## Supplementary Material

## Synthesis of heteroleptic yttrium and dysprosium 1,2,4-tris (trimethylsilyl)cyclopentadienyl complexes

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Synthesis of heteroleptic yttrium and dysprosium 1,2,4-tris(trimethylsilyl)cyclopentadienylcomplexesSophie C. Corner, ${ }^{1 \dagger}$ Conrad A. P. Goodwin, ${ }^{1 \dagger}$ Fabrizio Ortu, ${ }^{1 \dagger}$ Peter Evans, ${ }^{1}$ Hongrui Zhang, ${ }^{1}$ Gemma K.Gransbury, ${ }^{1}$ George F. S. Whitehead, ${ }^{1}$ and David P. Mills* ${ }^{1}$${ }^{1}$ Department of Chemistry, The University of Manchester, Oxford Road, Manchester, M13 9PL, U.K.
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## 1. Synthetic procedure for $\left[\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right]$

[ $\left.\mathbf{N E t}_{3} \mathbf{H}\right][\mathbf{B P h} 4]$. In air, $\mathrm{NaBPh}_{4}(25.000 \mathrm{~g}, 73.1 \mathrm{mmol})$ was added to a single-neck 1 L round bottomed flask. The solid was dissolved in deionised water $(400 \mathrm{~mL})$ at room temperature, and then cooled to $0^{\circ} \mathrm{C}$ in an ice bath. With vigorous stirring, $\mathrm{Et}_{3} \mathrm{~N} \cdot \mathrm{HCl}(10.055 \mathrm{~g}, 73.1 \mathrm{mmol})$ was added in a single portion, which resulted in the rapid precipitation of a white solid and the vessel became very slightly warm. Stirring and manual agitation were continued for 1 hour, then the mixture was filtered through a medium porosity fritted funnel and the solids collected. The white solids were washed with deionised water ( 100 mL ), followed by hot deionised water $\left(2 \times 200 \mathrm{~mL}\right.$ at $\left.70^{\circ} \mathrm{C}\right)$, and finally with $\mathrm{Et}_{2} \mathrm{O}(2 \times 100 \mathrm{~mL})$. The flowing white powder was then transferred to a Schlenk and dried in vacuo at room temperature for 12 hours to give anhydrous [ $\left.\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right]$ as a white solid. Yield: $29.420 \mathrm{~g}, 96 \%$. Recrystallization of a small portion of the solid from THF at $5^{\circ} \mathrm{C}$ gave crystals of $\left[\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right] \cdot \mathrm{THF}$ as large colourless blocks.

Data for $\left[\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right]: v_{\max }(\mathrm{Nujol}) / \mathrm{cm}^{-1} 3132(\mathrm{~m}, \mathrm{~N}-\mathrm{H}$ stretch), 3054 (m, C-H stretch arom.), 2984 (m, C-H stretch aliph.), 1580 (w, C-C stretch arom.), 1474 (m) 1424 (m), 1385 (m), 1264 (w), 1161 (m), 1065 (m), 1030 (m), 1011 (m), 863 (w), 839 (m), 808 (w), 773 (w), 738 (s), 703 (s), 604 (s), 460 (m), 432 (w). $\delta_{\mathrm{H}}\left(d_{6}\right.$-DMSO) $7.18(\mathrm{br} \mathrm{m}, 8 \mathrm{H}, m-\mathrm{C} H), 6.98\left(\mathrm{t},{ }^{3} J_{\mathrm{HH}}=7.4 \mathrm{~Hz}, 8 \mathrm{H}, o-\mathrm{CH}\right), 6.80\left(\mathrm{t},{ }^{3} J_{\mathrm{HH}}=7.1 \mathrm{~Hz}, 4 \mathrm{H}, p-\right.$ $\mathrm{CH}), 3.05\left(\mathrm{q},{ }^{3} \mathrm{~J}_{\mathrm{HH}}=7.3 \mathrm{~Hz}, 6 \mathrm{H}, \mathrm{N}\left(\mathrm{CH}_{2} \mathrm{CH}_{3}\right)_{3}\right), 1.15\left(\mathrm{t},{ }^{3} \mathrm{~J}_{\mathrm{HH}}=7.3 \mathrm{~Hz}, 9 \mathrm{H}, \mathrm{N}\left(\mathrm{CH}_{2} \mathrm{CH}_{3}\right)_{3}\right)$, NH not observed. $\delta_{\mathrm{B}}\left(d_{6}\right.$-DMSO $)-6.69\left(B \mathrm{Bh}_{4}\right) . \delta_{\mathrm{C}}\left(d_{6}\right.$-DMSO) $163.58\left(\mathrm{q},{ }^{1} J_{\mathrm{BH}}=49.5 \mathrm{~Hz}\right.$, ipso-C), $135.75(\mathrm{~m}-\mathrm{CH}), 125.60(\mathrm{q}$, $\left.{ }^{4} J_{\mathrm{BH}}=2.9 \mathrm{~Hz}, m-\mathrm{CH}\right), 121.85(p-\mathrm{CH}), 46.08\left(\mathrm{~N}_{( }\left(\mathrm{CH}_{2} \mathrm{CH}_{3}\right)_{3}\right), 8.85\left(\mathrm{~N}_{\left.\left(\mathrm{CH}_{2} \mathrm{CH}_{3}\right)_{3}\right) \text {. Anal. Calc. for } \mathrm{C}_{30} \mathrm{H}_{36} \mathrm{BN} \text { : }}\right.$ C 85.50, H 8.61, N 3.32. Found: C 84.78, H 8.57, N 3.32\%.
2. NMR spectroscopic data for $\mathbf{1 - 6},\left[\mathrm{NEt}_{3} \mathrm{H}\right][\mathrm{BPh} 4]$ and reaction mixtures


Figure S1. ${ }^{1} \mathrm{H}$ NMR spectrum of $\mathbf{1 - Y}$ in $d_{6}$-benzene. * denotes Si grease impurity.


Figure $\mathbf{S 2}$. ${ }^{13} \mathrm{C}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum of $\mathbf{1 - Y}$ in $d_{6}$-benzene.


Figure S3. ${ }^{29} \operatorname{Si}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum of 1-Y in $d_{6}$-benzene. * denotes Si-grease impurity.


Figure S4. ${ }^{1} \mathrm{H}$ NMR spectrum of $\mathbf{1}$-Dy in $d_{6}$-benzene.


Figure $\mathbf{S 5} .{ }^{1} \mathrm{H}$ NMR spectrum of 2-Y in $d_{6}$-benzene.


Figure S6. ${ }^{13} \mathrm{C}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum of 2-Y in $d_{6}$-benzene.


Figure S7. ${ }^{29} \mathrm{Si}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum of $\mathbf{2 - Y}$ in $d_{6}$-benzene.


Figure S8. ${ }^{1} \mathrm{H}$ NMR spectrum of 2-Dy in $d_{6}$-benzene.


Figure S9. ${ }^{1} \mathrm{H}$ NMR spectrum of $\mathbf{3}-\mathrm{Y}$ in $d_{6}$-benzene.


Figure S10. ${ }^{13} \mathrm{C}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum of 3-Y in $d_{6}$-benzene.


Figure S11. ${ }^{29}$ Si INEPT NMR spectrum of 3-Y in $d_{6}$-benzene.


Figure S12. Combined ${ }^{13}$ C DEPT 90 and DEPT 135 NMR spectra of 3-Y in $d_{6}$-benzene.


Figure S13. ${ }^{1} \mathrm{H}$ NMR spectrum of $\mathbf{4 - Y}$ in $d_{6}$-benzene.


Figure $\mathbf{S} 14 .{ }^{11} \mathrm{~B}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum of $\mathbf{4}-\mathrm{Y}$ in $d_{6}$-benzene.


Figure S15. ${ }^{11}$ B NMR spectrum of 4-Y in $d_{6}$-benzene.


Figure S16. ${ }^{13} \mathrm{C}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum of $\mathbf{4}$-Y in $d_{6}$-benzene.


Figure $\mathbf{S 1 7 .}{ }^{29} \operatorname{Si}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum of $4-\mathrm{Y}$ in $d_{6}$-benzene.


Figure S18. ${ }^{1} \mathrm{H}$ NMR spectrum of $\mathbf{5}$-Dy in $d_{6}$-benzene.


Figure S19. ${ }^{1} \mathrm{H}$ NMR spectrum of $\mathbf{6}-\mathbf{Y}$ in $d_{6}$-benzene.


Figure S20. ${ }^{11} \mathrm{~B}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum of $\mathbf{6}-\mathrm{Y}$ in $d_{6}$-benzene.


Figure S21. ${ }^{11}$ B NMR spectrum of $\mathbf{6 - Y}$ in $d_{6}$-benzene.


Figure S22. ${ }^{13} \mathrm{C}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum of $\mathbf{6}$-Y in $d_{6}$-benzene.


Figure S23. ${ }^{29} \mathrm{Si}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum of $\mathbf{6 - Y}$ in $d_{6}$-benzene.


Figure S24. ${ }^{1} \mathrm{H}$ NMR spectrum of $\mathbf{6}$-Dy in $d_{6}$-benzene.


Figure $\mathbf{S 2 5} .{ }^{1} \mathrm{H}$ NMR spectrum of the reaction mixture between $\mathbf{6 - Y}$ and $\left[\mathrm{CPh}_{3}\right]\left[\mathrm{B}\left(\mathrm{C}_{6} \mathrm{~F}_{5}\right)_{4}\right]$ in $d_{6}$-benzene.


Figure S26. ${ }^{11} \mathrm{~B}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum of the reaction mixture between $\mathbf{6 - Y}$ and $\left[\mathrm{CPh}_{3}\right]\left[\mathrm{B}\left(\mathrm{C}_{6} \mathrm{~F}_{5}\right)_{4}\right]$ in $d_{6}$ benzene.


Figure S27. ${ }^{19} \mathrm{~F}$ NMR spectrum of the reaction mixture between $\mathbf{6}$-Y and $\left[\mathrm{CPh}_{3}\right]\left[\mathrm{B}\left(\mathrm{C}_{6} \mathrm{~F}_{5}\right)_{4}\right]$ in $d_{6}$-benzene.


Figure S28. ${ }^{29} \mathrm{Si}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum of the reaction mixture between $\mathbf{6 - Y}$ and $\left[\mathrm{CPh}_{3}\right]\left[\mathrm{B}\left(\mathrm{C}_{6} \mathrm{~F}_{5}\right)_{4}\right]$ in $d_{6}$ benzene.


Figure S29. ${ }^{1} \mathrm{H}$ NMR spectra (collected in situ) of the reaction mixture between $\mathbf{3 - Y}$ and $\left[\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right]$ in $d_{6}$-benzene. Spectrum 1 (bottom) corresponds to pure 3-Y (as in Figure S9 above); Spectrum 2 (middle) is the reaction after 5 days at room temperature; Spectrum 3 (top) is the reaction mixture after 7 days at room temperature, followed by 2 hours at $80^{\circ} \mathrm{C}$. There is no time point for 7 days at room temperature without the heating - it was decided that the progress after 5 days suggested that further time at room temperature was unlikely to have driven the reaction to completion. Note in Spectrum 2 and 3 the presence of propene and $\mathrm{NEt}_{3}$ in solution, along with the disappearance of peaks associated with $\mathbf{3 - Y}$.


Figure S30. ${ }^{11} \mathrm{~B}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum (collected in situ) of the reaction mixture between 3-Y and [ $\left.\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right]$ in $d_{6}$-benzene after 7 days at room temperature, followed by 2 hours at $80^{\circ} \mathrm{C}$. Note only a single major peak is observed; the resonance for $\mathrm{BPh}_{3}$ would be expected around 68 ppm in $d_{6}$-benzene ${ }^{[1]}$ and there is a small feature here.


Figure S31. ${ }^{29}$ Si INEPT NMR spectrum (collected in situ) of the reaction mixture between 3-Y and $\left[\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right]$ in $d_{6}$-benzene after 7 days at room temperature, followed by 2 hours at $80^{\circ} \mathrm{C}$.


Figure S32. ${ }^{1} \mathrm{H}$ NMR spectrum of the reaction mixture between $\mathbf{3}-\mathbf{Y}$ and $\left[\mathrm{CPh}_{3}\right]\left[\mathrm{B}\left(\mathrm{C}_{6} \mathrm{~F}_{5}\right)_{4}\right]$ in $d_{6}$-benzene.


Figure S33. ${ }^{11} \mathrm{~B}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum of the reaction mixture between 3-Y and $\left[\mathrm{CPh}_{3}\right]\left[\mathrm{B}\left(\mathrm{C}_{6} \mathrm{~F}_{5}\right)_{4}\right]$ in $d_{6}$ benzene.


Figure S34. ${ }^{19} \mathrm{~F}$ NMR spectrum of the reaction mixture between 3-Y and $\left[\mathrm{CPh}_{3}\right]\left[\mathrm{B}\left(\mathrm{C}_{6} \mathrm{~F}_{5}\right)_{4}\right]$ in $d_{6}$-benzene.


Figure S35. ${ }^{1} \mathrm{H}$ NMR spectrum of $\left[\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right]$ in $d_{6}$-DMSO.


Figure S36. ${ }^{11} \mathrm{~B}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum of $\left[\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right]$ in $d_{6}$-DMSO.


Figure S37. ${ }^{13} \mathrm{C}\left\{{ }^{1} \mathrm{H}\right\}$ NMR spectrum of $\left[\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right]$ in $d_{6}$-DMSO.


Figure S38. FTIR spectrum of 1-Y (ATR-IR, microcrystalline powder).


Figure S39. FTIR spectrum of 1-Dy (Nujol mull, KBr discs).


Figure S40. FTIR spectrum of 2-Y (Nujol mull, KBr discs).


Figure S41. FTIR spectrum of 2-Dy (Nujol mull, KBr discs).


Figure S42. ATR-IR spectrum of 3-Y.


Figure S43. ATR-IR spectrum of 4-Y.


Figure S44. ATR-IR spectrum of 5-Dy.


Figure S45. ATR-IR spectrum of 6-Y.


Figure S46. ATR-IR spectrum of 6-Dy.


Figure S47. ATR-IR spectrum of $\left[\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right]$.

## 4. X-ray Crystallography crystallographic data for $1-8,\left[\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right]$ and $\left[\mathrm{Mg}\left(\mathrm{Cp}^{\prime \prime \prime}\right)(\mathrm{THF})(\mu-\mathrm{Cl})\right]_{2}$

Crystal data for complexes 1-8, $\left[\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right] \cdot \mathrm{THF}$ and $\left[\mathrm{Mg}\left(\mathrm{Cp}^{\prime \prime \prime}\right)(\mathrm{THF})(\mu-\mathrm{Cl})\right]_{2} \cdot \mathrm{C}_{6} \mathrm{H}_{14}$ are compiled in Tables S1-S5. Crystal data for 1-Dy and 2-Dy were collected on an Oxford Diffraction Xcalibur2 diffractometer, equipped with 4-circle kappa geometry goniometer, an Atlas CCD area detector, a sealed tube graphite monochromated $\mathrm{MoK} \alpha$ radiation $(\lambda=0.71073 \AA$ ) source and an Oxford Instruments Cryojet, set at a temperature of 150 K . Crystal data for $\mathbf{4} \mathbf{- Y},\left[\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right] \cdot \mathrm{THF}$ and $\left[\mathrm{Mg}\left(\mathrm{Cp}^{\prime \prime \prime}\right)(\mathrm{THF})(\mu-\right.$ $\mathrm{Cl})]_{2} \cdot \mathrm{C}_{6} \mathrm{H}_{14}$ were collected on an Oxford Diffraction Supernova diffractometer, equipped with 4 -circle kappa geometry goniometer, an Eos CCD area detector, a microfocus source with MoK $\alpha$ radiation $(\lambda=$ $0.71073 \AA$ A) and an Oxford Cryosystems Cryostream 700, set at a temperature of 150 K . Crystal data for $\mathbf{1 -}$ Y, 2-Y, 3-Y•C6H14, 5-Dy, 6-Dy, 6-Y, 7-Dy and 8-Y were collected on a Rigaku FR-X DW diffractometer equipped with an AFC-11 4-circle goniometer HyPix 6000HE photon counting pixel array detector, a microfocus rotating anode source, with Mo $\mathrm{K} \alpha$ radiation $(\lambda=0.71073 \AA)\left(\mathbf{3}-\mathbf{Y} \cdot \mathbf{C}_{\mathbf{6}} \mathbf{H}_{\mathbf{1 4}}\right)$ or $\mathrm{Cu} \mathrm{K} \alpha$ radiation $(\lambda=1.54178 \AA)(\mathbf{1 - Y}, \mathbf{2 - Y}, \mathbf{5 - D y}, \mathbf{6 - Y}, \mathbf{6}-\mathrm{Dy}, \mathbf{7 - D y}$ and $\mathbf{8 - Y})$ and an Oxford Cryosystems Cryostream 800, set at a temperature of $100 \mathrm{~K}\left(\mathbf{2 - Y}\right.$ and $\left.\mathbf{3 - Y} \cdot \mathbf{C}_{6} \mathbf{H}_{\mathbf{1 4}}\right)$ or $150 \mathrm{~K}(\mathbf{1 - Y}, \mathbf{5}-\mathrm{Dy}, \mathbf{6 - Y}, \mathbf{6 - D y}, \mathbf{7 - D y}$ and $\mathbf{8 - Y})$. A multi-scan absorption correction was applied for 1-Y, 2-Y, $\mathbf{6 - Y}$ and $\mathbf{7 - D y}$, whereas a Gaussian grid faceindexed absorption correction with a beam profile correction was applied for 1-Dy, 2-Dy, 3-Y•C6H14, 4-Y, 5-Dy, 6-Dy, 8-Y, $\left[\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right] \cdot \mathrm{THF}$ and $\left[\mathrm{Mg}\left(\mathrm{Cp}^{\prime \prime \prime}\right)(\mathrm{THF})(\mu-\mathrm{Cl})\right]_{2} \cdot \mathrm{C}_{6} \mathrm{H}_{14}$. The structures were solved by direct methods and were refined by full-matrix least-squares on all unique $F^{2}$ values, with anisotropic displacement parameters for all non-hydrogen atoms, and with constrained riding hydrogen geometries. CrysAlisPro ${ }^{[2]}$ was used for control and integration, and SHELX-20XX ${ }^{[3,4]}$ was employed through OLEX2 ${ }^{[5]}$ for structure solution and refinement. ORTEP-3 $3^{[6]}$ and POVRAY ${ }^{[7]}$ were used for molecular graphics.

Table S1. Crystal data for 1-Dy, 1-Y and 1a-Y.
${ }^{a}$ Conventional $R=\Sigma| | F_{\mathrm{o}}\left|-\left|F_{c}\right| / \Sigma\right| F_{\mathrm{o}} \mid ; R_{\mathrm{w}}=\left[\Sigma \mathrm{w}\left(F_{\mathrm{o}}{ }^{2}-\mathrm{F}_{\mathrm{c}}{ }^{2}\right)^{2} / \Sigma w\left(F_{\mathrm{o}}{ }^{2}\right)^{2}\right]^{1 / 2} ; S=\left[\Sigma w\left(F_{\mathrm{o}}{ }^{2}-F_{\mathrm{c}}{ }^{2}\right)^{2} / \mathrm{no}\right.$. data - no. params) $]^{1 / 2}$ for all data.

|  | $\mathbf{1 - D y}$ | $\mathbf{1 - Y}$ | $\mathbf{1 a - Y}$ |
| :--- | :--- | :--- | :--- |
| Formula | $\mathrm{C}_{56} \mathrm{H}_{116} \mathrm{Cl}_{4} \mathrm{Dy}_{2} \mathrm{~K}_{2} \mathrm{Si}_{12}$ | $\mathrm{C}_{56} \mathrm{H}_{116} \mathrm{Cl}_{4} \mathrm{~K}_{2} \mathrm{Si}_{12} \mathrm{Y}_{2}$ | $\mathrm{C}_{56} \mathrm{H}_{116} \mathrm{Cl}_{4} \mathrm{~K}_{2} \mathrm{Si}_{12} \mathrm{Y}_{2}$ |
| Fw | 1671.56 | 1524.38 | 1524.38 |
| Temperature, K | $150.00(10)$ | $150.00(10)$ | $150.00(10)$ |
| Crystal size, mm | $0.141 \times 0.084 \times 0.065$ | $0.425 \times 0.102 \times 0.067$ | $0.425 \times 0.102 \times 0.067$ |
| Crystal system | monoclinic | monoclinic | triclinic |
| Space group | $P 2_{1} / n$ | $P 2_{1} / n$ | $P-1$ |
| $a, \AA$ | $11.0500(7)$ | $11.05270(10)$ | $11.0201(5)$ |
| $b, \AA$ | $16.0860(11)$ | $16.0815(2)$ | $12.1921(11)$ |
| $c, \AA$ | $23.5320(18)$ | $23.5252(3)$ | $16.0564(9)$ |
| $\alpha,{ }^{\circ}$ |  |  | $81.714(7)$ |
| $\beta,{ }^{\circ}$ | $101.589(7)$ | $101.6330(10)$ | $89.858(4)$ |
| $\gamma,{ }^{\circ}$ |  |  | $74.331(7)$ |
| $V, \AA^{3}$ | $4097.5(5)$ | $4095.57(8)$ | $2054.0(2)$ |
| Z | 2 | 2 | 1 |
| $\rho_{\text {calc, }} \mathrm{g} /$ cm ${ }^{3}$ | 1.355 | 1.236 | 1.232 |
| $\mu$, mm $^{-1}$ | 2.248 | 5.914 | 5.896 |
| $F(000)$ | 1716 | 1608 | 804 |
| No. of reflection (uniq. $)$ | $15047(7524)$ | $20846(6384)$ | $5720(2877)$ |
| $R$ Rint | 0.148 | 0.038 | 0.133 |
| Data/restraints/parameters | $7524 / 626 / 361$ | $6384 / 0 / 361$ | $2877 / 626 / 361$ |
| $S^{a}$ | 0.97 | 1.08 | 1.14 |
| $R_{l}\left(w R_{2}\right)\left(F^{2}>2 \sigma\left(F^{2}\right)\right)$ | $0.1012(0.1488)$ | $0.0459(0.1204)$ | $0.1325(0.3793)$ |
| $R_{l}\left(w R_{2}\right)$ All Data | $0.2058(0.1916)$ | $0.0505(0.1246)$ | $0.1679(0.4061)$ |
| min. $/$ max. diff map, e $\AA^{-3}$ | $1.29 /-1.46$ | $1.15 /-0.68$ | $0.41 /-0.56$ |
|  |  |  |  |

Table S2. Crystal data for 2-Dy, 2-Y and 3-Y.
${ }^{a}$ Conventional $R=\Sigma| | F_{\mathrm{o}}\left|-\left|F_{c}\right| / \Sigma\right| F_{\mathrm{o}} \mid ; R_{\mathrm{w}}=\left[\Sigma \mathrm{w}\left(F_{\mathrm{o}}{ }^{2}-\mathrm{F}_{\mathrm{c}}{ }^{2}\right)^{2} / \Sigma w\left(F_{\mathrm{o}}{ }^{2}\right)^{2}\right]^{1 / 2} ; S=\left[\Sigma w\left(F_{\mathrm{o}}{ }^{2}-F_{\mathrm{c}}{ }^{2}\right)^{2} / \mathrm{no}\right.$. data - no. params) $]^{1 / 2}$ for all data.

|  | 2-Dy | 2-Y | 3-Y |
| :---: | :---: | :---: | :---: |
| Formula | $\mathrm{C}_{32} \mathrm{H}_{66} \mathrm{ClDyOSi}_{6}$ | $\mathrm{C}_{32} \mathrm{H}_{66} \mathrm{ClOSi}_{6} \mathrm{Y}$ | $\mathrm{C}_{37} \mathrm{H}_{77} \mathrm{Si}_{6} \mathrm{Y}$ |
| Fw | 833.33 | 759.74 | 779.43 |
| Temperature, K | 150.0(2) | 100.0(2) | 99.98(2) |
| Crystal size, mm | $0.377 \times 0.251 \times 0.191$ | $0.135 \times 0.072 \times 0.065$ | $0.589 \times 0.232 \times 0.203$ |
| Crystal system | monoclinic | monoclinic | triclinic |
| Space group | $P 21 / c$ | $P 2{ }_{1} / \mathrm{c}$ | $P-1$ |
| $a, ~ \AA$ | 16.6630(5) | 16.47510(10) | 10.9184(3) |
| $b, \AA$ | 13.2108(4) | 13.16310(10) | 12.8213(3) |
| $c, \AA$ | 20.1131(6) | 20.11540(10) | 17.0002(4) |
| $\alpha,{ }^{\circ}$ |  |  | 88.0069(19) |
| $\beta,{ }^{\circ}$ | 94.233(3) | 94.1510(10) | 83.231(2) |
| $\gamma,{ }^{\circ}$ |  |  | 76.864(2) |
| $V, \AA^{3}$ | 4415.4(2) | 4350.85(5) | 2301.32(10) |
| Z | 4 | 4 | 2 |
| $\rho_{\text {calc, }} \mathrm{g} / \mathrm{cm}^{3}$ | 1.254 | 1.16 | 1.125 |
| $\mu, \mathrm{mm}^{-1}$ | 1.937 | 4.191 | 1.446 |
| $F(000)$ | 1732 | 1624 | 844 |
| No. of reflection (uniq.) | 27776 (10383) | 47250 (8997) | 27379 (8406) |
| Rint | 0.038 | 0.043 | 0.065 |
| Data/restraints/parameters | 10383/383/465 | 8997/2420/749 | 8406/0/427 |
| $S^{a}$ | 1.03 | 1.08 | 1.05 |
| $R_{1}\left(w R_{2}\right)\left(F^{2}>2 \sigma\left(F^{2}\right)\right)$ | 0.0342 (0.0603) | 0.0330 (0.0814) | 0.0546 (0.1469) |
| $R_{1}\left(w R_{2}\right)$ All Data | 0.0508 (0.0669) | 0.0366 (0.0831) | 0.0623 (0.1515) |
| min./max. diff map, e $\AA^{-3}$ | 0.90/-0.71 | 0.72/-0.67 | 2.16/-0.60 |

Table S3. Crystal data for 5-Dy, 6-Dy and 6-Y.
${ }^{a}$ Conventional $R=\Sigma| | F_{\mathrm{o}}\left|-\left|F_{c}\right| / \Sigma\right| F_{\mathrm{o}} \mid ; R_{\mathrm{w}}=\left[\Sigma \mathrm{w}\left(F_{\mathrm{o}}{ }^{2}-\mathrm{F}_{\mathrm{c}}{ }^{2}\right)^{2} / \Sigma w\left(F_{\mathrm{o}}{ }^{2}\right)^{2}\right]^{1 / 2} ; S=\left[\Sigma w\left(F_{\mathrm{o}}{ }^{2}-F_{\mathrm{c}}{ }^{2}\right)^{2} / \mathrm{no}\right.$. data - no. params) $]^{1 / 2}$ for all data.

|  | $\mathbf{4 - Y}$ | $\mathbf{5 - D y}$ | $\mathbf{6 - D y}$ |
| :--- | :--- | :--- | :--- |
| Formula | $\mathrm{C}_{18} \mathrm{H}_{45} \mathrm{~B}_{2} \mathrm{OSi}_{3} \mathrm{Y}$ | $\mathrm{C}_{56} \mathrm{H}_{148} \mathrm{~B}_{8} \mathrm{Dy}_{4} \mathrm{Si}_{12}$ | $\mathrm{C}_{28} \mathrm{H}_{62} \mathrm{BDySi}_{6}$ |
| Fw | 472.34 | 1895.3 | 740.62 |
| Temperature, K | $150(2)$ | $149.99(10)$ | $150.00(10)$ |
| Crystal size, mm | $0.26 \times 0.177 \times 0.074$ | $0.146 \times 0.101 \times 0.058$ | $0.298 \times 0.215 \times 0.189$ |
| Crystal system | monoclinic | triclinic | monoclinic |
| Space group | $P 2_{1} / n$ | $P-1$ | $P 2_{1}$ |
| $a, \AA$ | $13.0628(10)$ | $11.7394(4)$ | $10.85530(15)$ |
| $b, \AA$ | $12.6435(13)$ | $15.4866(6)$ | $16.84522(19)$ |
| $c, \AA$ | $17.2075(15)$ | $57.0982(12)$ | $11.34382(15)$ |
| $\alpha,{ }^{\circ}$ |  | $88.431(2)$ |  |
| $\beta,{ }^{\circ}$ | $102.680(9)$ | $87.394(2)$ | $108.4482(15)$ |
| $\gamma,{ }^{\circ}$ |  | $68.254(3)$ |  |
| $V, \AA^{3}$ | $2772.7(4)$ | $9631.3(6)$ | $1967.73(5)$ |
| Z | 4 | 4 | 2 |
| $\rho_{\text {calc, }, \mathrm{g} / \mathrm{cm}}{ }^{3}$ | 1.132 | 1.307 | 1.25 |
| $\mu, \mathrm{~mm}^{-1}$ | 2.238 | 17.938 | 12.006 |
| $F(000)$ | 1008 | 3824 | 770 |
| No. of reflection (uniq. $)$ | $9085(5028)$ | $62038(20111)$ | $41794(7142)$ |
| Rint | 0.081 | 0.111 | 0.040 |
| Data/restraints/parameters | $5028 / 290 / 267$ | $20111 / 364 / 1566$ | $7142 / 5 / 355$ |
| $S^{a}$ | 1.03 | 1.1 | 1.06 |
| $R_{1}\left(w R_{2}\right)\left(F^{2}>2 \sigma\left(F^{2}\right)\right)$ | $0.0745(0.1323)$ | $0.0670(0.1694)$ | $0.0256(0.0706)$ |
| $R_{1}\left(w R_{2}\right)$ All Data | $0.1461(0.1741)$ | $0.0927(0.1839)$ | $0.0258(0.0707)$ |
| min. $/$ max. diff map, e $\AA^{-3}$ | $0.96 /-0.97$ | $1.71 /-1.96$ | $0.61 /-0.70$ |
| Flack parameter |  | $-0.003(2)$ | $-0.027(3)$ |

Table S4. Crystal data for 6-Y, 7-Dy and 8-Y.
${ }^{a}$ Conventional $R=\Sigma| | F_{\mathrm{o}}\left|-\left|F_{c}\right| / \Sigma\right| F_{\mathrm{o}} \mid ; R_{\mathrm{w}}=\left[\Sigma \mathrm{w}\left(F_{\mathrm{o}}{ }^{2}-\mathrm{F}_{\mathrm{c}}{ }^{2}\right)^{2} / \Sigma w\left(F_{\mathrm{o}}{ }^{2}\right)^{2}\right]^{1 / 2} ; S=\left[\Sigma w\left(F_{\mathrm{o}}{ }^{2}-F_{\mathrm{c}}{ }^{2}\right)^{2} / \mathrm{no}\right.$. data - no. params) $]^{1 / 2}$ for all data.

|  | 6-Y | 7-Dy | 8-Y |
| :---: | :---: | :---: | :---: |
| Formula | $\mathrm{C}_{28} \mathrm{H}_{62} \mathrm{BSi}_{6} \mathrm{Y}$ | $\mathrm{C}_{32} \mathrm{H}_{70} \mathrm{BDyOOSi}_{6}$ | $\mathrm{C}_{52} \mathrm{H}_{78} \mathrm{BSi}_{6} \mathrm{Y}$ |
| Fw | 667.03 | 812.73 | 971.4 |
| Temperature, K | 150(2) | 150.07(10) | 150(2) |
| Crystal size, mm | $0.367 \times 0.155 \times 0.151$ | $0.209 \times 0.145 \times 0.122$ | $0.148 \times 0.123 \times 0.106$ |
| Crystal system | monoclinic | monoclinic | triclinic |
| Space group | $P 2{ }_{1}$ | $P 2{ }_{1} / \mathrm{c}$ | $P-1$ |
| $a, \AA$ | 10.83339(8) | 16.8987(3) | 12.52981(18) |
| $b, \AA$ | 16.83695(10) | 13.0779(2) | 21.5621(3) |
| $c, \AA$ | 11.33098(8) | 20.2904(3) | 23.3261(4) |
| $\alpha,{ }^{\circ}$ |  |  | 64.3568(16) |
| $\beta,{ }^{\circ}$ | 108.3363(8) | 93.1940(10) | 77.9174(13) |
| $\gamma,{ }^{\circ}$ |  |  | 80.8704(13) |
| $V, \AA^{3}$ | 1961.85(2) | 4477.20(12) | 5538.85(17) |
| Z | 2 | 4 | 4 |
| $\rho_{\text {calc, }} \mathrm{g} / \mathrm{cm}^{3}$ | 1.129 | 1.206 | 1.165 |
| $\mu, \mathrm{mm}^{-1}$ | 3.947 | 10.613 | 2.953 |
| $F(000)$ | 716 | 1700 | 2072 |
| No. of reflection (uniq.) | 22451 (7159) | 51395 (8196) | 86762 (20083) |
| Rint | 0.0157 | 0.0801 | 0.0386 |
| Data/restraints/parameters | 7159/5/355 | 8196/119/440 | 20083/0/1117 |
| $S^{a}$ | 1.03 | 1.09 | 1.03 |
| $R_{I}\left(w R_{2}\right)\left(F^{2}>2 \sigma\left(F^{2}\right)\right)$ | 0.0160 (0.0422) | 0.0454 (0.1204) | 0.0330 (0.0817) |
| $R_{1}\left(w R_{2}\right)$ All Data | 0.0162 (0.0423) | 0.0533 (0.1248) | 0.0387 (0.0844) |
| min./max. diff map, e $\AA^{-3}$ | 0.24/-0.33 | 0.79/-1.83 | 0.59/-0.59 |

Table S5. Crystal data for $\left[\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right] \cdot$ THF and $\left[\mathrm{Mg}\left(\mathrm{Cp}^{\prime \prime \prime}\right)(\mathrm{THF})(\mu-\mathrm{Cl})\right]_{2} \cdot \mathrm{C}_{6} \mathrm{H}_{14}$.
${ }^{a}$ Conventional $R=\Sigma| | F_{\mathrm{o}}\left|-\left|F_{c}\right| / \Sigma\right| F_{\mathrm{o}} \mid ; R_{\mathrm{w}}=\left[\Sigma \mathrm{w}\left(F_{\mathrm{o}}{ }^{2}-\mathrm{F}_{\mathrm{c}}{ }^{2}\right)^{2} / \Sigma w\left(F_{\mathrm{o}}{ }^{2}\right)^{2}\right]^{1 / 2} ; S=\left[\Sigma w\left(F_{\mathrm{o}}{ }^{2}-F_{\mathrm{c}}{ }^{2}\right)^{2} / \mathrm{no}\right.$. data - no. params) $]^{1 / 2}$ for all data.

|  | $\left[\mathrm{NEt}_{3} \mathrm{H}\right][\mathrm{BPh} 4] \cdot \mathrm{THF}$ | $\left[\mathrm{Mg}\left(\mathrm{Cp}^{\prime \prime}\right)(\mathrm{THF})\left(\mu-\mathrm{Cl}_{2}\right]_{2} \cdot \mathrm{C}_{6} \mathrm{H}_{14}\right.$ |
| :--- | :--- | :--- |
| Formula | $\mathrm{C}_{34} \mathrm{H}_{44} \mathrm{BNO}$ | $\mathrm{C}_{42} \mathrm{H}_{88} \mathrm{Cl}_{2} \mathrm{Mg}_{2} \mathrm{O}_{2} \mathrm{Si}_{6}$ |
| Fw | 493.51 | 913.18 |
| Temperature, K | $100(2)$ | $150(2)$ |
| Crystal size, mm | $0.198 \times 0.424 \times 0.667$ | $0.147 \times 0.228 \times 0.242$ |
| Crystal system | monoclinic | triclinic |
| Space group | $P 2_{1} / c$ | $P-1$ |
| $a, \AA$ | $28.936(3)$ | $11.3143(7)$ |
| $b, \AA$ | $18.392(2)$ | $11.4487(7)$ |
| $c, \AA$ | $16.501(2)$ | $12.8059(8)$ |
| $\alpha,{ }^{\circ}$ |  | $65.240(6)$ |
| $\beta,{ }^{\circ}$ | $97.868(11)$ | $66.971(6)$ |
| $\gamma,{ }^{\circ}$ |  | $84.947(5)$ |
| $V, \AA^{3}$ | $8699.0(17)$ | $1380.56(16)$ |
| Z | 12 | 1 |
| $\rho_{\text {calcd }}, \mathrm{g}$ cm ${ }^{3}$ | 1.130 | 1.098 |
| $\mu$, mm ${ }^{-1}$ | 0.066 | 0.301 |
| $F(000)$ | 3216 | 498 |
| No. of reflections (uniq. $)$ | $13734(6649)$ | $8027(5008)$ |
| $R i n t$ | 0.091 | 0.031 |
| Data/restraints/parameters | $17524 / 0 / 1009$ | $5008 / 237 / 254$ |
| $S^{\text {a }}$ | 0.97 | 1.03 |
| $R_{1}\left(w R_{2}\right)\left(F^{2}>2 \sigma\left(F^{2}\right)\right)$ | $0.0552(0.1357)$ | $0.0681(0.1676)$ |
| $R 1(w R 2)$ All Data | $0.0753(0.1479)$ | $0.0977(0.1880)$ |
| min. $/$ max. diff map, e $\AA^{-3}$ | $-0.294,0.326$ | $-0.44,1.54$ |
|  |  |  |



Figure S48. Molecular structure of $\left[\left\{\mathrm{Y}_{( }\left(\mathrm{Cp}^{\prime \prime \prime}\right)_{2}(\mu-\mathrm{Cl})_{2} \mathrm{~K}\right\}_{2}\right]_{\infty}$ (1-Y) with selective atom labelling. Displacement ellipsoids set at 30 \% probability level and hydrogen atoms omitted for clarity. Symmetry operation to generate equivalent atoms: $2-x, 1-y, 1-z$.


Figure S49. Molecular structure of $\left[\mathrm{Y}\left(\mathrm{Cp}^{\prime \prime \prime}\right)_{2}(\mathrm{THF})(\mathrm{Cl})\right](\mathbf{2}-\mathrm{Y})$ with selective atom labelling. Displacement ellipsoids set at $30 \%$ probability level and hydrogen atoms and modelled disorder components omitted for clarity.


Figure S50. Molecular structure of $\left[\mathrm{Y}\left(\mathrm{Cp}^{\prime \prime \prime}\right)_{2}\left(\mathrm{BH}_{4}\right)\right](\mathbf{6 - Y})$ with selective atom labelling. Displacement ellipsoids set at $30 \%$ probability level and hydrogen atoms omitted for clarity, with the exception of those belonging to the borohydride group.


Figure S51. Molecular structure of $\left[\mathrm{NEt}_{3} \mathrm{H}\right]\left[\mathrm{BPh}_{4}\right]$. THF with selective atom labelling. Displacement ellipsoids set at $30 \%$ probability level and hydrogen atoms and lattice solvent omitted for clarity.


Figure S52. Molecular structure of $\left[\mathrm{Mg}\left(\mathrm{Cp}^{\prime \prime \prime}\right)(\mathrm{THF})(\mu-\mathrm{Cl})\right]_{2}$ with selective atom labelling. Displacement ellipsoids set at $30 \%$ probability level and hydrogen atoms omitted for clarity. Symmetry operation to generate equivalent atoms: $-x,-y, 1-z$.

## 5. Magnetic data for 5-Dy

Magnetic measurements were performed on a Quantum Design MPMS3 superconducting quantum interference device (SQUID) magnetometer. The sample of 5-Dy (19.1 mg) was ground to a powder, loaded in a borosilicate glass NMR tube and covered in ground eicosane $(9.7 \mathrm{mg})$ in a glovebox. The tube was removed from the glovebox, kept under a protected atmosphere and transferred onto a Schlenk line, where the eicosane powder was melted under an argon atmosphere. The NMR tube was then sealed at $\sim 3 \mathrm{~cm}$ under reduced pressure. Kapton tape was wrapped around the top of the tube, the NMR tube was held inside a straw by friction, and the straw was attached to the end of the sample rod.

All dc measurements were taken in dc scan mode with a 40 mm scan length and scan time of 60 s . The raw data were corrected for the diamagnetic contribution of the sample holder and eicosane using calibrated blanks. The data were corrected for the sample shape using the Quantum Design MPMS3 Geometry Simulator, assuming a uniform cylinder of 4.06 mm diameter and 3.58 mm height. Finally the data were corrected for the intrinsic diamagnetic contribution of the sample, estimated as the molecular weight ( $\mathrm{g} / \mathrm{mol}$ ) multiplied by $0.5 \times 10^{-6} \mathrm{~cm}^{3} \mathrm{~K} \mathrm{~mol}^{-1}$.

The equilibrium susceptibility was measured on cooling in temperature settle mode, with rates of 5 $\mathrm{K} / \mathrm{min}$ between 300 and $100 \mathrm{~K}, 2 \mathrm{~K} / \mathrm{min} 100-10 \mathrm{~K}$ and $1 \mathrm{~K} / \mathrm{min}$ below 10 K . The zero-field cooled (ZFC) and field cooled (FC) measurements were performed in temperature sweep mode with a sweep rate of 0.5 $\mathrm{K} / \mathrm{min}$ and range $2-100 \mathrm{~K}$. The ZFC sample was prepared by cooling from at least 100 K in zero field and holding at 2 K for 2.5 hrs before rapidly ramping the dc field at $700 \mathrm{Oe} / \mathrm{s}$ to 0.1 T and beginning the measurement on warming. The FC measurement was performed on cooling at the same rate. Hysteresis measurements were performed between +7 and -7 T in field sweep mode with sweep rates of $22 \mathrm{Oe} / \mathrm{s}$ between $\pm 1 \mathrm{~T}, 54 \mathrm{Oe} / \mathrm{s}$ for 1-2 T and $91 \mathrm{Oe} / \mathrm{s}$ for 2-7 T . Magnetisation measurements were performed between 0-7 T at 2 and 4 K in field settle mode. The field was ramped at $500 \mathrm{Oe} / \mathrm{s}$ between points and held constant for at least 5 min before measuring ( 10 min at $2 \mathrm{~K}, 0-3.5 \mathrm{~T}$ ). All ac data were collected with a five point measure, using an oscillating field amplitude of $\mathrm{H}_{\mathrm{ac}}=2 \mathrm{Oe}$. Data were collected at $8 \log$-spaced frequencies per decade in the range $0.1-1000 \mathrm{~Hz}$, averaging over 2 sec or 10 cycles, whichever was longer.


Figure S53. Temperature dependence of the product of magnetic susceptibility and temperature $(\chi \mathrm{T})$ for 5Dy, reported per Dy ion.


Figure S54. Magnetisation vs. field at 2 K (black) and 4 K (red) for 5-Dy, reported per Dy ion.


Figure S55. Hysteresis curve at 2 K (black) and 4 K (red) for 5-Dy, reported per Dy ion. Points recorded in 250 Oe steps with sweep rates of $22 \mathrm{Oe} / \mathrm{s}$ for $|\mathrm{H}|<1 \mathrm{~T}, 54 \mathrm{Oe} / \mathrm{s}$ for $1<|\mathrm{H}|<2 \mathrm{~T}$ and $91 \mathrm{Oe} / \mathrm{s}$ for $2<|\mathrm{H}|$ $<7 \mathrm{~T}$.


Figure S56. Zero-field cooled susceptibility measured on warming (black) and field-cooled susceptibility measured on cooling (red) for 5-Dy, reported per Dy ion. Measurements performed for 2-100 K, recording points every 1 K and with a sweep rate of $0.5 \mathrm{~K} / \mathrm{min}$.


Figure S57. Cole-Cole plot for 5-Dy, reported per Dy ion, at 2-8 K and measured in an applied field of 0.1 T. Lines are guides for the eye.


Figure S58. Frequency dependence of the out-of-phase susceptibility ( $\chi^{\prime \prime}$ ) per Dy ion for 5-Dy, measured at 2-8 K in an applied field of 0.1 T . Lines are guides for the eye.

## 6. CASSCF-SO calculations for 5-Dy

OpenMolcas ${ }^{[8]}$ was used to perform CASSCF-SO calculations on each $\left[\mathrm{Dy}\left(\mathrm{Cp}^{\prime \prime \prime}\right)\left(\mathrm{BH}_{4}\right)_{3}\right]^{-}$unit of 5Dy to determine the electronic structures of the four independent Dy(III) ions. The molecular geometries from the single crystal XRD structure were used with no optimization, taking the largest disorder component only. Integrals were performed in the SEWARD module using basis sets from ANO-RCC library ${ }^{[9,10]}$ with VTZP quality for Dy atoms, VDZP quality for the cyclopentadienyl C atoms and the borohydride B atoms and VDZ quality for all remaining atoms, employing the second-order DKH transformation. Cholesky decomposition of the two-electron integrals with a threshold of $10^{-8}$ was performed to save disk space and reduce computational demand. The molecular orbitals (MOs) were optimised in state-averaged CASSCF calculations in the RASSCF module, where the active space was defined by the nine 4 f electrons in the seven 4 f orbitals of $\operatorname{Dy}(\mathrm{III})$. Three such calculations were performed independently for each possible spin state, where 21 roots were included for $S=5 / 2,224$ roots were included for $S=3 / 2$, and 490 roots were included for $S=1 / 2$. The wavefunctions obtained from these CASSCF calculations were then mixed by spin orbit coupling in the RASSI module, where all $21 \mathrm{~S}=5 / 2$ states, the lowest $128 \mathrm{~S}=3 / 2$ states, and the lowest $130 \mathrm{~S}=1 / 2$ states were included. SINGLE_ANISO was used to decompose the resulting spin-orbit wave functions into the CF Hamiltonian formalism. ${ }^{[11]}$ Diamond was employed for molecular graphics. ${ }^{[12]}$

Table S6. Electronic structure of $\left[\mathrm{Dy}\left(\mathrm{Cp}^{\prime \prime \prime}\right)\left(\mathrm{BH}_{4}\right)_{3}\right]^{-}($where $\mathrm{Dy}(1)$ is the central ion) calculated with the crystal field parameters obtained from CASSCF-SO using the solid state geometry of 5-Dy in zero-field. Each row corresponds to a Kramers doublet.

| $\begin{aligned} & \hline \text { Energy } \\ & \left(\mathrm{cm}^{-1}\right) \end{aligned}$ | Energy (K) | $g_{\mathrm{x}}$ | $g_{y}$ | $g_{z}$ | $\begin{gathered} \hline \text { Angle }^{\mathrm{a}} \\ \text { (deg) } \end{gathered}$ | Wavefunction | $\left\langle J_{z}>\right.$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.00 | 0.00 | 0.0 | 0.0 | 19.8 | -- | $98.9 \% \pm 15 / 2\rangle$ | $\pm 7.5$ |
| 102.11 | 146.94 | 0.2 | 0.4 | 18.6 | 75.6 | $\begin{gathered} 21 \%\| \pm 5 / 2\rangle+16 \%\|\mp 7 / 2\rangle+15 \% \\ \| \pm 9 / 2\rangle+13 \%\|\mp 3 / 2\rangle+10 \%\| \pm 1 / 2\rangle \\ +8 \%\| \pm 7 / 2\rangle+6 \%\|\mp 11 / 2\rangle \end{gathered}$ | $\pm 3.1$ |
| 148.08 | 213.08 | 1.8 | 2.1 | 15.6 | 26.2 | $\begin{gathered} 46 \%\| \pm 13 / 2\rangle+22 \%\| \pm 11 / 2\rangle+14 \% \\ \mp \mp 13 / 2\rangle+5 \%\| \pm 9 / 2\rangle \end{gathered}$ | $\pm 5.8$ |
| 86.72 | 268.69 | 4.8 | 7.0 | 8.2 | 83.1 | $\begin{gathered} 28 \%\| \pm 9 / 2\rangle+13 \%\|\mp 7 / 2\rangle+11 \% \\ \| \pm 13 / 2\rangle+10 \%\|\mp 11 / 2\rangle+9 \% \\ \|\mp 13 / 2\rangle+8 \%\| \pm 11 / 2\rangle+5 \%\| \pm 7 / 2\rangle \end{gathered}$ | $\pm 4.6$ |
| 218.05 | 313.77 | 0.1 | 0.7 | 18.2 | 84.5 | $\begin{gathered} 26 \%\| \pm 5 / 2\rangle+25 \%\|\mp 3 / 2\rangle+20 \% \\ \pm 1 / 2\rangle+12 \%\|\mp 7 / 2\rangle \end{gathered}$ | $\pm 2.2$ |
| 254.04 | 365.57 | 0.4 | 2.6 | 13.6 | 82.8 | $\begin{gathered} 21 \%\| \pm 1 / 2\rangle+20 \%\|\mp 7 / 2\rangle+13 \% \\ \| \pm 9 / 2\rangle+9 \%\| \pm 11 / 2\rangle+9 \%\|\mp 11 / 2\rangle \\ +6 \%\|\mp 5 / 2\rangle+5 \%\| \pm 3 / 2\rangle+5 \% \\ \|\mp 3 / 2\rangle \end{gathered}$ | $\pm 3.2$ |
| 284.25 | 409.04 | 0.9 | 2.5 | 16.2 | 64.7 | $\begin{gathered} 17 \%\| \pm 9 / 2\rangle+17 \%\| \pm 5 / 2\rangle+15 \% \\ \pm \pm 11 / 2\rangle+12 \%\|\mp 3 / 2\rangle+11 \% \\ \|\mp 7 / 2\rangle+7 \%\| \pm 13 / 2\rangle+7 \% \\ \|\mp 11 / 2\rangle+7 \%\| \pm 1 / 2\rangle \end{gathered}$ | $\pm 3.8$ |
| 397.99 | 572.71 | 0.0 | 0.1 | 19.3 | 85.5 | $\begin{gathered} 28 \%\| \pm 3 / 2\rangle+26 \%\|\mp 3 / 2\rangle+10 \% \\ \|\mp 5 / 2\rangle+9 \%\| \pm 1 / 2\rangle+8 \%\| \pm 7 / 2\rangle+ \\ 8 \%\| \pm 5 / 2\rangle+5 \%\|\mp 9 / 2\rangle \end{gathered}$ | $\pm 1.9$ |

${ }^{\mathrm{a}}$ The angle between the $\mathrm{g}_{2}$ value of the excited Kramers doublet and the ground Kramers doublet.

Table S7. Electronic structure of $\left[\mathrm{Dy}\left(\mathrm{Cp}^{\prime \prime \prime}\right)\left(\mathrm{BH}_{4}\right)_{3}\right]^{-}($where $\mathrm{Dy}(2)$ is the central ion) calculated with the crystal field parameters obtained from CASSCF-SO using the solid state geometry of 5-Dy in zero-field. Each row corresponds to a Kramers doublet.

| Energy $\left(\mathrm{cm}^{-1}\right)$ | Energy <br> (K) | $g_{x}$ | $g_{y}$ | $g_{z}$ | Angle ${ }^{\text {a }}$ <br> (deg) | Wavefunction | < $J_{\mathrm{Z}}>$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.00 | 0.00 | 0.6 | 5.8 | 13.0 | -- | $\begin{gathered} 36 \%\| \pm 15 / 2\rangle+30 \%\| \pm 11 / 2\rangle+18 \% \\ \| \pm 7 / 2\rangle \end{gathered}$ | $\pm 5.4$ |
| 16.10 | 23.17 | 1.4 | 3.9 | 12.3 | 42.1 | $\begin{gathered} 25 \%\| \pm 9 / 2\rangle+15 \%\|\mp 9 / 2\rangle+14 \% \\ \| \pm 15 / 2\rangle+10 \%\|\mp 5 / 2\rangle+9 \%\| \pm 5 / 2\rangle \end{gathered}$ | $\pm 4.5$ |
| 57.57 | 82.84 | 0.8 | 1.9 | 14.0 | 24.7 | $\begin{gathered} 49 \%\| \pm 13 / 2\rangle+20 \%\| \pm 7 / 2\rangle+12 \% \\ \| \pm 11 / 2\rangle+5 \%\| \pm 3 / 2\rangle \end{gathered}$ | $\pm 5.3$ |
| 97.73 | 140.64 | 1.6 | 4.3 | 9.9 | 74.3 | $\begin{gathered} 19 \%\| \pm 3 / 2\rangle+16 \%\|\mp 5 / 2\rangle+11 \% \\ \|\mp 1 / 2\rangle+9 \%\|\mp 13 / 2\rangle+8 \% \\ \| \pm 15 / 2\rangle+7 \%\|\mp 11 / 2\rangle+6 \% \\ \| \pm 11 / 2\rangle+5 \%\| \pm 9 / 2\rangle \end{gathered}$ | $\pm 3.6$ |
| 118.91 | 171.11 | 2.2 | 6.2 | 7.4 | 38.5 | $\begin{gathered} 25 \%\| \pm 15 / 2\rangle+15 \%\| \pm 9 / 2\rangle+13 \% \\ \| \pm 11 / 2\rangle+11 \%\|\mp 9 / 2\rangle+8 \% \\ \|\mp 11 / 2\rangle+6 \%\|\mp 5 / 2\rangle+5 \% \\ \|\mp 13 / 2\rangle+5 \%\|\mp 1 / 2\rangle \end{gathered}$ | $\pm 5.0$ |
| 137.99 | 198.57 | 0.5 | 4.3 | 6.5 | 46.0 | $\begin{gathered} 17 \%\| \pm 7 / 2\rangle+16 \%\|\mp 7 / 2\rangle+12 \% \\ \| \pm 13 / 2\rangle+9 \%\|\mp 1 / 2\rangle+8 \%\| \pm 11 / 2\rangle \\ +8 \%\|\mp 15 / 2\rangle+7 \%\| \pm 9 / 2\rangle+7 \% \\ \|\mp 3 / 2\rangle+5 \%\|\mp 11 / 2\rangle+5 \%\|\mp 9 / 2\rangle \end{gathered}$ | $\pm 4.0$ |
| 176.71 | 254.29 | 2.9 | 5.4 | 12.3 | 86.3 | $\begin{gathered} 28 \%\| \pm 5 / 2\rangle+18 \%\|\bar{\mp} 1 / 2\rangle+10 \% \\ \| \pm 3 / 2\rangle+9 \%\|\mp 7 / 2\rangle+8 \%\|\mp 3 / 2\rangle+ \\ 5 \%\| \pm 11 / 2\rangle+5 \%\|\mp 5 / 2\rangle \end{gathered}$ | $\pm 2.7$ |
| 274.31 | 394.73 | 0.1 | 0.3 | 19.0 | 83.5 | $\begin{aligned} & 34 \%\| \pm 1 / 2\rangle+18 \%\|\mp 3 / 2\rangle+15 \% \\ & \| \pm 5 / 2\rangle+14 \%\| \pm 3 / 2\rangle+8 \%\|\mp 1 / 2\rangle \end{aligned}$ | $\pm 1.5$ |

[^0]Table S8. Electronic structure of $\left[\mathrm{Dy}\left(\mathrm{Cp}^{\prime \prime \prime}\right)\left(\mathrm{BH}_{4}\right)_{3}\right]^{-}($where $\mathrm{Dy}(3)$ is the central ion) calculated with the crystal field parameters obtained from CASSCF-SO using the solid state geometry of 5-Dy in zero-field. Each row corresponds to a Kramers doublet.

| Energy <br> $\left(\mathrm{cm}^{-1}\right)$ | Energy <br> (K) | $g_{x}$ | $g_{y}$ | $g_{z}$ | Angle ${ }^{a}$ <br> (deg) | Wavefunction | < ${ }_{\text {z }}>$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.00 | 0.00 | 0.1 | 0.2 | 19.2 | -- | $91 \%\| \pm 15 / 2\rangle+5 \%\| \pm 9 / 2\rangle$ | $\pm 7.2$ |
| 68.78 | 98.97 | 0.5 | 0.8 | 17.9 | 44.0 | $\begin{gathered} 37 \%\| \pm 11 / 2\rangle+26 \%\| \pm 13 / 2\rangle+16 \% \\ \| \pm 9 / 2\rangle+5 \%\| \pm 15 / 2\rangle+5 \%\|\mp 1 / 2\rangle \end{gathered}$ | $\pm 5.1$ |
| 95.35 | 137.21 | 2.7 | 3.8 | 12.2 | 40.8 | $\begin{gathered} 31 \%\| \pm 7 / 2\rangle+26 \%\| \pm 13 / 2\rangle+13 \% \\ \| \pm 9 / 2\rangle+7 \%\|\mp 3 / 2\rangle+6 \%\|\mp 5 / 2\rangle+ \\ 5 \%\|\mp 7 / 2\rangle+5 \%\| \pm 5 / 2\rangle \end{gathered}$ | $\pm 4.3$ |
| 143.06 | 205.86 | 1.4 | 4.7 | 10.2 | 89.4 | $\begin{gathered} 19 \%\| \pm 5 / 2\rangle+16 \%\|\mp 5 / 2\rangle+15 \% \\ \| \pm 3 / 2\rangle+10 \%\| \pm 11 / 2\rangle+8 \% \\ \| \pm 13 / 2\rangle+7 \%\|\mp 1 / 2\rangle+6 \%\|\mp 9 / 2\rangle \\ +5 \%\| \pm 9 / 2\rangle+5 \%\|\mp 3 / 2\rangle \end{gathered}$ | $\pm 3.2$ |
| 168.06 | 241.84 | 1.8 | 2.6 | 13.0 | 89.2 | $\begin{gathered} 17 \%\| \pm 3 / 2\rangle+15 \%\|\mp 5 / 2\rangle+15 \% \\ \| \pm 7 / 2\rangle+15 \%\| \pm 1 / 2\rangle+10 \%\|\mp 9 / 2\rangle \\ +10 \%\|\mp 1 / 2\rangle \end{gathered}$ | $\pm 2.5$ |
| 196.84 | 283.25 | 0.3 | 5.5 | 11.9 | 84.1 | $\begin{gathered} 19 \%\| \pm 1 / 2\rangle+16 \%\| \pm 3 / 2\rangle+13 \% \\ \| \pm 13 / 2\rangle+11 \%\|\mp 7 / 2\rangle+8 \% \\ \|\mp 5 / 2\rangle+7 \%\| \pm 9 / 2\rangle+7 \%\| \pm 7 / 2\rangle+ \\ 7 \%\|\mp 1 / 2\rangle+6 \%\|\mp 13 / 2\rangle \end{gathered}$ | $\pm 3.0$ |
| 226.41 | 325.80 | 1.3 | 4.1 | 13.1 | 60.5 | $\begin{gathered} 33 \%\| \pm 11 / 2\rangle+21 \%\| \pm 9 / 2\rangle+9 \% \\ \|\mp 7 / 2\rangle+7 \%\| \pm 13 / 2\rangle+7 \% \\ \|\mp 5 / 2\rangle+6 \%\|\mp 3 / 2\rangle \end{gathered}$ | $\pm 4.3$ |
| 300.09 | 431.84 | 0.2 | 0.6 | 18.4 | 85.1 | $\begin{gathered} 22 \%\| \pm 3 / 2\rangle+21 \%\|\mp 1 / 2\rangle+11 \% \\ \|\mp 5 / 2\rangle+9 \%\|\mp 11 / 2\rangle+8 \%\|\mp 9 / 2\rangle \\ +8 \%\| \pm 7 / 2\rangle+6 \%\| \pm 1 / 2\rangle+5 \% \\ \| \pm 5 / 2\rangle \end{gathered}$ | $\pm 2.5$ |

[^1]Table S9. Electronic structure of $\left[\mathrm{Dy}\left(\mathrm{Cp}^{\prime \prime \prime}\right)\left(\mathrm{BH}_{4}\right)_{3}\right]^{-}$(where $\mathrm{Dy}(4)$ is the central ion) calculated with the crystal field parameters obtained from CASSCF-SO using the solid state geometry of 5-Dy in zero-field. Each row corresponds to a Kramers doublet.

| $\begin{aligned} & \text { Energy } \\ & \left(\mathrm{cm}^{-1}\right) \end{aligned}$ | Energy (K) | $g_{\mathrm{x}}$ | $g_{y}$ | $g_{z}$ | $\begin{gathered} \text { Angle }^{\mathrm{a}} \\ \text { (deg) } \end{gathered}$ | Wavefunction | $\left\langle J_{z}>\right.$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.00 | 0.00 | 0.0 | 0.1 | 19.7 | -- | $97 \%\| \pm 15 / 2\rangle$ | $\pm 7.4$ |
| 103.70 | 149.23 | 0.5 | 1.1 | 17.0 | 52.3 | $\begin{aligned} & 28 \%\| \pm 9 / 2\rangle+21 \%\| \pm 11 / 2\rangle+15 \% \\ & \| \pm 13 / 2\rangle+12 \%\| \pm 7 / 2\rangle+6 \%\|\mp 5 / 2\rangle \end{aligned}$ | $\pm 4.6$ |
| 137.49 | 197.85 | 2.9 | 6.5 | 11.3 | 72.2 | $\begin{gathered} 26 \%\| \pm 7 / 2\rangle+22 \%\| \pm 5 / 2\rangle+15 \% \\ \|\mp 7 / 2\rangle+8 \%\|\mp 13 / 2\rangle+7 \% \\ \|\mp 11 / 2\rangle+6 \%\|\mp 9 / 2\rangle+5 \%\|\mp 5 / 2\rangle \end{gathered}$ | $\pm 3.6$ |
| 174.28 | 250.79 | 1.5 | 4.1 | 8.5 | 54.9 | $\begin{gathered} 18 \%\| \pm 3 / 2\rangle+14 \%\|\mp 13 / 2\rangle+12 \% \\ \|\mp 9 / 2\rangle+12 \%\| \pm 5 / 2\rangle+9 \%\| \pm 9 / 2\rangle \\ +7 \%\|\mp 3 / 2\rangle+6 \%\| \pm 7 / 2\rangle+5 \% \\ \|\mp 7 / 2\rangle \end{gathered}$ | $\pm 3.4$ |
| 203.70 | 293.13 | 0.1 | 1.0 | 9.2 | 44.6 | $\begin{gathered} 14 \%\| \pm 13 / 2\rangle+13 \%\|\mp 13 / 2\rangle+ \\ 12 \%\|\mp 9 / 2\rangle+10 \%\| \pm 7 / 2\rangle+10 \% \\ \|\mp 5 / 2\rangle+6 \%\|\mp 7 / 2\rangle+6 \%\| \pm 1 / 2\rangle+ \\ 6 \%\|\mp 1 / 2\rangle+5 \%\|\mp 11 / 2\rangle+5 \% \\ \pm 5 / 2\rangle+5 \%\|\mp 3 / 2\rangle \end{gathered}$ | $\pm 4.0$ |
| 223.85 | 322.12 | 0.4 | 4.4 | 11.1 | 47.5 | $\begin{gathered} 35 \%\| \pm 11 / 2\rangle+15 \%\| \pm 13 / 2\rangle+12 \% \\ \| \pm 1 / 2\rangle+9 \%\| \pm 9 / 2\rangle+7 \%\|\mp 1 / 2\rangle+ \\ 5 \%\|\mp 13 / 2\rangle+5 \%\|\mp 9 / 2\rangle+5 \% \\ \| \pm 3 / 2\rangle \end{gathered}$ | $\pm 4.2$ |
| 254.27 | 365.90 | 0.6 | 4.2 | 10.2 | 86.3 | $\begin{gathered} 19 \%\| \pm 3 / 2\rangle+13 \%\| \pm 5 / 2\rangle+13 \% \\ \|\mp 5 / 2\rangle+13 \%\| \pm 1 / 2\rangle+9 \%\|\mp 3 / 2\rangle \\ +8 \%\|\mp 7 / 2\rangle+6 \%\|\mp 11 / 2\rangle+5 \% \\ \| \pm 11 / 2\rangle \end{gathered}$ | $\pm 2.7$ |
| 286.71 | 412.58 | 1.0 | 4.4 | 14.4 | 84.2 | $\begin{gathered} 36 \%\| \pm 1 / 2\rangle+16 \%\| \pm 3 / 2\rangle+10 \% \\ \|\mp 11 / 2\rangle+10 \%\|\mp 1 / 2\rangle+7 \% \\ \|\mp 9 / 2\rangle+7 \%\|\mp 3 / 2\rangle \end{gathered}$ | $\pm 2.0$ |

[^2]
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[^0]:    ${ }^{\mathrm{a}}$ The angle between the $\mathrm{g}_{\mathrm{z}}$ value of the excited Kramers doublet and the ground Kramers doublet.

[^1]:    ${ }^{\mathrm{a}}$ The angle between the $\mathrm{g}_{\mathrm{z}}$ value of the excited Kramers doublet and the ground Kramers doublet.

[^2]:    ${ }^{\mathrm{a}}$ The angle between the $\mathrm{g}_{2}$ value of the excited Kramers doublet and the ground Kramers doublet.

