

Supplementary material

**Dealing with propositions, not with the characters: the ability of three-taxon statement analysis to recognise groups based solely on ‘reversals’, under the maximum-likelihood criteria**

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**Table S1. Summary of the results of maximum-parsimony (MP) analyses of 18 binary matrices from Nelson and Platnick (1991)**

Consistency Index (CI), Retention index (RI) (reviewed in Kitching *et al.* 1998)

| Matrix | MP (PAUP*): topology, uniform weighting | Number of steps     | CI                        | RI                        |
|--------|-----------------------------------------|---------------------|---------------------------|---------------------------|
| 1      | (O(A(B(CD))))                           | 9                   | 0.667                     | 0.5                       |
|        | (O((AB)(CD)))                           | 9                   | 0.667                     | 0.5                       |
| 2      | (O(A(B(CD))))                           | 51 <sup>A</sup> /18 | 0.705 <sup>A</sup> /0.722 | 0.583 <sup>A</sup> /0.615 |
| 3      | (O(B(A(DC))))                           | 9                   | 0.667                     | 0.5                       |
|        | (O(A(B(DC))))                           | 9                   | 0.667                     | 0.5                       |
|        | (O((AB)(DC)))                           | 9                   | 0.667                     | 0.5                       |
| 4      | (O(B(A(DC))))                           | 19                  | 0.737                     | 0.643                     |
| 5      | (O(AE(B(CD))))                          | 8                   | 0.625                     | 0.5                       |
|        | (O(AE(C(BD))))                          | 8                   | 0.625                     | 0.5                       |
| 6      | (O(E(A(C(BD))))))                       | 24                  | 0.75                      | 0.667                     |
|        | (O(E(A(B(CD))))))                       | 24                  | 0.75                      | 0.667                     |
|        | (O(A(E(C(BD))))))                       | 24                  | 0.75                      | 0.667                     |
|        | (O(A(E(B(CD))))))                       | 24                  | 0.75                      | 0.667                     |
| 8      | (O((H(AB))(C(E(G(DF))))))               | 39                  | 0.615                     | 0.68                      |
|        | (O((H(AB))(C(E(F(DG))))))               | 39                  | 0.615                     | 0.68                      |
|        | (O((H(AB))(C(E(D(FG))))))               | 39                  | 0.615                     | 0.68                      |
| 9      | (O((H(AB))(C(E(G(DF))))))               | 385 <sup>B</sup>    | 0.735                     | 0.639                     |
| 11     | (O(A(D(CB))))                           | 7                   | 0.714                     | 0.6                       |
| 12     | (O(D(A(BC))))                           | 15                  | 0.733                     | 0.636                     |
|        | (O(A(D(BC))))                           |                     |                           |                           |
| 13     | (O(A(D(BC))))                           | 9                   | 0.667                     | 0.5                       |
| 14     | (O(D(A(BC))))                           | 18                  | 0.722                     | 0.615                     |
| 15     | (O(A(B(C(D(E(FG))))))                   | 8                   | 0.875                     | 0.889                     |
| 16     | (O((E(FG))(A(B(CD))))                   | 26                  | 0.923                     | 0.916                     |
| 17     | (O(A(B(C(D(EF))))                       | 6                   | 0.833                     | 0.875                     |
| 18     | (O(A(B(C(D(EF))))                       | 50                  | 0.88                      | 0.863                     |
|        | (O(A(B((CD)(EF))))                      | 50                  | 0.88                      | 0.863                     |
| 19     | (O((AF)((DE)(BC))))                     | 22                  | 0.636                     | 0.467                     |
| 20     | (O((F(DE))(A(CB))))                     | 84                  | 0.761                     | 0.687                     |

<sup>A</sup>If weights of three-taxon statements (3TSs) assigned as proposed by Nelson and Platnick (1991).

<sup>B</sup>386 steps in Nelson and Platnick (1991, p. 358).

**Table S2. Summary of the results of maximum-likelihood (ML) analyses of the fractionally weighted three-taxon statement (3TS) representations of the selected matrices from Kluge (1994), Farris (1997), Farris and Kluge (1998) and Nelson and Platnick (1991)**

| Source of the 3TS representation                                | Most probable ML-3TS topology (PAUP*, Mk, FW)                          | -log likelihood | Number of 3TSs |
|-----------------------------------------------------------------|------------------------------------------------------------------------|-----------------|----------------|
| Table 2 from Kluge (1994)                                       | (X(A(B(C(D(E(FGH(I(JK))))))))))<br>(X(A(B(C(D(E((FGH(I(JK))))))))))    | 412.23921       | 708            |
| Table 3 from Kluge (1994)                                       | (X(A(B(C(D(E(FG)))))))                                                 | 98.27079        | 90             |
| Matrix Z from Farris (1997)                                     | (O((A(B(C(D(E(FG)))))))(H(I(J(K(L(MN)))))))                            | 758.78826       | 810            |
| Figure 5 from Farris and Kluge (1997)                           | (O(A(B(C(D(E(F(G(H(I(J(K(L(M(N(P(Q(R(S(T(U(V(W(X(YZ))))))))))))))<br>) | 5582.0033       | 17 720         |
| Modified matrix 17 from Nelson and Platnick (1991) <sup>A</sup> | (O(A(B(C(D(EF))))))                                                    | 42.60620        | 40             |

<sup>A</sup>Character four excluded (see also Fig. 1 in the main paper).

## References

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