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Corrigendum to: Circular Flip-Flop Index: quantifying revision stability of forecasts of direction

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This corrigendum corrects Journal of *Southern Hemisphere Earth Systems Science* **71**(3) 266–271. doi:10.1071/ES21010

The authors of the above-mentioned paper regret to inform readers that the two values of 30 in the bottom row in Table 1 were incorrect in the published version of this paper. Those values should instead be 16. This is corrected below (highlighted cells):

Table 1. Forecast sequences for wind direction and corresponding Circular Flip-Flop Index calculations. Forecast f_i was issued i days prior to the validity period of the forecast.

	Official forecasts for Melbourne Airport valid 0000 UTC 27 December 2020	Synthetic Example 1	Synthetic Example 2	Synthetic Example 3	Synthetic Example 4
Direction (°)					
f ₇	9	50	340	360	360
f ₆	341	80	10	40	80
f ₅	354	70	360	80	360
f ₄	353	120	50	120	240
f ₃	5	110	40	160	320
f ₂	1	100	30	200	80
f ₁	359	60	350	240	360
$\sum_{i} \sum_{i} (\circ)$					
$f_i \text{ in } \{f_5, f_6, f_7\}$	28	30	30	80	80
$f_i \text{ in } \{f_1, f_2, f_3\}$	6	50	50	80	80
f_i in { f_1 , f_2 , f_3 , f_4 , f_5 , f_6 , f_7 }	28	70	70	240	200
Circular Flip-Flop Index (°)					
For sequence f_5 , f_6 , f_7	13	10	10	0	80
For sequence f_1 , f_2 , f_3	0	0	0	0	80
For sequence <i>f</i> ₁ , <i>f</i> ₂ , <i>f</i> ₃ , <i>f</i> ₄ , <i>f</i> ₅ , <i>f</i> ₆ , <i>f</i> ₇	6.4	16	16	12	76

Thank you to Philip Gill and Clare Bysouth from The Met Office for alerting us to the error.

We apologise for these errors and any confusion their inclusion may have caused.

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Circular Flip-Flop Index: quantifying revision stability of forecasts of direction

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ABSTRACT

The Flip-Flop Index, designed to quantify the extent to which a forecast changes from one issue time to the next, is extended to a Circular Flip-Flop Index for use with forecasts of wind direction, swell direction or similar. The index was devised so we could understand the degree of stability in wind direction forecasts. The Circular Flip Flop Index is independent of observations, has a relatively simple definition and does not penalise a sequence of forecasts that show a trend as long as the forecasts stay within a 180° sector. The Circular Flip-Flop Index is interpreted in terms of the impact of changing forecasts on decisions made by users of the forecast. The Circular Flip-Flop Index has been used to compare the stability of sequences of automated forecast guidance to the official Australian Bureau of Meteorology forecasts, which are prepared manually. It is the first objective assessment of the stability of forecast guidance, itself a consensus of many numerical weather models, are more stable than the official, manual forecasts. The Circular Flip-Flop Index does not measure skill but can play a complementary role in characterising and evaluating a forecasting system.

Keywords: flip-flop, forecast assessment, forecast convergence, forecast oscillations, forecast stability, forecast volatility, wind verification.

I Introduction

The extent and frequency of changes as a forecast is revised, from one issue time to the next, is an aspect of a forecast system that interests forecasters and users. Too much stability may signify issues with the forecast process as may too little stability. This is discussed in Griffiths *et al.* (2019).

There have been several indices developed to measure forecast stability, each tailored to a specific use and almost all relating to a scalar quantity. For example, see Ruth *et al.* (2009), Zsoter *et al.* (2009), Ehret (2010), Griffiths *et al.* (2019). No-one has tackled a vector quantity, such as wind, or a circular quantity, such as wind direction, although Fowler *et al.* (2015) tackled the complex question of forecast revisions of tropical cyclone tracks.

We provide an analogous index to the Flip-Flop Index of Griffiths *et al.* (2019) to extend it to be suitable for a circular quantity, such as wind direction. We provide examples to illustrate the Circular Flip-Flop Index and interpret the index in terms of threshold-based decisions of users of the forecast.

The convention used is that wind direction is the direction from which the wind blows, and is measured clockwise from true north. A forecast wind direction of 360° refers to a wind blowing from north to south, referred to as a northerly wind. Similarly, a wind direction of 180° refers to a southerly wind, blowing from south to north.

2 The Circular Flip-Flop Index

Consider sequences of successive forecasts, or forecast revisions, labelled as $f_1, f_2, ..., f_n$. Each forecast f_i is for the same quantity or event, including the same validity time, but is

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issued at a different time. The forecasts would usually be issued at regular intervals with each subscript representing a different lead time, the time between the forecast being issued and the validity time.

For example, the forecast f_7 may be an initial forecast for the chance of rain, or maximum wind speed, on a particular day of interest, issued a week beforehand. A new forecast may be issued each day with f_1 the forecast issued the day before the day of interest. In this case the subscripts represent the lead time in days.

For a scalar forecast, the Flip-Flop Index, as per Griffiths *et al.* (2019), is defined as

Flip-Flop Index =
$$\frac{1}{n-2} \left\{ \sum_{i=1}^{n-1} |f_i - f_{i+1}| - \left(\max_i f_i - \min_i f_i \right) \right\}.$$
 (1)

For forecasts of wind direction between 0° and 180° , for example, the Flip-Flop Index formula can be used. However, as the directions become more widely varying, possibly rotating around the whole dial, we cannot ignore the circular nature of the forecast parameter and we need to modify the definition.

Let $f_1, f_2, ..., f_n$ be a revision sequence of forecasts in degrees. Define

Circular Flip-Flop Index =
$$\frac{1}{n-2} \left\{ \sum_{i=1}^{n-1} |\operatorname{Sector}(f_i, f_{i+1})| - \min\left(\left| \operatorname{Sector}(f_i) \right|, 180^\circ \right) \right\}$$
(2)

where $\left| \underset{i}{\operatorname{Sector}}(f_i) \right|$ is the size of the smallest sector in

degrees containing all directions f_i , and $|\text{Sector } (f_i, f_j)|$ is the size of the smallest sector in degrees containing the two directions f_i and f_j .

Table 1 shows some forecast sequences and their calculated Circular Flip-Flop Index. Synthetic Examples 1 and 2 are simple rotations of each other. That they have the same Circular Flip-Flop Index is an essential property of any index used to measure stability. As desired, the Circular Flip-Flop Index of Synthetic Example 1 equals the Flip-Flop Index of the same example when interpreted as a scalar forecast.

Table I. Forecast sequences for wind direction and corresponding Circular Flip-Flop Index calculations. Forecast f_i was issued *i* days prior to the validity period of the forecast.

	Official forecasts for Melbourne Airport valid 0000 UTC 27 December 2020	Synthetic Example I	Synthetic Example 2	Synthetic Example 3	Synthetic Example 4
Direction (°)					
f7	9	50	340	360	360
f6	341	80	10	40	80
fs	354	70	360	80	360
f4	353	120	50	120	240
f3	5	110	40	160	320
f2	I.	100	30	200	80
fi	359	60	350	240	360
$\operatorname{Sector}_{i}(f_{i}) (^{\circ})$					
f_i in { f_5 , f_6 , f_7 }	28	30	30	80	80
f_i in $\{f_1, f_2, f_3\}$	6	50	50	80	80
f; in {f1, f2, f3, f4, f5, f6, f7}	28	70	70	240	200
Circular Flip-Flop Index (°)					
For sequence f_5 , f_6 , f_7	13	10	10	0	80
For sequence f_1 , f_2 , f_3	0	0	0	0	80
For sequence <i>f</i> ₁ , <i>f</i> ₂ , <i>f</i> ₃ , <i>f</i> ₄ , <i>f</i> ₅ , <i>f</i> ₆ , <i>f</i> ₇	6.4	30	30	12	76

3 Practical interpretation with examples

The Flip-Flop Index can be interpreted in terms of a simple user decision model with a user making one decision when the forecast exceeds a user-defined threshold and changing that decision if a revised forecast is at or below the same threshold. For example, you may plan a picnic if the chance of rain is less than 40% but change your plan to a trip to the museum if the chance of rain is at least 40%. In this case, your user-defined threshold is 40%. When analysing forecast sequences of length 3, the Flip-Flop Index measures the range of thresholds for which users with those decision thresholds will change their mind twice based on the forecast. More generally, the Flip-Flop Index is a measure of the number of times a forecast threshold is crossed (beyond the first time), integrated over all forecast thresholds and normalised according to the length of the forecast revision sequence. For further details, see Griffiths et al. (2019).

We give a similar interpretation of the Circular Flip-Flop Index, interpreting the decision threshold in a way appropriate to directions.

A pilot, Barb, wants to take-off into the wind along a north–south runway. Her decision regarding which end of the runway to start at is informed by whether the wind has a southerly component or a northerly component. That is, her decision is based on directions being within the 180° arc from 90° through southerly to 270° or in the complementary 180° arc from 270° through northerly to 90°. We can think of her decision threshold being 90° and 270°, which are congruent mod 180°. If a forecast revision crosses either 90° or 270°, changing from having a northerly to a southerly component (or *vice versa*) she will revise her decision. This is illustrated in Fig. 1.

Consider the Synthetic Example 1 in Table 1 of forecasts of wind direction (f_7 , f_6 , f_5 , f_4 , f_3 , f_2 , $f_1 = 50^\circ$, 80° , 70° , 120° , 110° , 100° , 60°) all lying within a 70° sector. Applying this sequence of generally easterly wind forecasts to Barb's decision, her decision threshold is 90° . For the forecasts of wind from 50° , 80° and 70° , Barb plans to take-off from the south. For the forecasts of 120° , 110° and 100° , she plans to take-off from the north. However, with a final forecast revision from 100° to 60° , she reverts to her initial plan.



Fig. 1. A forecast direction of f_3 is revised to f_2 , then f_1 . The solid grey arc indicates forecast decision thresholds (direction of dividing lines) that experience a flip-flop. The horizontal (east-west) line is one decision threshold within the sector. The dashed arc indicates the first term of the index: the sum of the successive forecast differences.

She has changed her plans twice, and experienced a single Flip-Flop.

Consider a nearby runway that is only approximately aligned north–south and has a decision threshold of 75° (or equivalently, 255°). For the same forecast sequence Synthetic Example 1 in Table 1, a pilot would have changed their plans four times.

A similar example might be someone wanting to picnic on the sheltered side of an east–west aligned (north–south facing) wall. Again, their decision will be based on whether the wind has a northerly component or a southerly component, and the decision threshold will be 90° (or equivalently, 270°).

The Synthetic Example 2 in Table 1 is a simple rotation of Synthetic Example 1. In this case it is people with a decision threshold between north and north-east that will change their plans at least once. For both Synthetic Examples 1 and 2, the thresholds that will experience at least one change in plans are those within a 70° sector, being from 50° to 120° (or equivalently, 230° to 300°) for Example 1, and being from 340° to 50° (or equivalently, 160° to 230°) for Example 2.

Note that the most extreme change for a directional forecast is 180°. Forecasts that change by 180° will cause all pilots or picnickers to change their plans regardless of the alignment of their runway or sheltering wall (ignoring the edge case of a runway or wall aligned due east-west).

As with the Flip-Flop Index, when used with a forecast sequence of length 3, the Circular Flip-Flop Index measures the range of thresholds for which users with those decision thresholds will change their mind twice based on the forecast.

In looking at the terms of the Flip-Flop Index (Eqn 1) and Circular Flip-Flop Index (Eqn 2), in Eqn 1 we have $|f_i - f_{i+1}|$, the difference between successive forecasts, which is replaced in Eqn 2 by $|\text{Sector}(f_i, f_i)|$, which is also the difference between successive forecasts. In both indices, summing the difference between successive forecasts gives a measure of the number of times a forecast threshold is crossed, integrated over all forecast thresholds. In Eqn 1 we subtract $max f_i - min f_i$, the magnitude of the smallest interval containing all forecasts, which is replaced in Eqn 2 by the magnitude of the smallest sector containing all forecasts limited by 180°. In both cases, this second term is the range of thresholds crossed at least once by forecast revisions. So, as for the Flip-Flop Index, the Circular Flip-Flop Index can be described as a measure of the number of times a forecast threshold is crossed (beyond the first time), integrated over all forecast thresholds and normalised according to the length of the forecast revision sequence.

The maximum value of the Circular Flip-Flop Index is 180°. The maximum value of the Flip-Flop Index is the range of possible forecast values, which will be 100% for probability forecasts and will typically be less than 100°C for forecasts of temperature.

We now consider Synthetic Example 3 from Table 1 (f_7 , f_6 , f_5 , f_4 , f_3 , f_2 , $f_1 = 360^\circ$, 40° , 80° , 120° , 160° , 200° , 240°).

The forecast revisions are all gradual and uniform, with each forecast 40° more clockwise than the previous. We note that a user with a decision threshold of 10° (equivalently 190°) changes their decision between f_7 and f_6 and again between f_3 and f_2 . Indeed, all users with decision thresholds between 360° and 60° experience two changes of decision (a flipflop). Users with decision thresholds between 60° and 180° change their decision once, but do not experience a flip-flop.

Checking the formula of the Circular Flip-Flop Index, we find the smallest sector containing all forecasts is 240°, so

Sector(f_i), 180° = 180°. That is, all users will min

change their decision at least once. The Circular Flip-Flop Index equals

$$\frac{1}{7-2} \{ (40^\circ + 40^\circ + 40^\circ + 40^\circ + 40^\circ + 40^\circ) - 180^\circ \}$$

= 12°.

This contrasts to the Circular Flip-Flop Index calculated for any three consecutive forecasts in Example 3, which is

$$\frac{1}{3-2}\{(40^{\circ} + 40^{\circ}) - 80^{\circ}\} = 0^{\circ}$$

Finally, consider Synthetic Example 4 from Table 1 (f_7 , f_6 , $f_5, f_4, f_3, f_2, f_1 = 360^\circ, 80^\circ, 360^\circ, 240^\circ, 320^\circ, 80^\circ, 360^\circ).$ Inspection shows that the forecast is much less stable than Example 3 and this is confirmed by the Circular Flip-Flop Index. The smallest sector containing all directions f_i is 200°, so min ||Sector(f_i)|, 180°| = 180°. The Circular Flip-Flop

Index equals

$$\frac{1}{7-2} \{ (80^\circ + 80^\circ + 120^\circ + 80^\circ + 120^\circ + 80^\circ) - 180^\circ \} = 76^\circ.$$

In Synthetic Example 4, users with decision thresholds between 0° and 60° (equivalently, between 180° and 240°) change their decision four times, experiencing three flipflops. Users with the decision thresholds of 60° to 80° (equivalently, 240° to 260°) change their decision six times, experiencing five flip-flops. Users with the decision thresholds of 80° to 180° (equivalently, 260° to 360°) change their decision twice, experiencing a single flip-flop. Integrating the number of flip-flops experienced across the different thresholds we get $3 \times 60^{\circ} + 5 \times 20^{\circ} + 1 \times 100^{\circ} = 380^{\circ}$ which is divided by n - 2 = 5 to get the Circular Flip-Flop Index.

The example of actual forecasts in Table 1 for Melbourne Airport on 27 December 2020 is typical of most wind forecasts, which display little flip-flopping, especially as the lead days get shorter. In this example, using real forecasts, the Circular Flip-Flop Index for lead days 7-5 is 13°, but for lead

days 3–1 it is 0°. For the revision sequence of length seven, the Circular Flip-Flop Index is only 6.4°.

4 Application to forecasts of wind direction

In this section we give examples of using the Circular Flip-Flop Index to analyse and compare properties of some real forecasts of wind direction. We present data from forecasts of wind at forecast sites coinciding with automatic weather stations in Australia valid for each of the 24 hours of each day for 3 months. These were updated daily, giving for each f_4, f_3, f_2, f_1) where the subscripts represent the lead time in days, i.e. the number of days before the validity time of the forecast. We had Operational Consensus Forecasts (OCF) and Official forecasts. OCF are a bias corrected blend of Numerical Weather Prediction (NWP) outputs (Bureau of Meteorology 2014). The Official forecasts are as issued by the Bureau of Meteorology. They are often based on a blend of NWP, but the on-duty meteorologists make a judgement call as to which NWP to use and may manually enhance sea breezes, sharpen fronts or otherwise modify the NWP guidance.

When dealing with wind, the direction has no meaning if the forecast wind is calm. In our assessment of forecast stability, we excluded wind direction forecasts when the forecast wind speed was less than 0.05 m/s. If, for example, f_4 was excluded due to a forecast wind speed of less than 0.05 m/s, or was missing for some other reason such as a technical fault, then we did not calculate the Circular Flip-Flop Index for any forecast revision sequences that included f_{4} .

To present our results, we calculated the Circular Flip-Flop Index for all available forecast revision sequences $(f_7, f_6, f_5, f_4, f_3, f_2, f_1), (f_7, f_6, f_5), (f_5, f_4, f_3) \text{ and } (f_3, f_2, f_1).$ For each of these we, summarised the results over 450 forecast locations and 2200 validity times. We plotted the frequency with which the Circular Flip-Flop Index exceeded values of 5, 10, 15, 20, etc. as shown in Figs 2, 3.

By plotting the Circular Flip-Flop Index of forecasts of wind direction and the Flip-Flop Index of forecasts of wind speed, we have been able to track changes in forecast stability from year to year and compare forecast stability of different forecast systems. We have been able to compare forecast stability in winter compared to summer and in the mid-latitudes compared to the tropics. We have been able to quantify the stability at shorter lead times compared to longer lead times. Some of these results are shown here.

Reading one value from the graph in Fig. 2 we see that for winter 2020 in southern Australia, the Circular Flip-Flop Index was at least 30° just 9% of the time when considering forecast revisions from lead days 7-5. Interestingly, the forecasts from lead days 5-3 were almost as stable as those for lead days 3-1, with the Circular Flip-Index being at least 30° only 3% of the time for each. Fig. 4 shows the forecast sites included in these results.

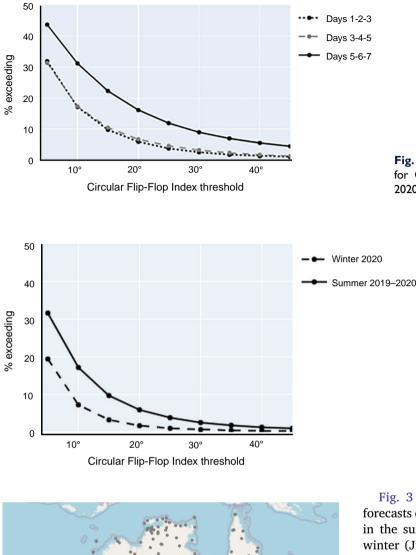


Fig. 2. Frequency of exceedance of Flip-Flop Index thresholds for Official forecasts of wind direction for June-July-August 2020. The results are from about 200 sites in southern Australia.

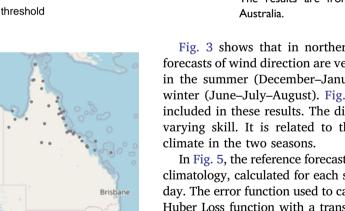




Fig. 4. The southern Australia sites relevant to the results of Figs 2, 5 are shown with black dots. The northern Australia sites relevant to the results of Fig. 3 are shown with grey dots.

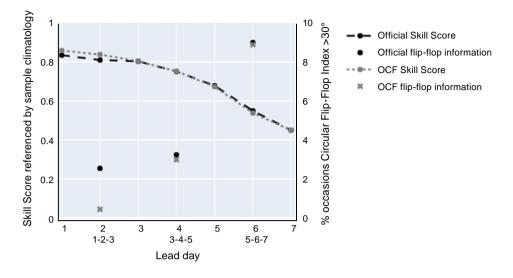
for official forecasts of wind direction from lead days 3-1, comparing winter 2020 to the previous summer. The results are from about 85 sites in northern

Fig. 3. Frequency of exceedance of Flip-Flop Index

Fig. 3 shows that in northern Australia the short-term forecasts of wind direction are very stable, but flip-flop more in the summer (December-January-February) than in the winter (June-July-August). Fig. 4 shows the forecast sites included in these results. The difference does not represent varying skill. It is related to the relative stability of the

In Fig. 5, the reference forecast for the Skill Score is sample climatology, calculated for each station and each hour of the day. The error function used to calculate the Skill Score is the Huber Loss function with a transition point from squared to linear penalties at 90° (Huber 1964). The choice of Huber loss, rather than squared error, was made due to not using quality controlled observations and wanting to limit the extent of the impact of large errors. A Skill Score of 1 represents a perfect forecast. The Circular Flip-Flop Index has been calculated for revision sequences of length 3, with the lead days indicated by the lower values labelling the horizontal axis.

Fig. 5 shows that the skill and stability of OCF and the Official forecasts in winter 2020 for southern Australia were very similar for lead days 3-7. However, at the shorter lead days, OCF had a slightly higher skill than the Official forecast and greater stability. The Circular Flip-Flop Index for the forecast revisions for lead days 3-1 only exceeded 30°



2.5% of the time for the Official forecasts but even less frequently (0.5% of the time) for the OCF.

5 Discussion and conclusion

The Circular Flip-Flop Index extends the Flip-Flop Index, providing a way to characterise the revision stability of forecasts of direction. This allowed us to make quantitative comparisons between different forecast systems, and for one system, to quantify differences between regions and seasons. It shares the desirable characteristic of the Flip-Flop Index of distinguishing between large and small flip-flops and being insensitive to small perturbations within the revision sequence. The Flip-Flop Index has not been extended to vector forecasts. That is, we have a way to examine the stability of forecasts of magnitude and direction separately, but not together.

Quantifying stability using the Circular Flip-Flop Index, combined with measures of forecast skill, has supported the Bureau of Meteorology in its choice to increasingly rely on consensus forecast guidance.

We recognise that both the Flip-Flop Index and the Circular Flip-Flop Index provide a very generic assessment **Fig. 5.** Results for forecasts of wind direction for southern Australia from winter 2020. The left hand axis and the data connected by lines shows the Skill Score of Official forecasts and OCF. The right hand axis and points show the percentage of occasions that the Flip-Flop Index exceeds 30°. See the text for further details.

of forecasts with very simplistic assumptions about users' decision models. In practice many users will make a decision based on a combination of magnitude and direction, or may be interested in a specific directional sector less than 180°, and may want to create a Flip-Flop Index tailored to their specific decision structure.

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Data availability. The data that support this study will be shared upon reasonable request to the corresponding author.

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