sub>max</sub>	Maximum fraction of $\text{NH}_4^+$ nitrified ( $0.10 \text{ d}^{-1}$ )
K <sub>m</sub>	$\text{NH}_4^+$ concentration that produces a rate of $1/2 V_{max}$ , which is the maximum nitrification rate at the optimum $\text{NH}_4^+$ concentration
f <sub>(SW_N2O_n)</sub>	Modifiers for the effects of soil moisture on K <sub>I</sub>
f <sub>(ST_N2O_n)</sub>	Modifiers for the effects of soil temperature on K <sub>I</sub>
B <sub>n</sub>	Biomass of nitrifiers ( $\text{kg C ha}^{-1}$ )
C <sub>NH4</sub>	$\text{NH}_4^+$ concentration
pH	Soil pH
ST	Soil temperature
SW	soil volumetric water content
SWg	soil gravimetric water content
FC	Soil water content at field capacity
PO	Soil porosity
WP	Soil water content at plant wilting point

SW25	Soil water content at WP + 0.25×(FC-WP)
$\varphi$	Soil water potential (m H <sub>2</sub> O)
N <sub>min</sub>	Daily net N mineralization rate
WFPS	Water Filled Pore Space
DUL	Soil water content at drained upper limit
SAT	Soil water content at saturation
LL	Soil water content at lower limit, assumed to be equivalent to water content at 15 bars in APSIM
WFD	Internal parameter used in APSIM
R <sub>d</sub>	Actual rates of denitrification. The unit varies with models
R <sub>P_d</sub>	Potential rates of denitrification. The unit varies with models
f <sub>(NO<sub>3</sub>)</sub>	Dimensionless modifiers for the effect of NO <sub>3</sub> <sup>-</sup> on denitrification
f <sub>(OC)</sub>	Dimensionless modifiers for the effect of soil organic carbon on denitrification
f <sub>(C<sub>OC_A</sub>)</sub>	Dimensionless modifiers for the effect of soil active soil organic carbon on denitrification, used in APSIM
f <sub>(CO<sub>2</sub>)</sub>	Dimensionless modifiers for the effect of soil heterotrophic CO <sub>2</sub> respiration on denitrification, used in DayCent
f <sub>(SW_d)</sub>	Dimensionless modifiers for the effect of soil moisture on denitrification
f <sub>(ST_d)</sub>	Dimensionless modifiers for the effect of soil temperature on denitrification
f <sub>(pH_d)</sub>	Dimensionless modifiers for the effect of soil pH on denitrification
C <sub>oc</sub>	Percent content of the soil organic carbon (%)
C <sub>SOC</sub>	Concentration of soil organic carbon (kg C ha <sup>-1</sup> )
C <sub>OC_A</sub>	Active soil organic carbon, estimated by Humus and fresh organic carbon pools. This is used in APSIM
C <sub>DOC</sub>	Concentration of dissolved organic carbon (kg C/ha)
C <sub>NO<sub>3</sub></sub>	NO <sub>3</sub> <sup>-</sup> concentration
K <sub>m_d</sub>	NO <sub>3</sub> <sup>-</sup> concentration that produces a rate of 1/2 V <sub>max</sub> , which is the maximum nitrification rate at the optimum NO <sub>3</sub> <sup>-</sup> concentration
K <sub>N<sub>2</sub>O_d</sub>	Potential fraction of N <sub>2</sub> O emitted from denitrification to daily denitrification rate
N <sub>2</sub> O <sub>d</sub>	N <sub>2</sub> O flux produced from denitrification (kg N ha <sup>-1</sup> day <sup>-1</sup> )

$K_{r_d}$	Ratio of $N_2/N_2O$ emitted during denitrification
$CO_2$	Heterotrophic $CO_2$ respiration
$f_{(NO3\_N2O\_d)}$	Modifiers for the effect of $NO_3^-$ concentration on $K_2$
$f_{(SOC\_N2O\_d)}$	Modifiers for the effect of soil organic carbon on $K_2$
$f_{(SW\_N2O\_d)}$	Modifiers for the effect of soil moisture on $K_2$
$f_{(ST\_N2O\_d)}$	Modifiers for the effect of soil temperature on $K_2$
$f_{(ST\_N2O\_dwpt)}$	Modifiers for the effect of soil depth on $K_2$
$f_{(clay)}$	Modifiers for the effect of soil clay content on $K_2$
$f_{(NO3/SOC\_N2O\_d)}$	Modifiers for the interaction effect of $NO_3^-$ concentration and heterotrophic $CO_2$ respiration on $K_2$
CLAY	Soil clay content (%)
Depth	Soil depth (cm)
$k_{d1}$	Parameter is related to gas diffusivity in soil at field capacity
$U_{NO3(max)}$	Maximum growth rate of nitrogen oxides denitrifier
$K_c$	Half-saturation value of soluble carbon
$K_n$	Half-saturation value of N-oxide
$M_c$	Maintenance coefficient on C
$Y_c$	Maximum growth rate of soluble C
$C_N$	Concentration of $NO_3^-$ , $NO_2^-$ , NO and $N_2O$ ( $kg\ N/m^3$ )
$C_{NOx}$	Concentration of all $NO_x$ ( $kg\ N/m^3$ )
$f_{pH1}$	pH factors for $NO_3^-$ denitrifiers
$f_{pH2}$	pH factors for $NO_2^-$ and NO denitrifiers
$f_{pH3}$	pH factors for $N_2O$ denitrifiers
$B_{dg}$	Denitrifiers biomass ( $kg\ C/ha$ )
$U_{NOx}$	Relative growth rate of $NO_x$ denitrifiers
$U_{dg}$	Relative growth rate of total denitrifiers
$R_{dg}$	Growth rate of total denitrifiers
$R_d$	Death rate of total denitrifiers

$R_c$	Carbon consumption rate
$R_{NOx}$	Consumption rates of $NO_x$
$M_{NOx}$	Maintenance coefficient on N oxides
$Y_{NOx}$	Maximum growth rate on N oxides ( $NO_3^-$ , $NO_2^-$ , NO and $N_2O$ )
$D_{NO}$	Gas diffusion to NO and $N_2O$
$D_{N2}$	Gas diffusion rate of $N_2O$ and NO
ANVF	Volumetric fraction of anaerobic microsites
a, b, c, d and $a_d$	Inner parameters used in DayCent
$A_{nitr}$ , $B_{nitr}$ , $C_{nitr}$	Inner parameters used in DayCent for estimating soil temperature impact on daily nitrification rate, which vary with the optimal soil temperature for nitrification (site specific parameter)
$a_h$ , $a_Q$ , $b_Q$ , $c_Q$ , $d_Q$ , $a_u$ , $b_u$ , $c_u$ , $d_u$ , $a_d$ , $b_d$ , $a_N$ , $b_N$ , $a_C$ , $b_C$ , and $c_C$	Inner parameters used in FASSAT
$A_{max}$	Maximum death rate of nitrifiers
$U_{max}$	Maximum growth rate of nitrifiers
$a_{den}$	Maximum fraction of $N_2O$ emission in total denitrification that is at 0.8 of WFPS (0–1)